



ASTR 221 - Stars & Planets

Fall 2021

Mw 12:45-2:00 Sears Library 552

Bill Janesh

ASTR 221 — Stars and Planets

Time: Mondays & Wednesdays, 12:45 pm - 2:00 pm

Place: Sears Library 552 (the “Astronomy Classroom”)

Instructor: Bill Janesh **TA:** Ray Garner
bfj2@case.edu crg56@case.edu

Course Webpage: <http://astroweb.case.edu/bjanesh/astr221/> & Canvas for announcements and grades

Required Text: *Foundations of Astrophysics*, by Ryden and Peterson (ISBN 978-1-108-83195-6)

Other Useful Books: *Astronomy: A Physical Perspective, 2e*, by Kutner
Introduction to Modern Astrophysics, 2e, by Carroll and Ostlie

Grades: Homework: 45% *We will use the CWRU Standard Grading Scheme*
Midterm: 25% ($A \geq 90\%$ | $B \geq 80\%$ | $C \geq 70\%$ | $D \geq 60\%$ | etc.)
Final Exam: 30%

Course Description: Stellar structure and energy production. Formation and evolution of stars. Supernovae, neutron stars, and black holes. Star clusters. Planetary systems and the detection of extrasolar planets. The application of physical laws to the study of the universe.

Disability Accommodations: In accordance with federal law, if you have a documented disability, you may be eligible to request accommodations from Disability Resources. In order to be considered for accommodations you must first register with the Disability Resources office. Please contact their office at 216.368.5230 to register or get more information on how to begin the process. Keep in mind that accommodations are not retroactive.

Homework: There will be a total of 6 homework assignments. Collaborative discussion is permitted and encouraged, but **each person must turn in their own solutions with unique writeup/analysis**. Collaborative means talking with each other about approaches, techniques, etc., and *not* swapping final solutions to copy! **Submissions will be accepted on paper or in PDF format via Canvas**. Write-ups should be typed or *neatly* handwritten. For PDF submissions, scan your handwritten work properly (see homework tips page for suggestions) and please make an effort to merge all parts into a single file for submission. **Homework will generally be due in class** but see each assignment for specifics.

Exams: There will be one midterm and one final exam. **You are allowed one sheet of letter/A4-sized paper with notes on both sides**, but exam questions will ask you to synthesize information from what you know, not just work a problem or cite facts. You **may not** work collaboratively with your classmates, and I’ll only answer clarifying or format questions. The final exam is scheduled for 12/15 from 12-3pm, please register any time conflicts with Undergraduate Studies. *Academic integrity violations during an exam will result in, at minimum, the failure of the exam.*

Attendance/Late Policy: *Attendance:* you are **encouraged, but not required, to attend lectures**. I will be recording class audio, which will be posted on the course webpage along with slides and notes. *Late work:* **You get one free no excuse late homework (up to one week). All other late work loses 20% per day.** If you have an emergency or otherwise legitimate reason out of your control for missing a homework due date (illness, technology issues, etc.), please document this with your Navigator and me ASAP. We’ll then work out an alternate due date without penalty.

Computing: Some HW assignments will **require you to write and run code in Python** to solve astronomical problems. Don’t worry — we’ll spend at least one class getting more familiar with Python before I ask you to use it, but **ask for help if you need it**. Typed reports can easily be created using a Jupyter notebook, showing formatted text alongside code and math. *If you would like access to departmental computing resources, or have questions or concerns about this aspect of the course, please let me know as soon as possible.*

Office Hours: Mondays and Wednesdays the hour after class ends, and a 90 minute block on Thursday decided by class popular vote, or just drop in! Some questions can probably be answered via email; I will do my best to respond as soon as possible during normal business hours. If you have a question in person, please come prepared — for homework questions, you must attempt the problem on your own first! I will ask you to show me what you’ve tried before I answer questions. If you’re not sure where to start, see the homework tips page.

Ray - Tues: 10-11 Fri 2-3

	Date	General Topic	Ryden & Peterson Readings	Due
WEEK 1	Aug 23	Introductions; Orbits and Kepler's Laws	2.3, 2.5, 3.1	
	Aug 25	Orbits and Kepler's Laws; Gravity; Tides	3.1-3.4, 4.2, 4.3	
WEEK 2	Aug 30	The Sky; Constellations	1.3-1.6, 2.1, 2.2	
	Sept 1	Celestial Sphere; Coordinate Systems	1.1, 1.2	
WEEK 3	Sept 6	Labor Day (no class)		
	Sept 8	Light; Radiation; Blackbodies; Spectra	5.1-5.7	HW1
WEEK 4	Sept 13	Astronomical Techniques; Telescopes	6.1-6.7	
	Sept 15	Python Introduction	bring a computer!	
WEEK 5	Sept 20	The Sun; Hydrostatic Equilibrium	7.1-7.3, 14.1	
	Sept 22	Distances, Magnitudes, Colors	13.1-13.2	HW2
WEEK 6	Sept 27	Spectral Types; The H-R Diagram	13.3-13.6, 14.2-14.4	
	Sept 29	Velocities; Binary Stars; Stellar Masses	13.5	
WEEK 7	Oct 4	Nuclear Fusion; Energy Transport in Stars	15.1-15.4	
	Oct 6	Low Mass Stellar Evolution	17.2	HW3
WEEK 8	Oct 11	Review!		
	Oct 13	Midterm Exam	don't forget your notes sheet!	
WEEK 9	Oct 18	Fall Break (no class)		
	Oct 20	High Mass Stellar Evolution; Supernovae	17.3	
WEEK 10	Oct 25	White Dwarfs, Neutron Stars, Black Holes	18.1-18.4	
	Oct 27	Star Clusters	14.2-14.4, 17.2, 17.3	HW4
WEEK 11	Nov 1	Interstellar Medium; Star Formation	16.1-16.3, 17.1	
	Nov 3	Star Formation	17.1	
WEEK 12	Nov 8	Solar System Formation	8.1-8.3, 12.2	
	Nov 10	The Earth and Moon	9.1-9.5	HW5
WEEK 13	Nov 15	Rocky Planets; Interior Processes	10.1	
	Nov 17	Moons; Comets; Asteroids; Tiny Things	11.1-11.4	
WEEK 14	Nov 22	Atmospheres; Gas Giants	10.2-10.3, 9.2	
	Nov 24	Gas Giants	10.2-10.3	
WEEK 15	Nov 29	Exoplanets	12.3-12.4	
	Dec 1	Exoplanets	12.3-12.4	HW6
	Dec 15	Final Exam 12-3pm	don't forget your notes sheet!	

8/23 Orbits & Kepler's Laws

How did astronomy become a thing?

Navigation, time, seasons, religion

What's that stuff in the sky?

Gravity.

Why am I here?

Geocentric Model

(E)

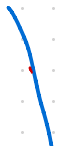
○ Moon



Mercur



Venus



Sun



Mars



Jupiter



Saturn

circular orbits

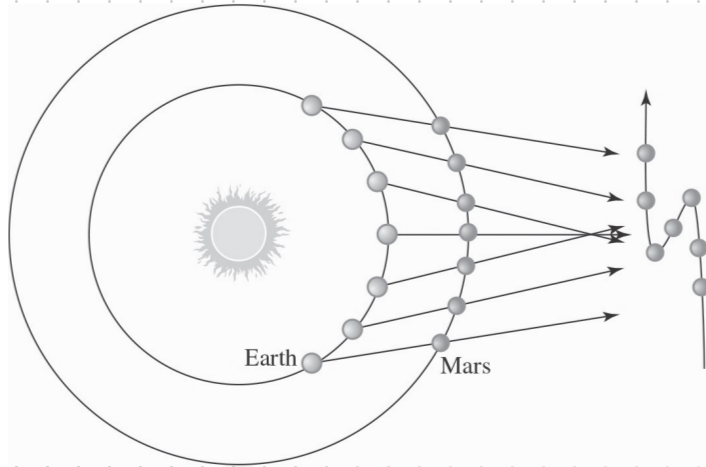
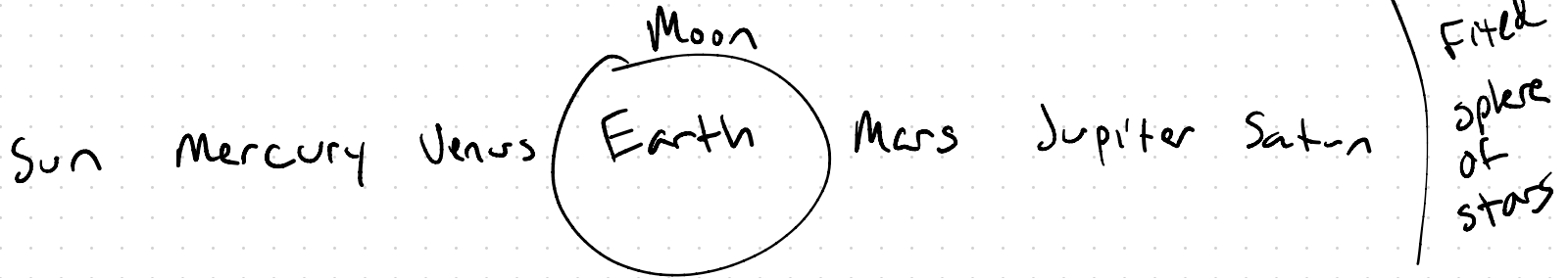
Fixed Sphere of Stars



retrograde Motion ?

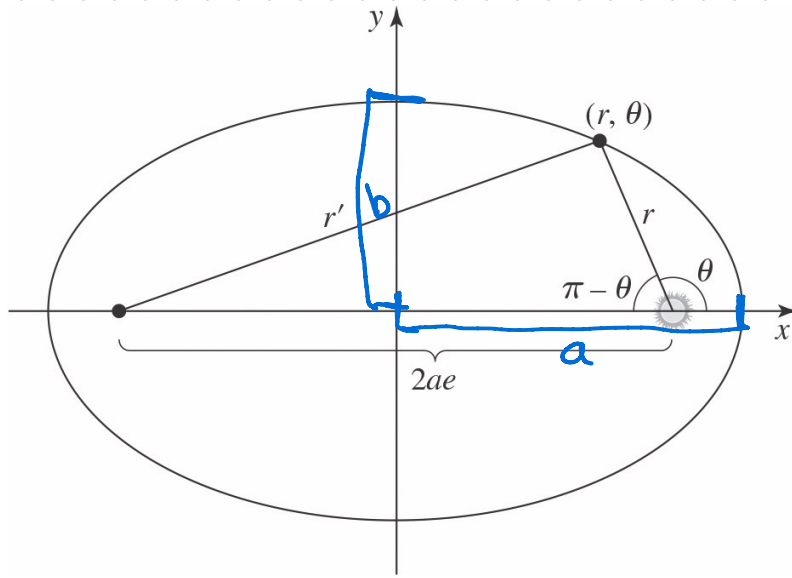
Simplify?

Helio-centric Model



Kepler's 1st Law

planets orbit in ellipses, with the Sun at one focus of the ellipse



a semi-major axis

b semi-minor axis

e ellipticity / eccentricity

$$= \sqrt{1 - \left(\frac{b}{a}\right)^2}$$

$e = 0$ circle

$e = 1$ straight line

periapsis (closest approach to star)

perihelion

perigee

periastron

perigalacticon

$$r_p = a(1 - e)$$

apoapsis (furthest)

aphelion

apogee

apastron

$$r_a = a(1 + e)$$

$$e_{\text{Earth}} = 0.017$$

Astronomical Unit (AU)

"mean distance between Earth & Sun"

150 million km & 93 million miles

semi-major axis of Earth's orbit

$$a = 1.0 \text{ AU}$$

	a	e	P
Mercury	0.39 AU	0.205	0.24 years
Venus	0.72	0.007	0.62
Earth	1.0	0.017	1.0
Mars	1.52	0.093	1.88
Jupiter	5.20	0.048	11.86
Saturn	9.54	0.054	29.45
Uranus	19.19	0.047	84.02
Neptune	30.07	0.009	164.8
Pluto	39.45	0.250	247.9
Comets	varies	0.75-0.995	varies

Kepler's 3rd Law

"for all planets, the orbital period squared divided by the semi-major axis cubed is constant."

$$p^2 \propto k a^3$$

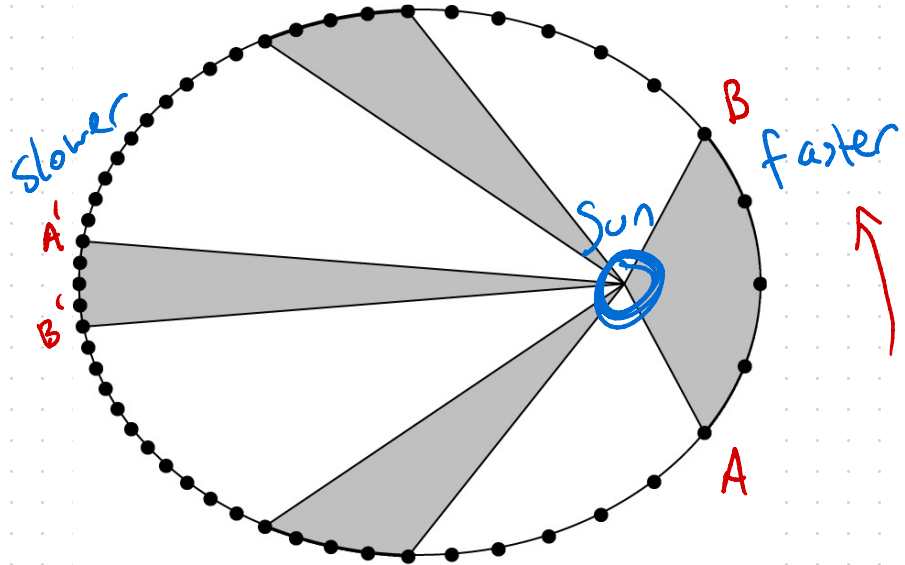
years AU

Kepler's 2nd Law

The Law of Equal Areas

"The line connecting a planet & the Sun sweeps out equal areas in equal amounts of time!"

planets move
faster in their orbits
when they are
closer to the Sun

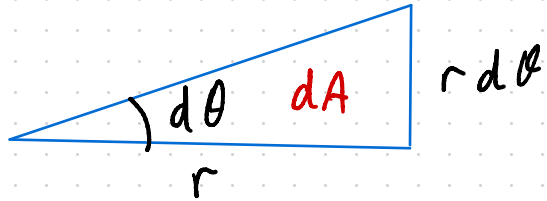


Kepler's 1st Law Revisited

The Earth does not orbit the Sun. (?)

Each object moves on an ellipse w/ COM
at one focus of the ellipse.

Kepler's 2nd Law Revisited



$$dA = \frac{1}{2} r (r d\theta)$$

$$\vec{L} = m (\vec{r} \times \vec{v})$$

$$\Rightarrow L = m r v_{\theta} \quad \frac{L}{m} = r v_{\theta}$$

$$\frac{dA}{dt} = \frac{1}{2} r \left(r \frac{d\theta}{dt} \right)$$

$$= \frac{1}{2} r v_{\theta}$$

$$\frac{dA}{dt} = \frac{1}{2} \frac{L}{m}$$

constant

Kepler's 3rd Law Revisited

$$G = 6.67 \times 10^{-11} \frac{\text{m}^3}{\text{kg s}^2}$$

$$F_g = \frac{GMm}{r^2}$$

$$F_{\text{cent}} = \frac{mv^2}{r}$$

$$\frac{GMm}{r^2} = \frac{mv^2}{r}$$

$$v = \frac{2\pi r}{P}$$

$$r = \frac{M}{m+M} r$$

$$\frac{GMm}{r^2} = \frac{m \cdot 4\pi^2 r}{P^2}$$

$$\frac{GM}{r^2} = \frac{4\pi^2}{P^2} \frac{M}{m+M} r$$

$$G = 4\pi^2 \frac{AU^3}{M_{\odot} \text{yr}^2}$$

$$P^2 = \frac{4\pi^2}{G(m+M)} r^3 = a^3$$

Does an orbit have to be an ellipse
or a circle?

Orbital Classification

closed

v

$$E_{\text{tot}} < 0$$

kinetic < potential

bound

circular, elliptical

open

$$E_{\text{tot}} > 0$$

kinetic > potential

unbound

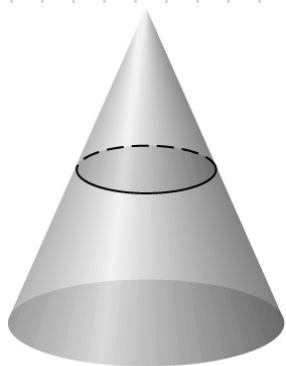
hyperbola

"critical"

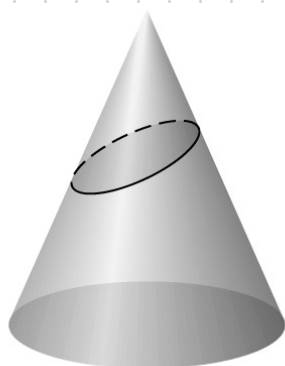
$$E_{\text{tot}} = 0$$

kinetic = potential

parabolic



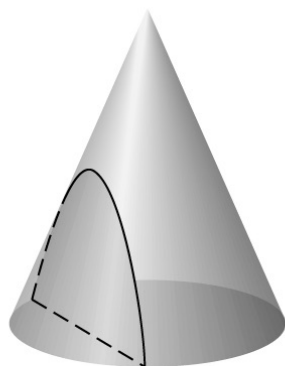
Circle



Ellipse

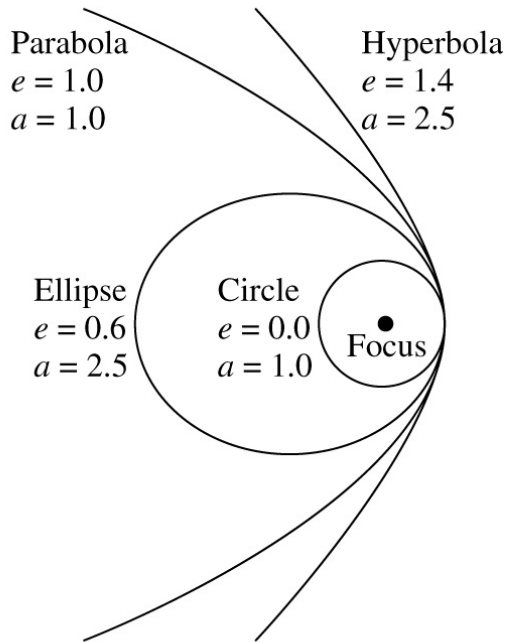


Parabola



Hyperbola

(a)



(b)

Gravitational Potential Energy

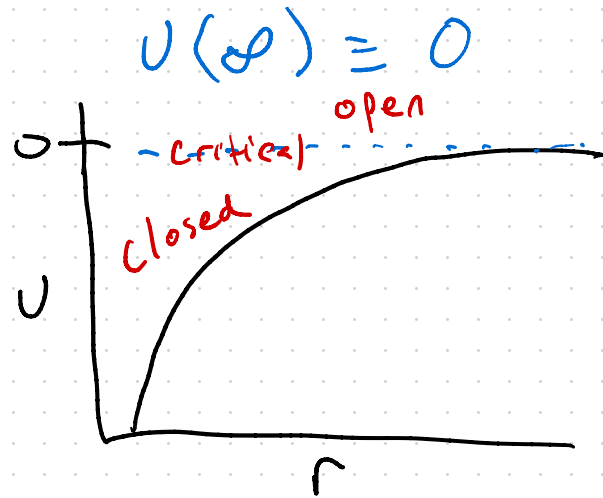
push it away from the sun

$$\Delta U = - \int_{\vec{r}_i}^{\vec{r}_f} \vec{F} d\vec{r} = - \int_{r_i}^{r_f} G \frac{Mm}{r^2} dr$$

$$U_f - U_i = -GMm \left(\frac{1}{r_f} - \frac{1}{r_i} \right)$$

$$U = - \frac{GMm}{r}$$

$$K = \frac{1}{2} M v_{\text{planet}}^2$$



$$K + U = \text{constant}$$

$$E_{\text{tot}} = \frac{1}{2} m v^2 - \frac{G M m}{r}$$

$$0 = \frac{1}{2} m v_{\text{esc}}^2 - \frac{G M m}{r}$$

$$v_{\text{esc}} = \left(\frac{2GM}{r} \right)^{1/2}$$

$$N_c = \frac{2\pi a}{P}$$

$$P^2 = \frac{4\pi^2}{GM} a^3$$

$$N_c^2 = \frac{4\pi^2 a^2}{P^2}$$

$$N_c^2 = \frac{4\pi a^2}{4\pi a^3} GM \Rightarrow N_c^2 = \frac{GM}{a}$$

$$E_{\text{tot}} = \frac{1}{2} m v^2 - \frac{GMm}{a}$$

$$= \frac{1}{2} m \frac{GM}{a} - \frac{GMm}{a}$$

$$= -\frac{GMm}{2a}$$

$$K = \frac{1}{2} U$$

Generalized orbital speed

$$\frac{1}{2} m v^2 - \frac{GMm}{r} = -\frac{GMm}{2a}$$

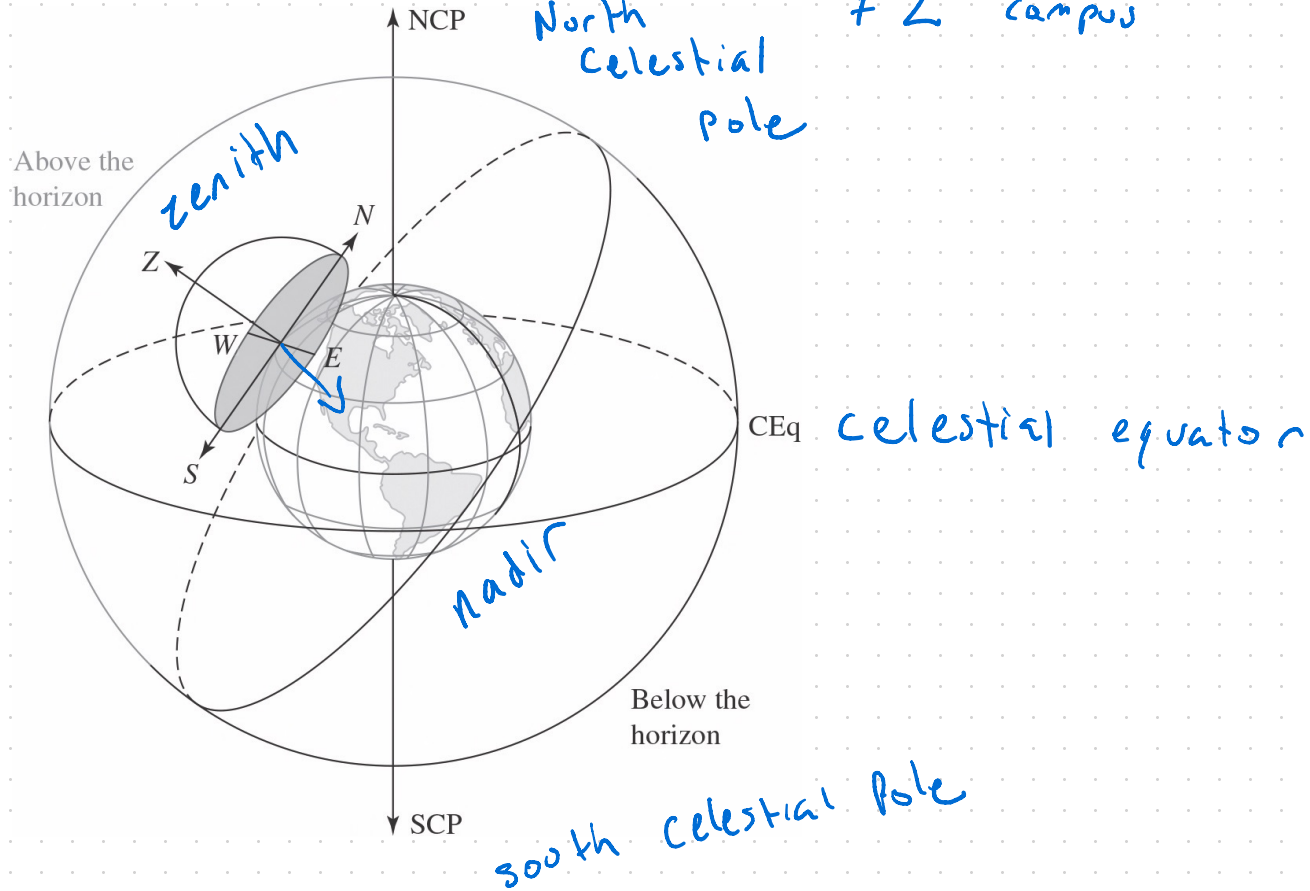
$$\frac{1}{2} m v^2 = \frac{GMm}{r} - \frac{GMm}{2a}$$

$$v^2 = GM \left(\frac{2}{r} - \frac{1}{a} \right)$$

$$\text{perihelion } v_p^2 = \frac{GM}{a} \left(\frac{1+e}{1-e} \right)$$

$$\text{aphelion } v_a^2 = \frac{GM}{a} \left(\frac{1-e}{1+e} \right)$$

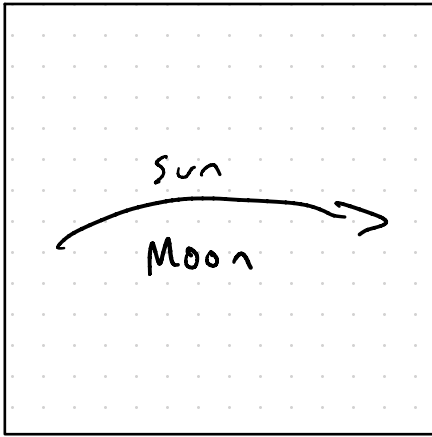
The Sky



+ 6

+ 2 campus

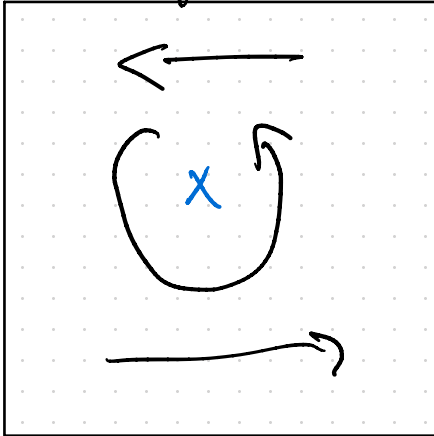
E



W

looking South

W



E

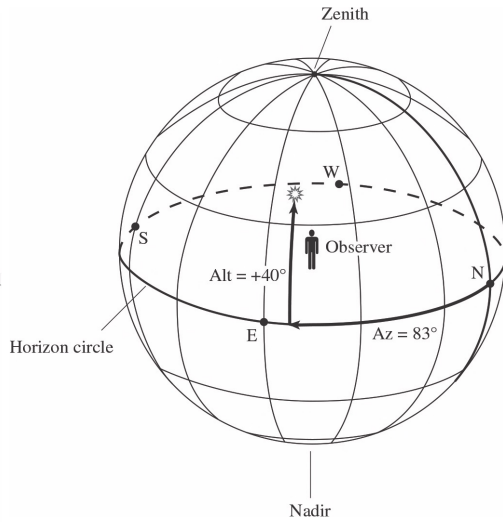
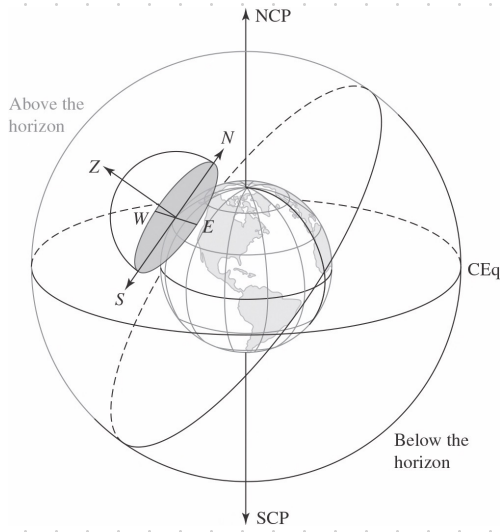
looking North



circumpolar stars

$$\text{Latitude} > 90^\circ - \phi$$

42



Altitude - Azimuth
 "Horizon" System
 latitude - longitude

Equatorial Coordinates

- aligned to Earth's system

$$\begin{matrix} \circ & \circ & \circ \\ (\theta, \phi, r) \end{matrix}$$

- $\theta, \phi = 0, 0 \rightarrow$ where the ecliptic @ equator cross on the vernal equinox \perp

- declination (latitude) δ degrees

RA - right ascension (longitude) α hours ???

1 hour = 15 degrees

hours degrees

minutes = arcminutes $\frac{1}{60}$ degree

seconds = arcseconds $\frac{1}{60}$ arcminute

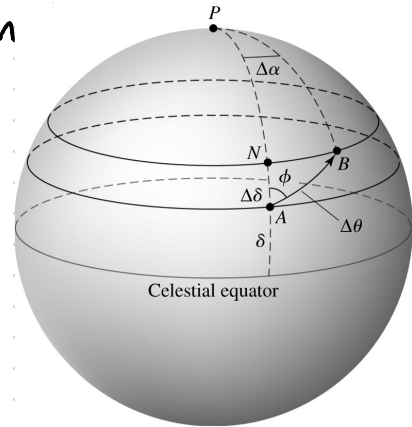
(5h 55^m 12^s, 12° 15' 25")

Angular separation ($\Delta\theta$) degrees, arcmin

$$\Delta\alpha = \Delta\theta \frac{\sin\phi}{\cos\delta}$$

$$\Delta\delta = \Delta\theta \cos\phi$$

$$(\Delta\theta)^2 = (\Delta\alpha \cos\delta)^2 + (\Delta\delta)^2$$



Sidereal Time

the amount of "clock time" since the vernal equinox crossed the meridian

the RA coordinate of a star crossing the meridian at a given point in time

meridian = the line that passes through North, zenith, South perpendicular to horizon

Betelgeuse = 5h 55m

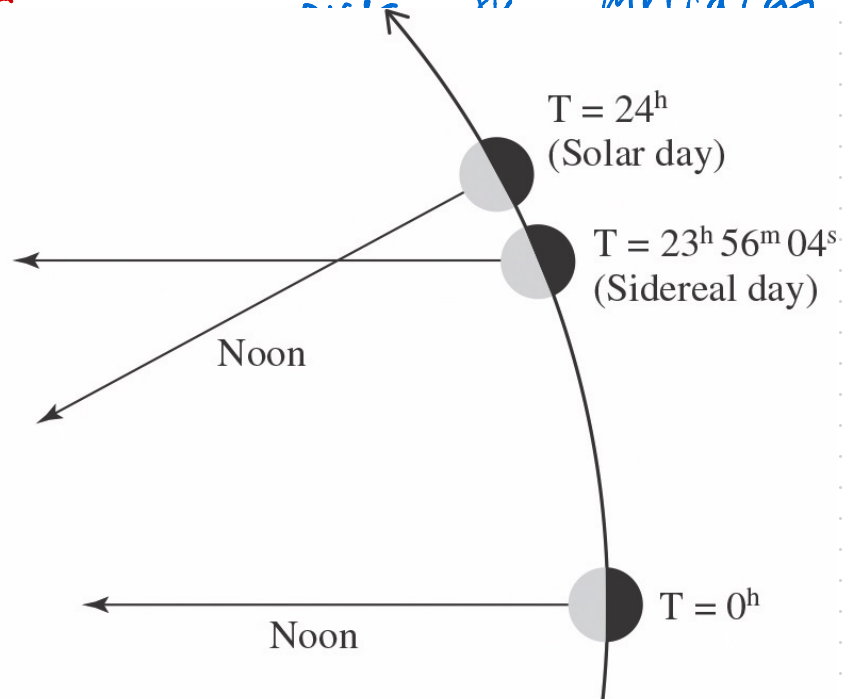
Sidereal Day

length of time
between successive
crossings of the
vernal equinox meridian

23^h

Solar Day

length of time
between successive
crossings of the Sun
meridian



Light

What is light?

"Sometimes" it's a wave

"Sometimes" it's a particle \rightarrow photon
(no mass)

Fast! 3×10^8 m/s
 3×10^5 km/s

Energy

some behavior can be described by a wave \rightarrow
" " " " " " " " " " particle how?

wave

wavelength

double-slit experiment

Doppler effect

antenna

particle

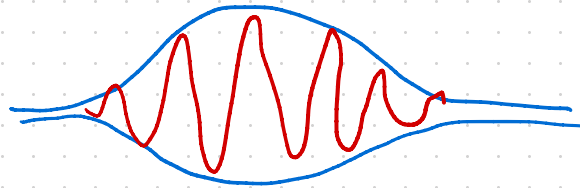
photo electric effect

travel over long distances

momentum

$$E = pc$$

gravity



Electromagnetic Spectrum

$$\lambda \cdot f = c$$

wavelength
length

frequency
1/time

speed of light
length/time

EM bands

Gamma Rays

high f

$$\lambda < 1 \text{ nm}$$

X-rays

$$1 \text{ nm} < \lambda < 10 \text{ nm}$$

UV

$$10 \text{ nm} < \lambda < 400 \text{ nm}$$

Visible (Optical)

$$400 \text{ nm} < \lambda < 700 \text{ nm}$$

IR

$$700 \text{ nm} < \lambda < 1 \text{ mm}$$

Micro-wave

$$1 \text{ mm} < \lambda < 10 \text{ cm}$$

Radio

low f

$$10 \text{ cm} > \lambda$$

$$\text{Angstrom} = 0.1 \text{ nm}$$
$$\text{\AA} = 1 \times 10^{-10} \text{ m}$$

Why is
light useful?

elemental composition

direction of motion

presence of light-emitting objects

temperature

density

Kirchoff's Laws

1. a hot, dense gas or solid object emits a continuous spectrum "all wavelengths, unbroken"

2. hot, diffuse gas produces bright spectral lines "emission spectrum"

3. a cool, diffuse gas in front of a continuous spectrum produces dark spectral lines → "absorption spectrum"

HW 2 now due 9/27 @ 2pm

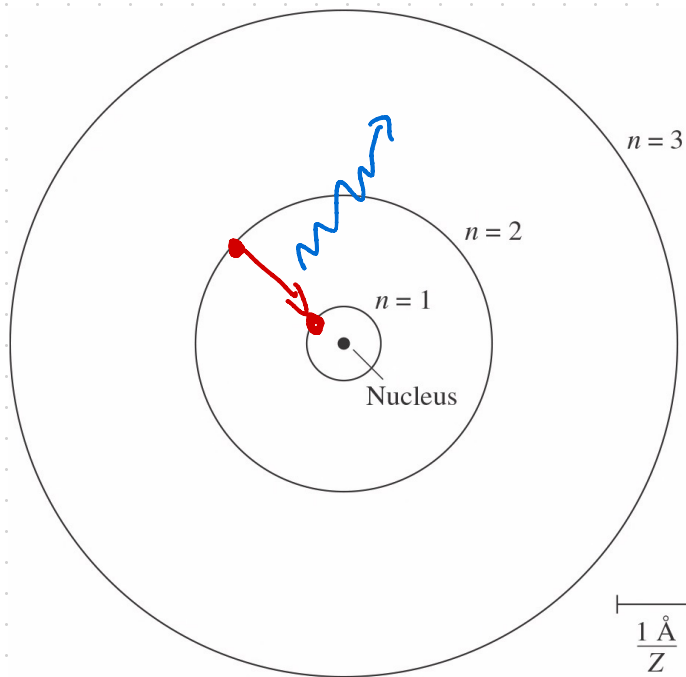
Python Intro Wednesday 9/15

Hydrogen

$$E_n = \frac{-13.6 \text{ eV}}{n^2}$$

$$\Delta E = E_f - E_i$$

$$= E_1 - E_2$$

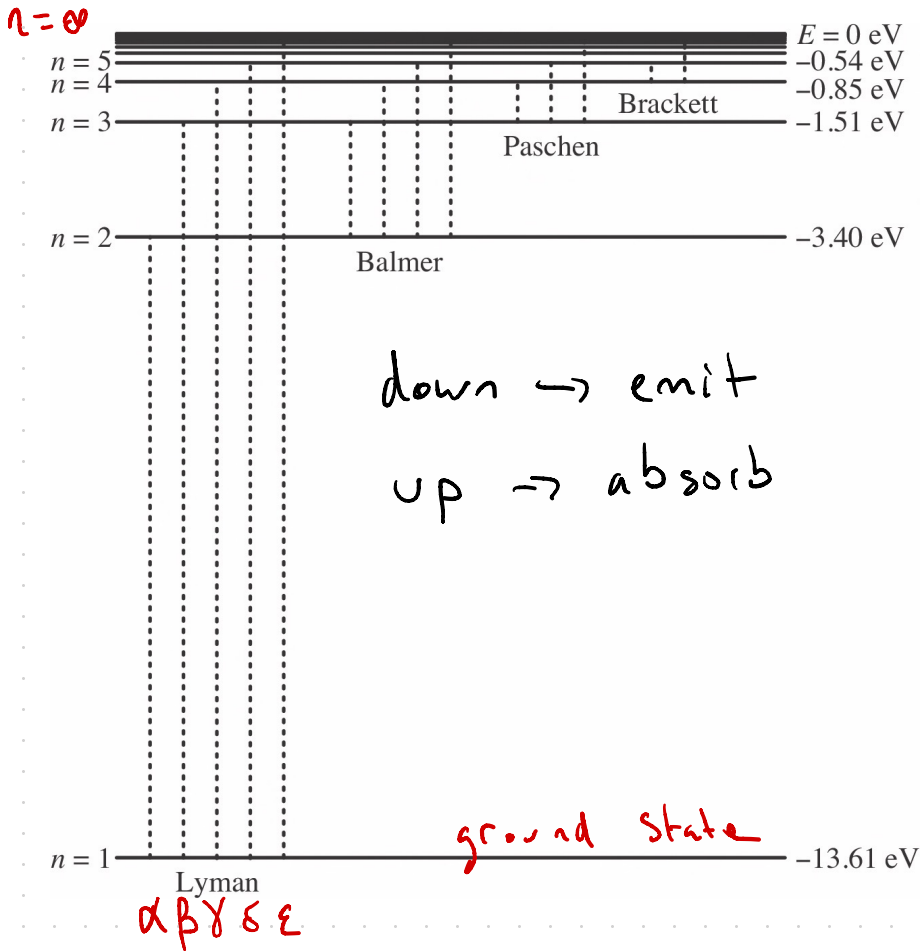


$$E_\gamma = hf$$

h = planck constant
 $6.626 \times 10^{-34} \text{ J}\cdot\text{Hz}$

$$E_\gamma = \frac{hc}{\lambda}$$

$$\Delta E_{if} = \frac{hc}{\lambda}$$



Balmer Series

$$n = 2 \leftrightarrow 3 \quad H\alpha \quad 656.3 \text{ nm}$$

$$n = 2 \leftrightarrow 4 \quad H\beta \quad 486.1 \text{ nm}$$

$$n = 2 \leftrightarrow 5 \quad H\gamma \quad 434.0 \text{ nm}$$

$$n = 2 \leftrightarrow 6 \quad H\delta \quad 410.2 \text{ nm}$$

ionization

collisional excitation

kinetic energy

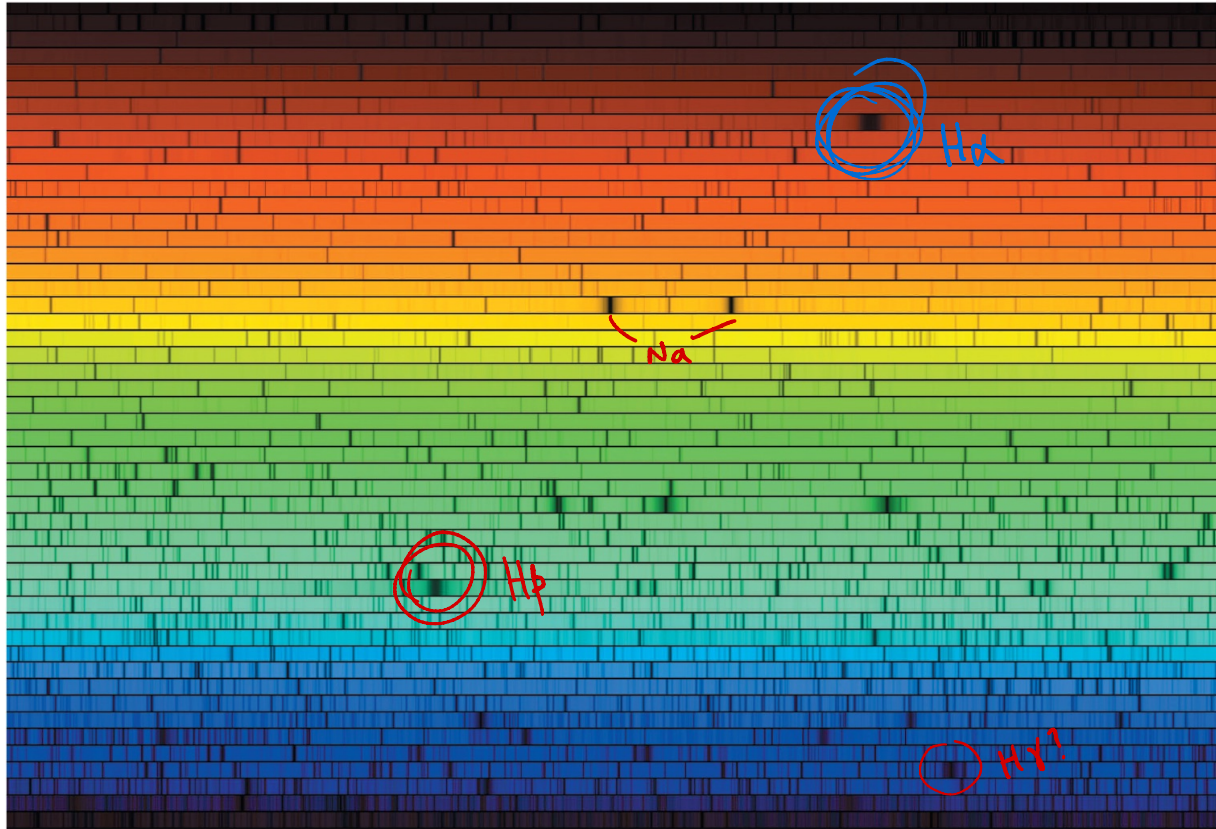
$$K = \frac{1}{2} m v^2$$

continuous = rainbow

IR

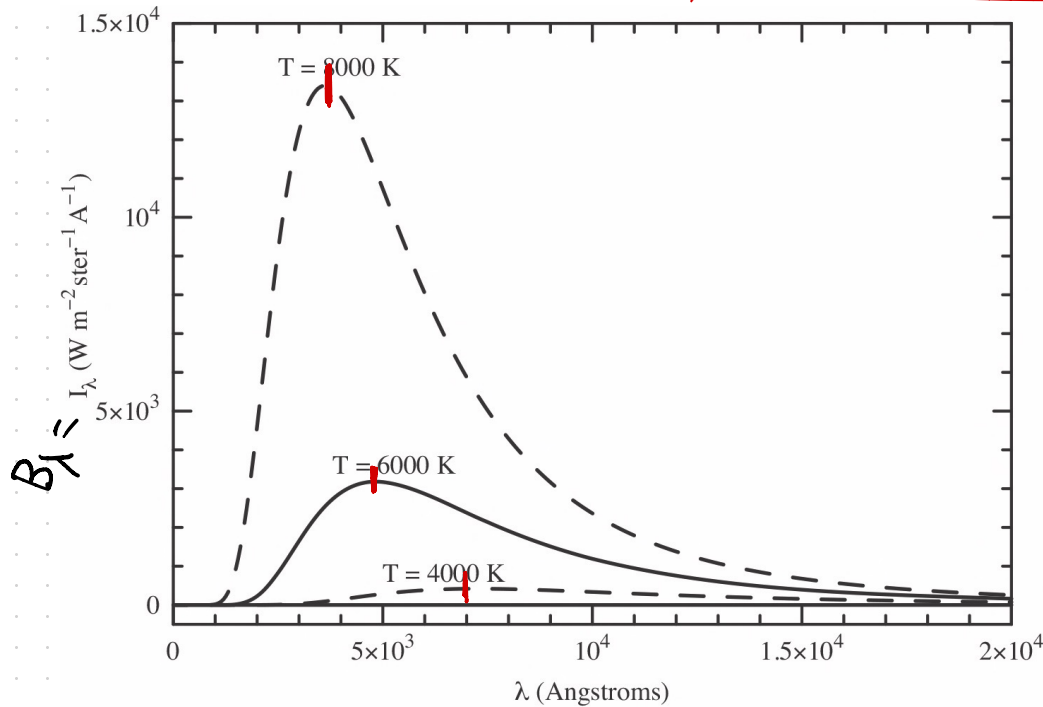
Visible

UV



"ideal emitter" - absorbs all the light that is incident upon it, then reradiates the same amount of energy in a characteristic spectrum

"black body"



Wien's Law

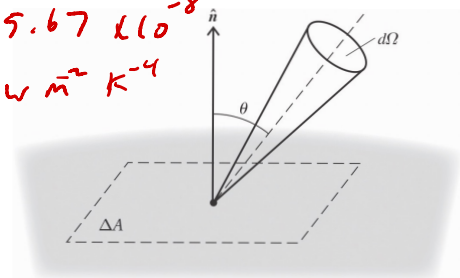
$$\lambda_{\text{max}} = \frac{0.0029 \text{ m} \cdot \text{K}}{T}$$

Luminosity

$$L = A \sigma T^4$$

$\sigma =$ Stefan-Boltzmann constant

$$5.67 \times 10^{-8} \text{ W m}^{-2} \text{K}^{-4}$$



Planck Equation

$$B_{\lambda}(T) = \frac{2hc^2/\lambda^5}{e^{(hc/\lambda kT)} - 1}$$

↑
Intensity

h = Planck

k = Boltzmann

c = Speed of light

$$L_{\lambda} d\lambda = B_{\lambda}(T) d\lambda dA \cos \theta d\Omega$$

$\text{W} \quad \text{m}^2 \quad \text{sr}$

Telescopes

what is a telescope?

why is it useful (for astronomy)?

lenses & mirrors

Magnification / Resolution

Different EM bands

see to further distances

Light Gathering Power

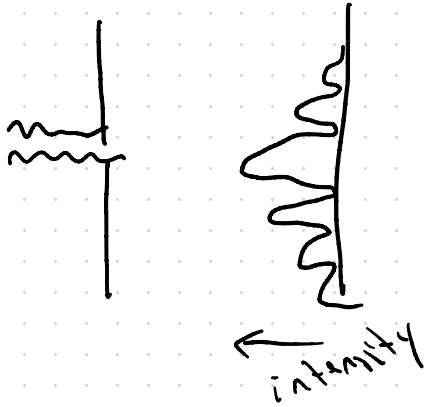
$$LGP \propto d^2 = A_{\text{re}}$$

bigger is
better

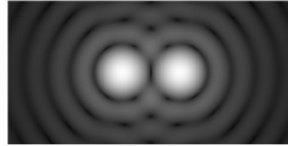
Resolution "see more detail"

smaller is better

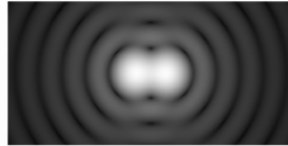
Limited by diffraction of light



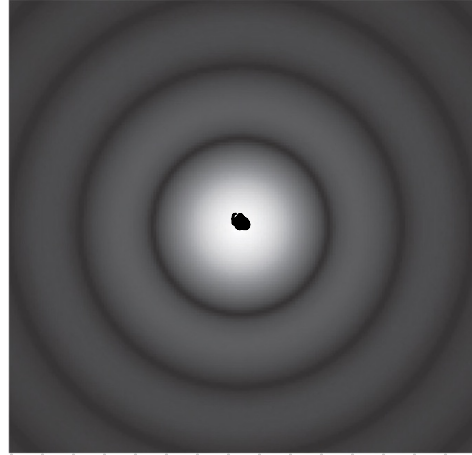
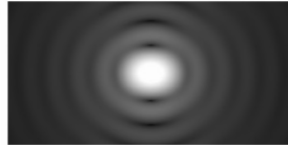
easily



just



not



wavelength of light

Airy Disk

Rayleigh Criterion

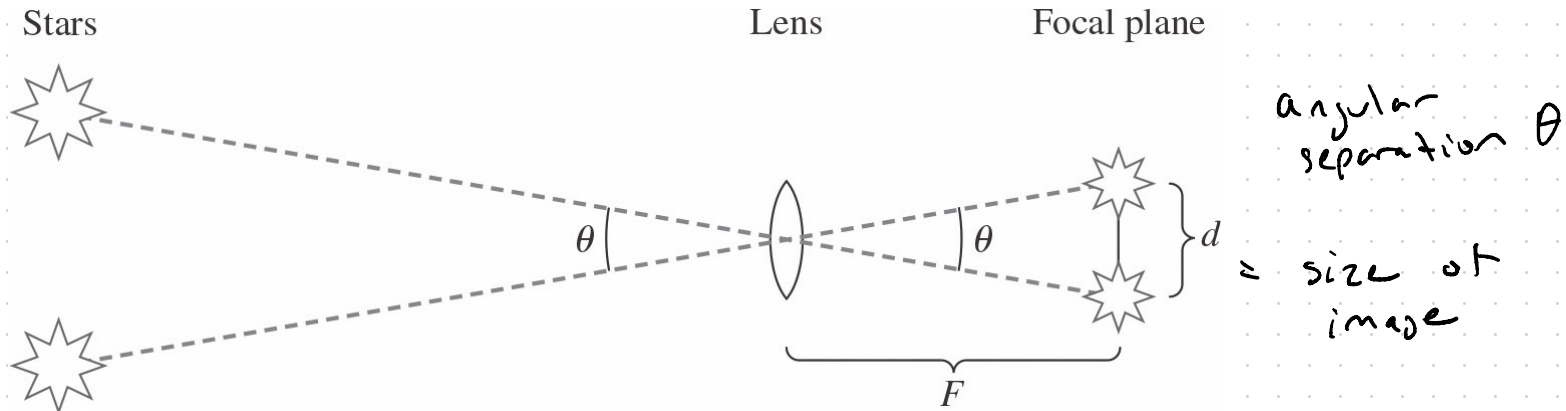
"minimum resolvable angular distance between two objects"

two objects are just resolved when the central maximum overlaps the 1st minimum of the other

$$\theta_{\min} = \frac{1.22 \lambda}{D}$$

aperture diameter

Simplest possible design - a single lens



$$\tan \theta = \frac{d}{F}$$

$$\tan \theta \approx \theta$$

radians

$$\theta = \frac{d}{F}$$

$$\theta = 206,265 \frac{d}{F}$$

focal length

How far away

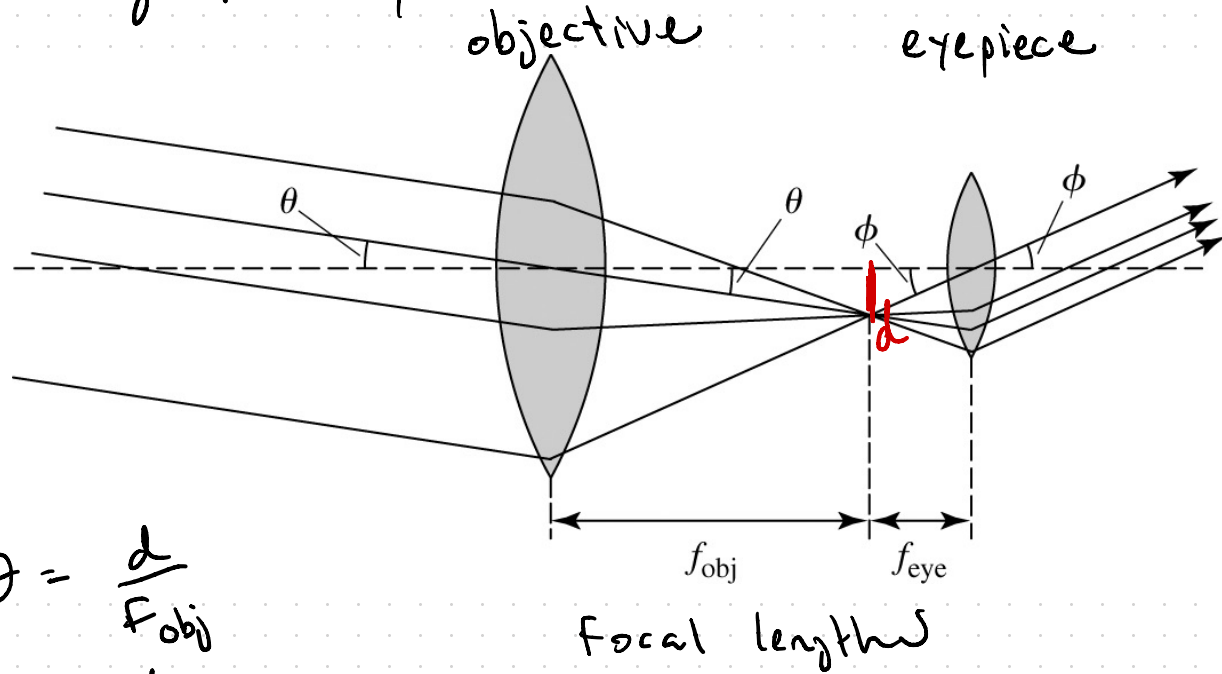
from lens is image
in focus

$$\frac{180^\circ}{\pi} \times \frac{3600''}{10}$$

plate scale

$$s = \frac{\theta}{d} = \frac{206265''}{F \text{ (cm)}}$$

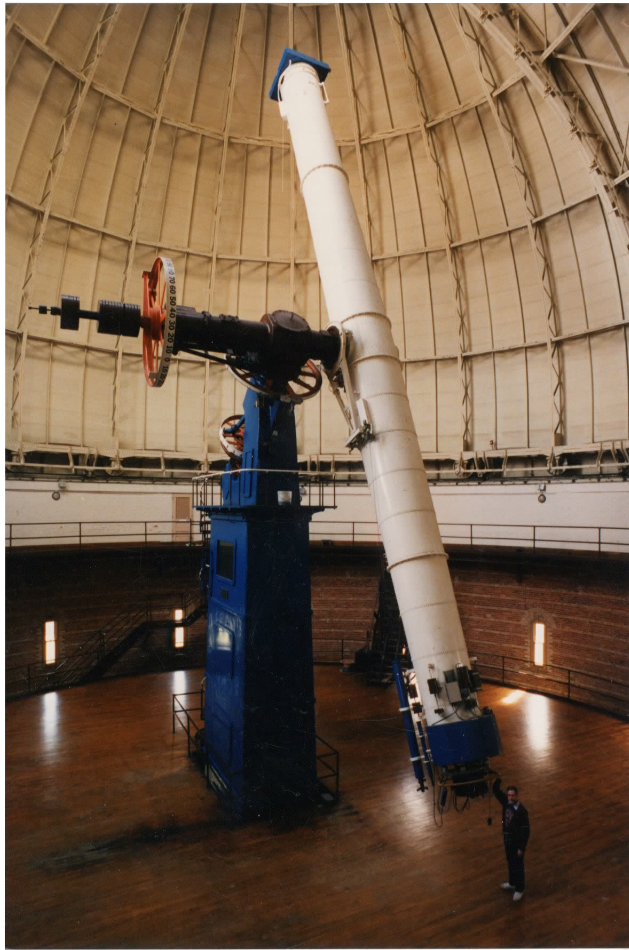
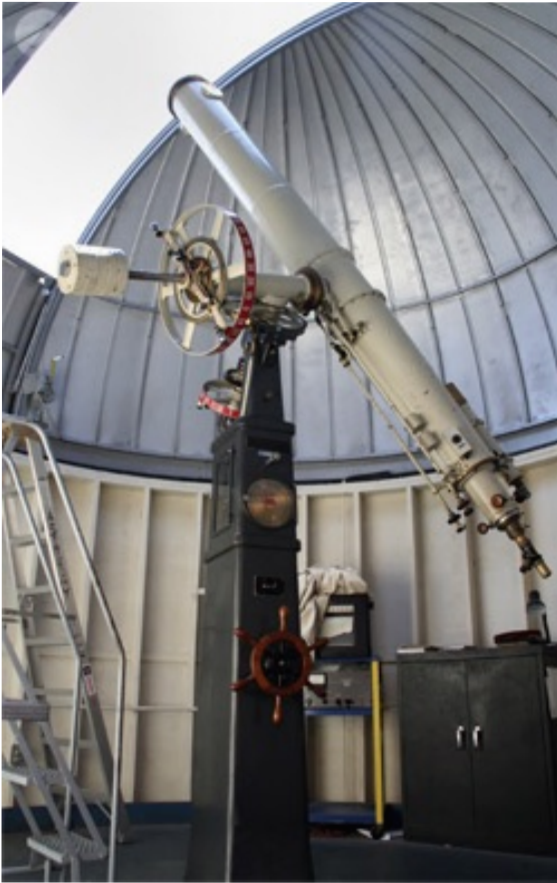
Refracting Telescope



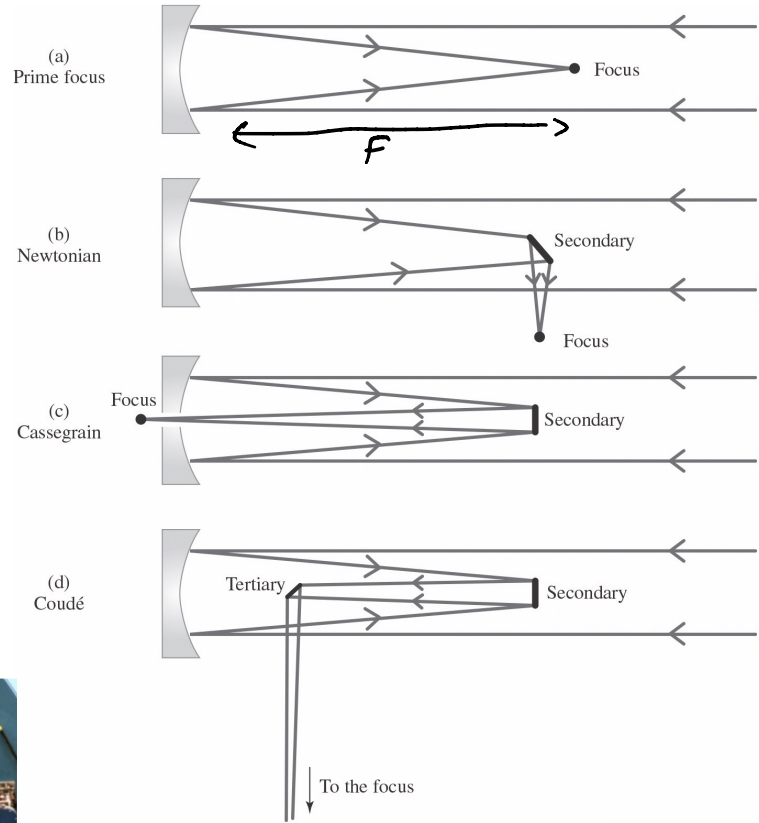
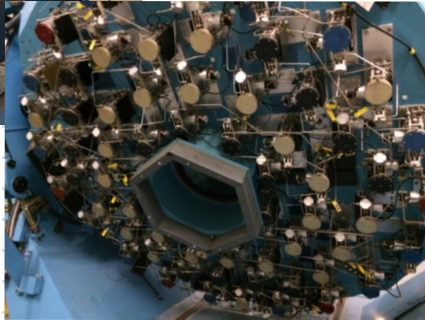
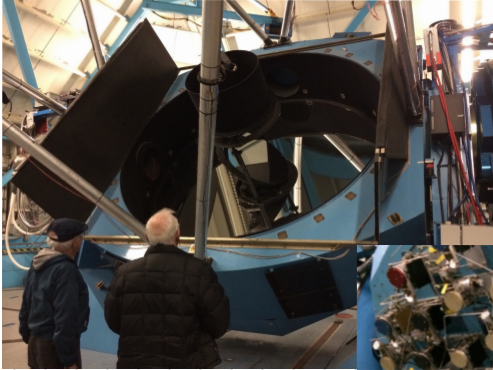
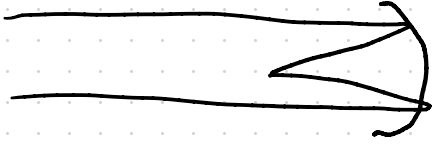
$$\tan \theta = \frac{d}{f_{obj}}$$

$$\tan \phi = \frac{d}{f_{eye}}$$

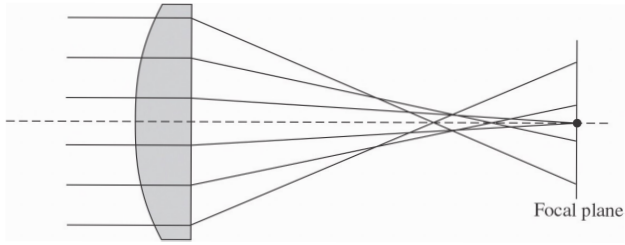
$$\frac{\phi}{\theta} = \frac{f_{obj}}{f_{eye}} = m \quad \text{magnification}$$



Reflecting telescope

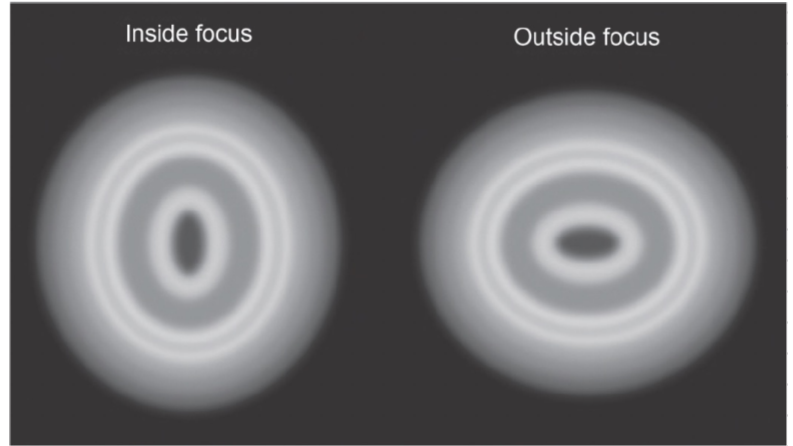
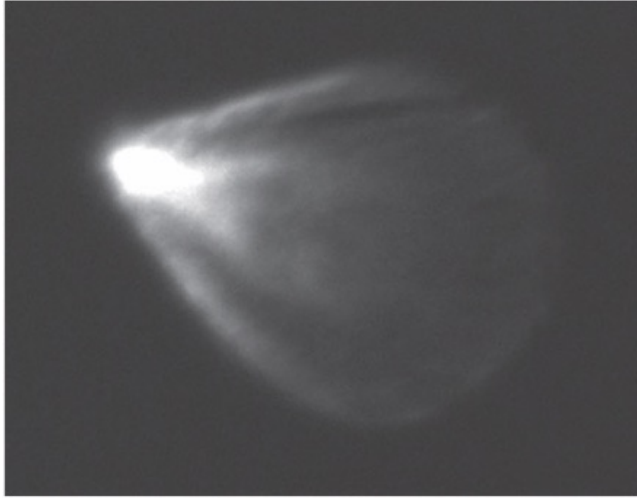


Spherical aberration




astigmatism

coma



Hybrid design

Schmidt-type
 lens

 mirror

Ritchey-Chrétien

hyperboloid mirrors

Practical considerations

funding

logography

demand

clouds

damage

manufacturing

mounting design

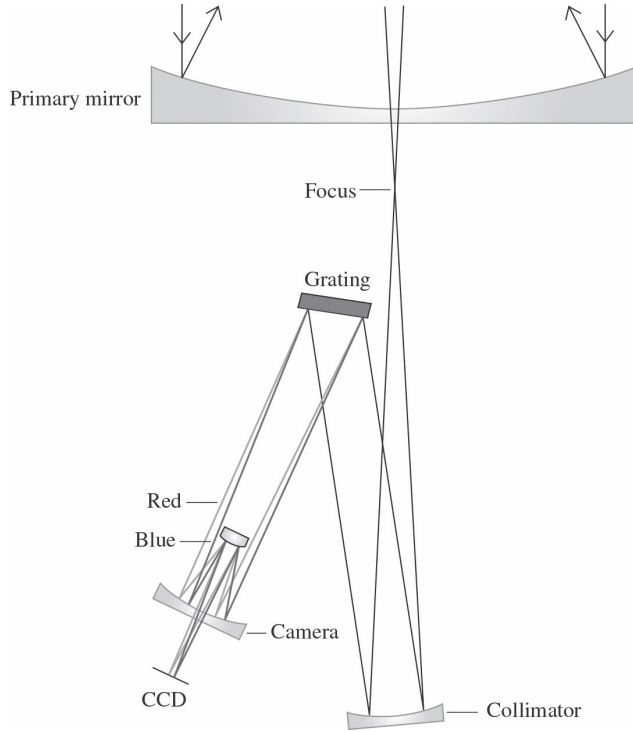
type of observation

training

light pollution

atmosphere

Spectrographs



disperse light by wavelength
using prisms or gratings

gratings more common in
modern applications → reflective
transmission

works by diffraction

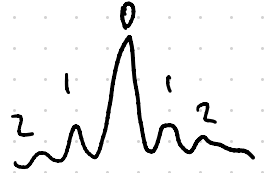
$$d \sin \theta_m = m \lambda$$

slit
spacing

angle
of
diffracted
light

integer
order

wavelength



Resolution $R = \frac{\lambda}{d\lambda}$ wavelength
distance between
distinguishable features

Detectors

the human eye

photographic emulsions
(film / plates)

photoelectric effect devices

- photoemissive
multiplier tubes

- photoconductive
charge-coupled devices (CCDs)

Quantum Efficiency

"how many incident photons
do you detect?"

eyes - ~~10%~~ 1%

film - 1%

multiplier
tubes - 10%

CCDs - 80%

over
visible
range

what are advantages of "artificial" detectors
over the human eye?

CCDs

grids of capacitive "wells" that collect charge
produced via photoelectric effect

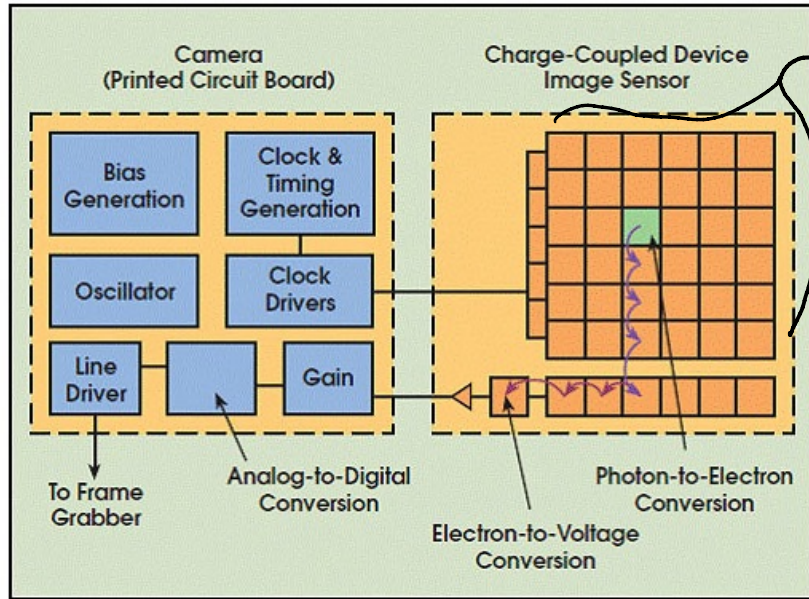


image detecting grid

photons \rightarrow
electrons

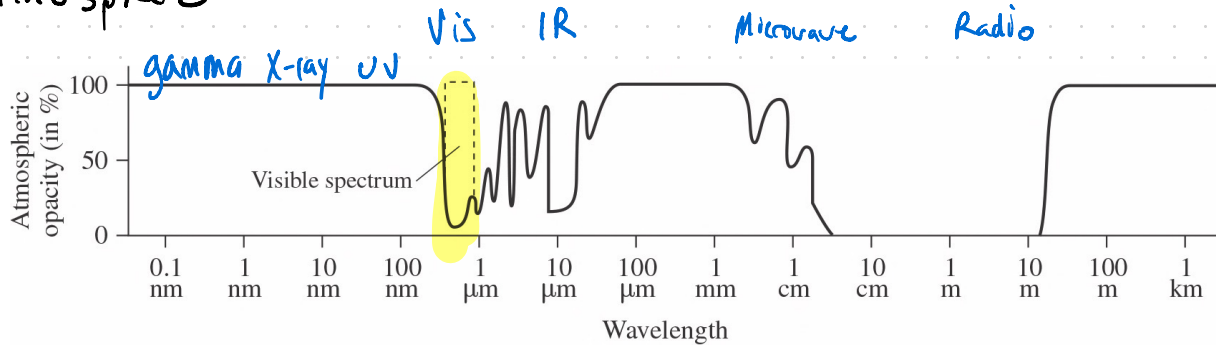
shift charge
down by rows into

readout register

then measure
voltage in
each column

and convert to digital image

The Atmosphere



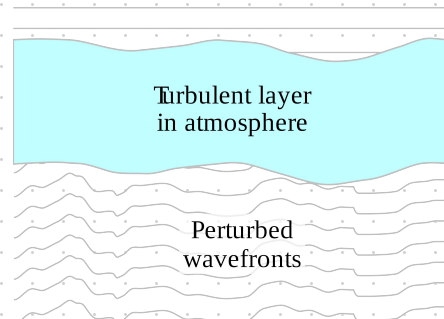
Most of EM spectrum is blocked by atmosphere

light that does make it through is blurred

by atmospheric refraction producing an effect

called "seeing"

Plane waves from distant point source



turbulent layer always changing so amount of blurring constantly varies

Interferometry

Combining images from multiple telescopes to create an image with higher resolution.

usually used in radio astronomy to improve resolution at very long wavelengths

$$\theta_{\min} = \frac{1.22 \lambda}{D}$$

Resulting image has same resolution as a single dish with size = separation between the smaller telescopes!

but not the same light gathering power!

Angular Size

1 full circle 360°

1 degree = $60'$

1 arcmin = $60''$

Sizes of things in sky

sky 180°

big dipper 24°

thumb @ arms length 1°

moon / sun $30' = 0.5^\circ$

Jupiter $40''$

naked eye limit $30''$

atmospheric turbulence
"seeing" $1''$ $0.5''$

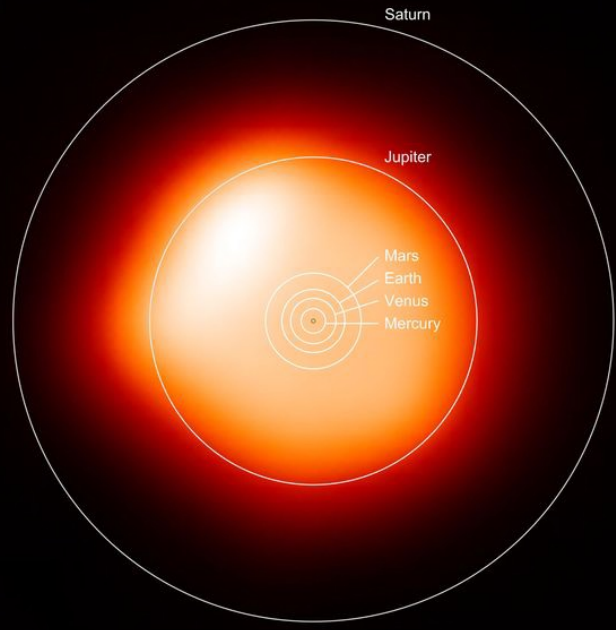
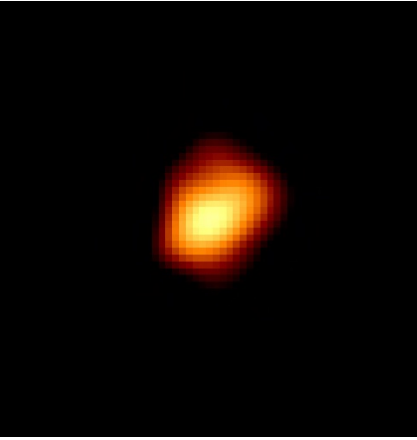
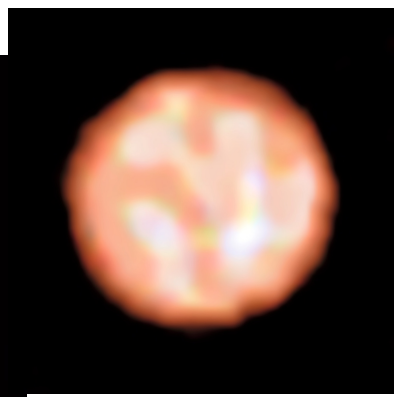
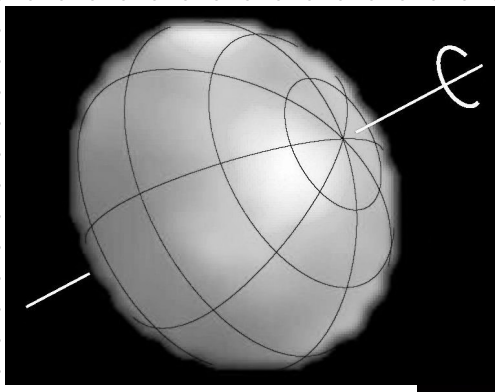
resolution limit HST $0.1''$

nearest star $0.03''$

w/ small angle approx

$$\frac{\text{physical size}}{\text{distance}} = \frac{\theta''}{206,265''/\text{rad}}$$

a handful of stars are resolved



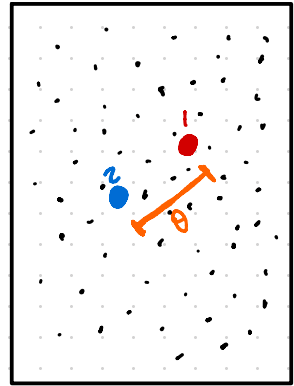
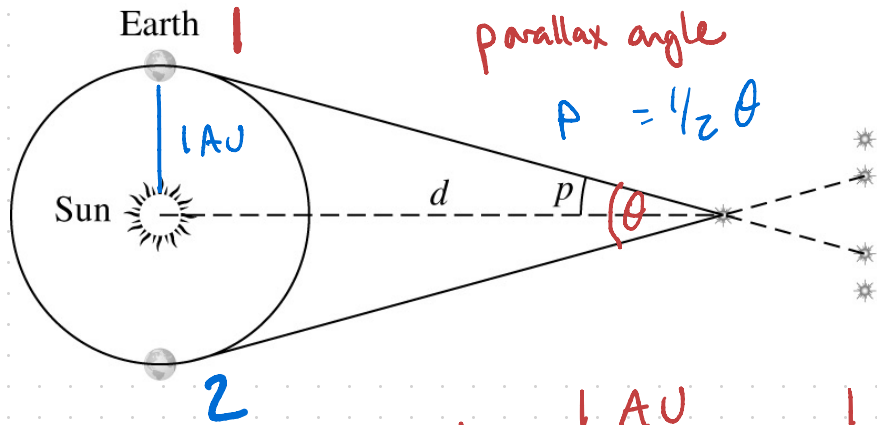
0.015"

How would you measure distance in space?

trigonometric parallax

standard candle - something we know the luminosity of
"spectroscopic parallax"

trigonometric parallax



$$d = \frac{1 \text{ AU}}{\tan p} = \frac{1 \text{ AU}}{p} \leftarrow \text{in radians}$$

$$d = \frac{206265'' / \text{rad}}{p''} \text{ AU}$$

define a **parsec**

$$1 \text{ pc} = 206,265 \text{ AU}$$

$$d = \frac{1}{p''} \text{ pc}$$

parsec is distance
when $p = 1''$

parallax arc second

$$1 \text{ pc} = 3.26 \text{ ly}$$

nearest star
proxima cen

$$4.2 \text{ ly} \\ p = 0.77''$$

Smallest "possible" $p = \sim 20 \text{ microarcsec} \sim 0.00002''$
 $\sim 50,000 \text{ pc}$

Brightness

Luminosity (W)

{ intrinsic property
{ total energy output of star

Brightness (W/m²)

how bright the star appears observed
from a given distance

aka "flux"

$$b = \frac{L}{4\pi d^2}$$

$$L_{\text{sun}} = 3.8 \cdot 10^{26} \text{ W}$$

$$d = 1.5 \times 10^{11} \text{ m}$$

$$L = A \sigma T^4$$

$$= 4\pi R^2 \sigma T^4$$

$$b = \frac{3.8 \times 10^{26} \text{ W}}{4\pi (1.5 \times 10^{11} \text{ m})^2}$$

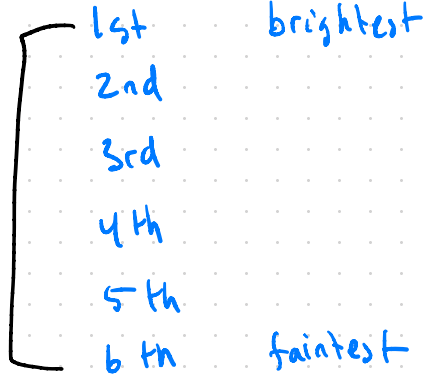
$$= 1,344 \text{ W/m}^2$$

"solar constant"

Magnitudes

6 groups

100x
brightness
ratio



human eye's response
to light is logarithmic

groups separated by
flux ratios, not differences

difference of 5 magnitudes equal "logarithmic scale"
to ratio of 100 in brightness

$$\begin{aligned} \frac{b_1}{b_2} &= 100^{(m_2 - m_1) / 5} = 100^{5/5} = 100^1 = 100 \\ &= 100^{10/5} = 100^2 = 10,000 \\ &= 100^{11/5} = 100^{0.2} = 2.512 \end{aligned}$$

$$b = \frac{L}{4\pi d^2}$$

$$L = A\sigma T^4 = 4\pi R^2 \sigma T^4$$

$$\frac{b_1}{b_2} = 10^{2(m_2 - m_1)/5}$$

$$\frac{b_1}{b_2} = 10^{0.4(m_2 - m_1)} = 10^{(m_2 - m_1)/2.5}$$

$$\log_{10}(10^{(m_2 - m_1)/2.5}) = \log_{10} \frac{b_1}{b_2}$$

$$m_2 - m_1 / 2.5 = \log_{10} b_1 / b_2$$

$$m_2 - m_1 = 2.5 \log_{10} b_1 / b_2$$

$$m_2 - m_1 = -2.5 \log_{10} b_2 / b_1$$

why?

Spectroscopic parallax

magnitudes

log scale

$\Delta m = \text{Flux ratios}$

$$\Delta m = 5 \rightarrow 100:1 \text{ brightness}$$

$$\Delta m = 1 \rightarrow 100^{1/5}:1 = 2.512:1$$

Smaller apparent magnitudes (more negative) are brighter

Sun -26.8

Sirius -1.46

Vega 0.000000000

naked eye
limit $\sim +6$

theoretical limit +29
for current modern telescopes

$$m_1 - m_2 = -2.5 \log \left(\frac{f_1}{f_2} \right)$$

$$m \text{ apparent magnitude } b = \frac{L}{4\pi d^2}$$

$$M \text{ absolute magnitude } b = \frac{L}{4\pi (10\text{pc})^2}$$

$$m - M = -2.5 \log_{10} \left(\frac{\frac{L}{4\pi d^2}}{\frac{L}{4\pi (10)^2}} \right)$$

$$m - M = -2.5 \log_{10} \left(\frac{\cancel{4\pi} d^2}{\cancel{4\pi} (10^2)} \right)$$

$$m - M = -2.5 \log_{10} \left(\frac{10^2}{d^2} \right)$$

$$m - M = -2.5 \log(10^2) + 2.5 \log(d^2)$$

$$m - M = -5 \log(10) + 5 \log d$$

$$m - M = 5 \log d - 5 \quad \text{distance modulus}$$

↑ d in parsecs

$$M_{\text{sun}} = 4.76$$

$$-\log \left(\frac{1}{x^2} \right) = +2 \log x$$

$$\log \left(\frac{x}{y} \right) = \log x - \log y$$

Adding magnitudes

$$M_1 + M_2$$

$$M_1 = -2.5 \log(L_1 / 4\pi d_1^2)$$

$$M_2 = -2.5 \log(L_2 / 4\pi d_2^2)$$

The Sun

What do you know about the Sun?

93 million miles away

150 million km

powered by nuclear fusion

totally average

onion structure

magnetic field

eject matter

orbiting around Galaxy

spin/rotate

R_{\odot}

$H \rightarrow He$

$T_{\text{eff}} = 5780 \text{ K}$ "surface temp"

pale yellow

$R_{\odot} = 6.96 \times 10^5 \text{ km} = 1 \text{ solar radius}$

$L_{\odot} = 3.9 \times 10^{26} \text{ W} = 10^{35} \text{ erg/s}$

1 solar Luminosity

$M_{\odot} = 1.99 \times 10^{30} \text{ kg} = 1 \text{ solar mass}$

chemical composition

by mass

70% H

28% He

2% everything else

by #

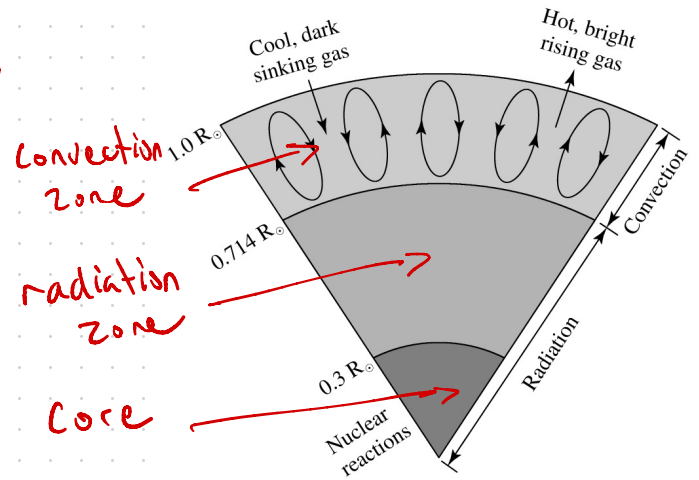
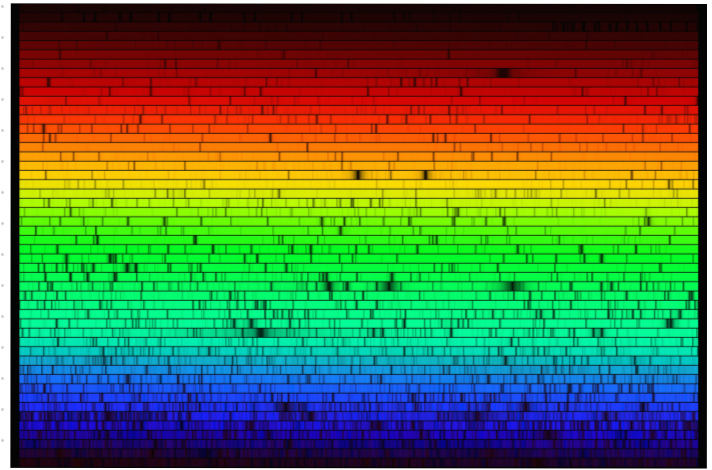
92.1% H

7.8% He

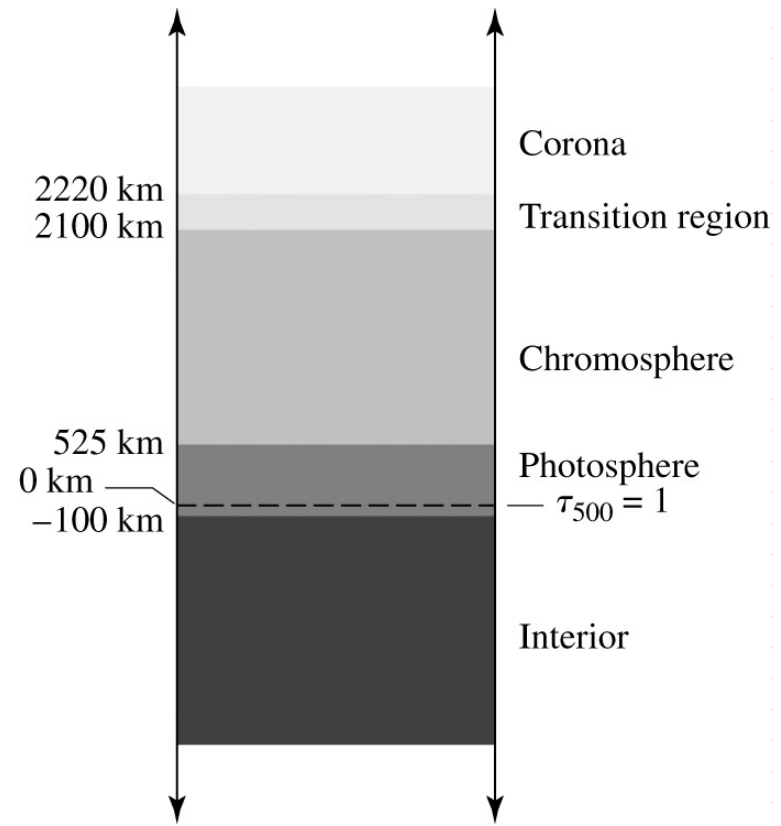
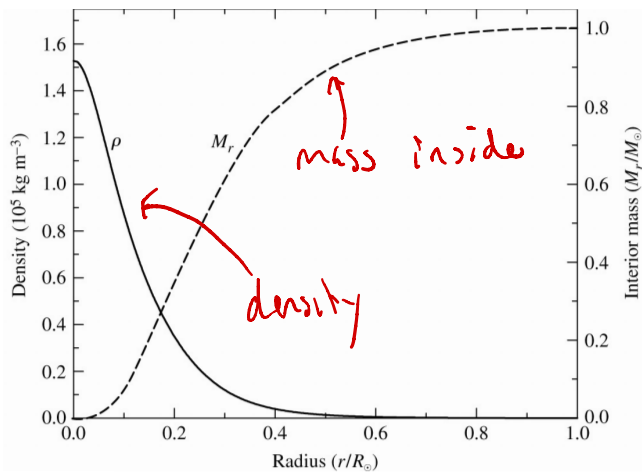
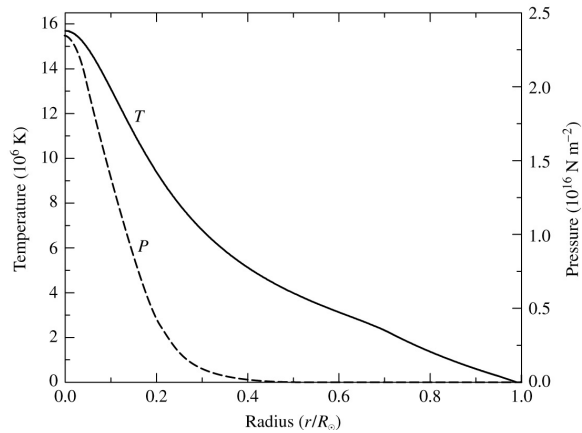
0.1% "metals"

O, N, C, Fe, Mg, Si "Metal"

mean density $1,440 \text{ kg/m}^3$



interior temp/pressure



HW 3

due 11:59pm

10/11

Midterm

10/13

in class

Observing

Night

8pm

10/13

14 or 15



Corona

during

total

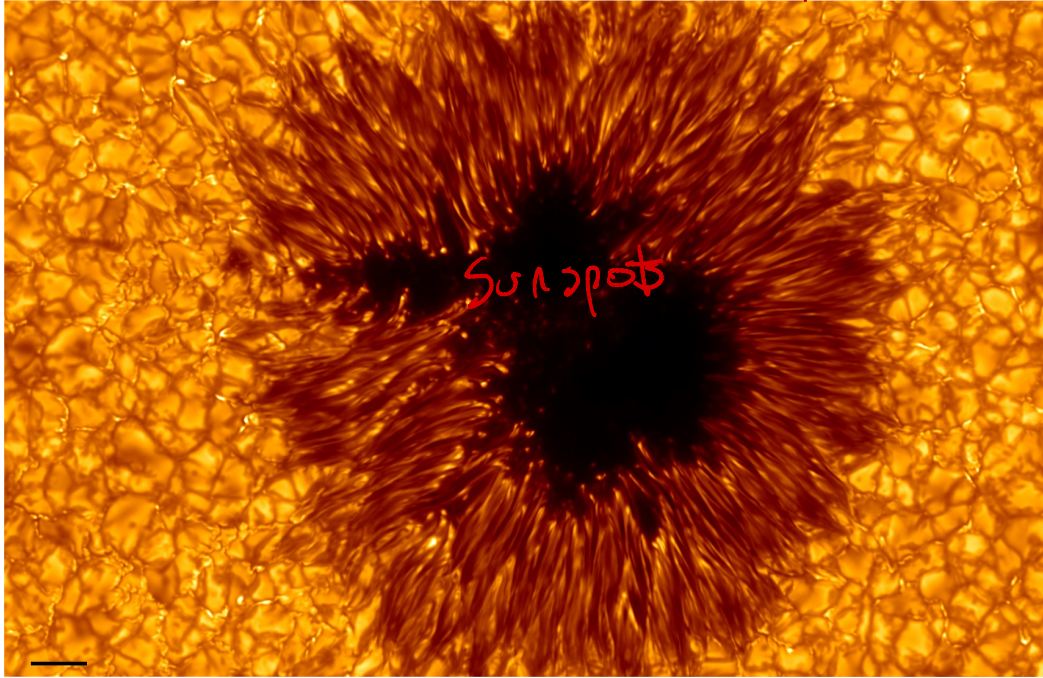
solar

eclipse

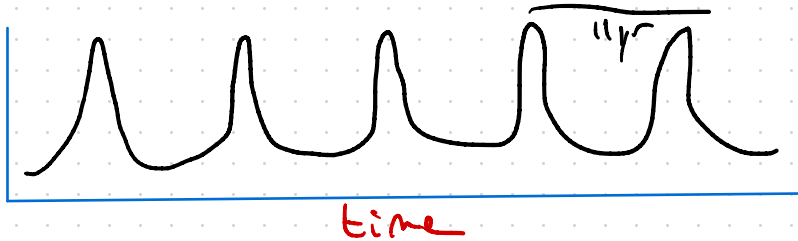
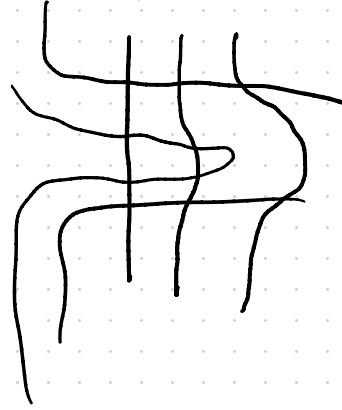
$$L = A \sigma T^4$$

cooler
areas
are
darker

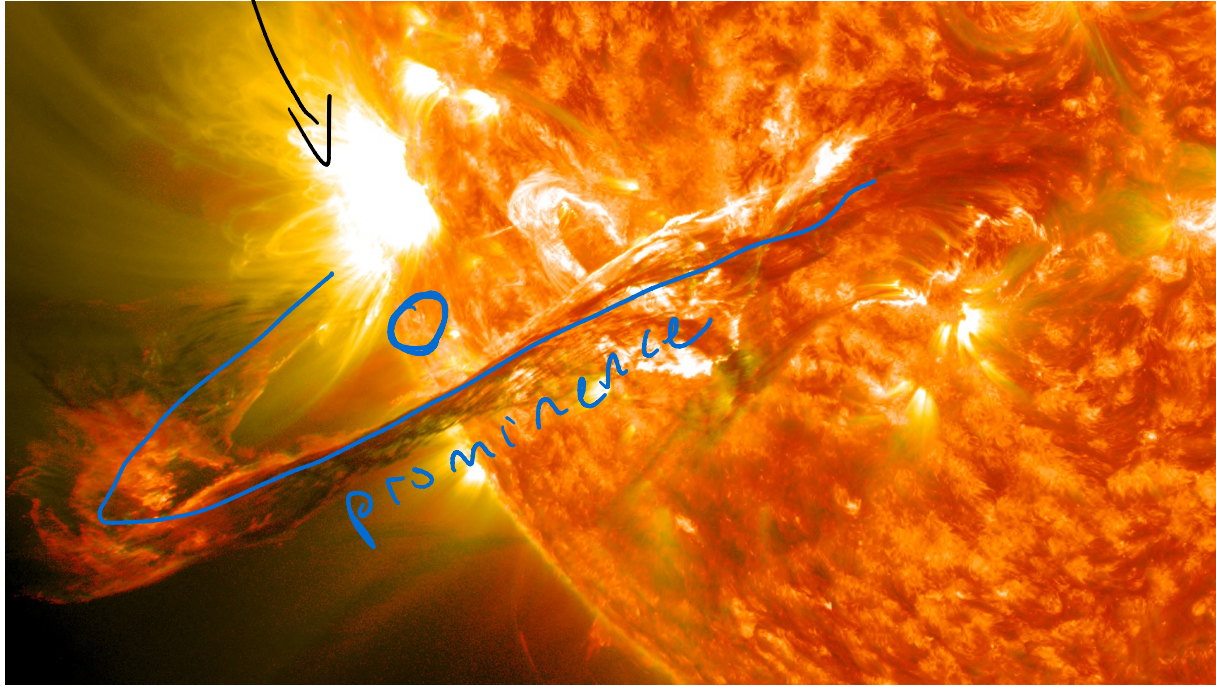
granules



sunspots \rightarrow magnetic field
inhibit convection lines

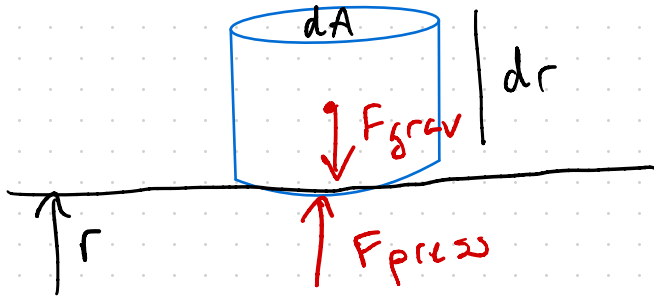


Solar flare



Hydrostatic Equilibrium

gravity vs. pressure



$$\text{density} = \rho(r)$$

$$\text{volume} = dr dA$$

$$\text{mass } dm = \rho(r) dr dA$$

$$\begin{aligned} F_{\text{grav}} &= -\frac{GMm}{r^2} = -\frac{GM(r)dm}{r^2} \\ &= \underbrace{-\frac{GM(r)}{r^2}}_{g(r)} \rho(r) dr dA \end{aligned}$$

$$F_{\text{grav}} = -g(r) \rho(r) dr dA$$

$$\text{net pressure} = P(r + dr) - P(r)$$

$$F_{\text{press}} = (P(r + dr) - P(r)) dA = \underline{dP dA}$$

$$F_{\text{press}} = F_{\text{grav}}$$

$$\cancel{dP dA} = -g(r) \rho(r) dr \cancel{dA}$$

$$dP = -g(r) \rho(r) dr$$

$$\frac{dP}{dr} = -g(r) \rho(r) = -\frac{GM(r) \rho(r)}{r^2}$$

Central Pressure

$$a) \text{ } \rho = 1440 \text{ kg/m}^3$$

$$M(r) = \frac{4}{3} \pi r^3 \rho$$

$$\frac{dp}{dr} = - \frac{G M(r) \rho(r)}{r^2} = - \frac{4}{3} G \pi r^3 \rho \frac{\rho}{r^2}$$

$$\frac{dp}{dr} = - \frac{4}{3} \pi G r \rho^2$$

$$\int_{p_c}^0 dp = - \frac{4}{3} \pi G \rho^2 \int_0^R r dr$$

\uparrow
Central pressure

$$- p_c = - G \frac{4}{3} \pi \rho^2 \frac{1}{2} R^2$$

$$P_c = \frac{2}{3} \pi G \langle \rho \rangle^2 R^2$$

$$P_c = 2.5 \times 10^{16} \text{ N/m}^2$$

\rightarrow 250 billion atm

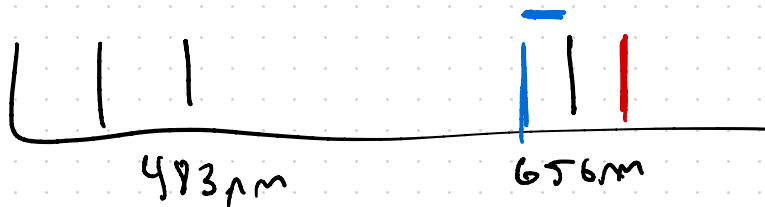
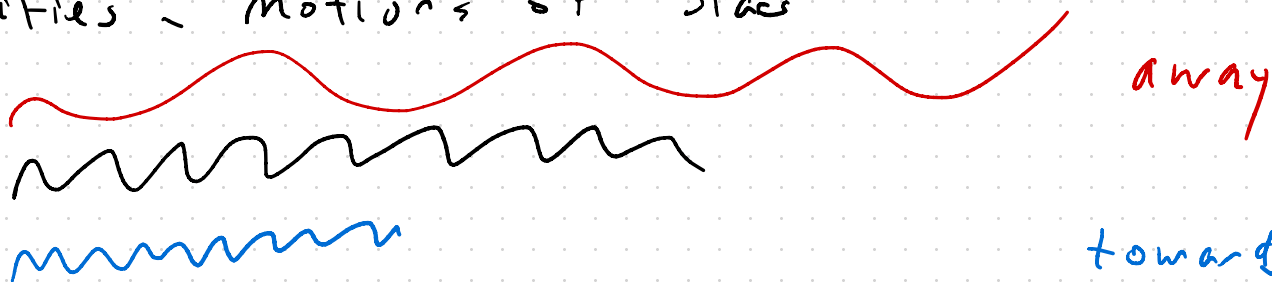
Mariana Trench
1,070 atm

$T = 15$ million K

how do we know the mass of the sun?

$$P^2 = \frac{4\pi^2}{GM} a^3$$

Velocities - motions of stars



$$\frac{\lambda_{\text{obs}} - \lambda_{\text{rest}}}{\lambda_{\text{rest}}} = z$$

"redshift"

$$z = \frac{V_r}{c}$$

velocity

"proper motion"

HW 3 Equation Reminders

$$d = \frac{1}{p''} \quad \text{in parsecs, arcseconds}$$

parallax distances

$$m - M = 5 \log_{10} d - 5$$

apparent magnitude absolute magnitude in parsecs

distance modulus

$$\frac{x}{d} = \frac{\theta''}{206,265''}$$

$$L = 4\pi R^2 \sigma T^4$$

luminosity

magnitudes / fluxes

$$m = -2.5 \log f$$
$$= -2.5 \log \left(\frac{L}{4\pi d^2} \right)$$

$$m_1 - m_2 = -2.5 \log f_1 / f_2$$

magnitude differences

$$P^2 = \frac{4\pi^2}{G(M_1 + M_2)} a^3$$

Kepler's 3rd Law

$$G = 4\pi^2$$

in AU
yr²
M₀

"proper motion"

measure side-to-side velocity

typically measure w/ parallax

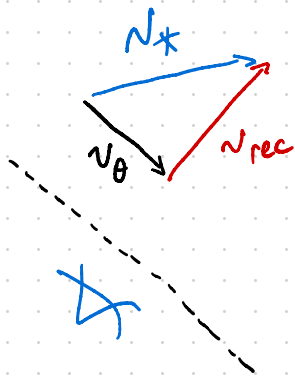
→ change in sky position over time

$$\mu = \text{PM in } \text{''/year}$$

$$= \frac{d\theta}{dt} = \frac{v_{\theta}}{d}$$

$$v_{\theta} = 4.74 \mu d$$

[km/s] [''/yr] [pc]



therefore "true space motion"

$$v_{*}^2 = v_{rec}^2 + v_{\theta}^2$$

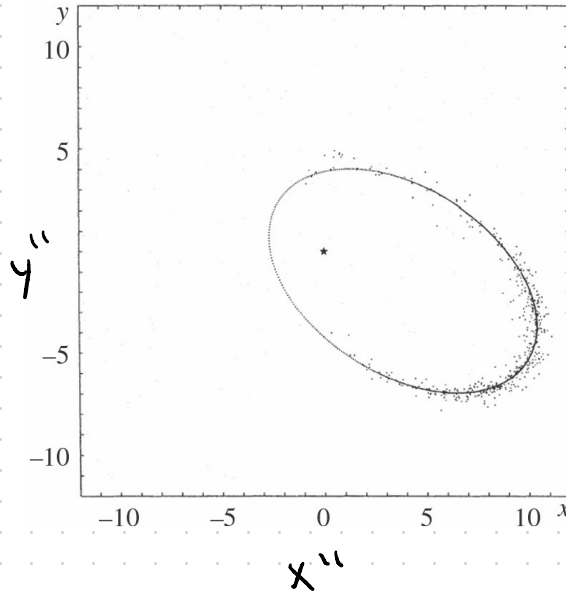
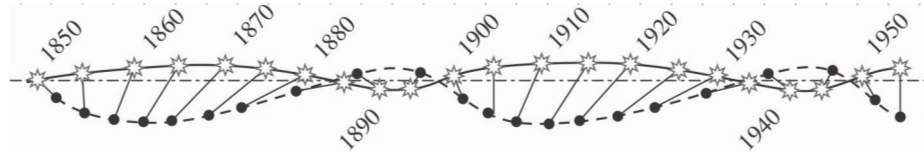
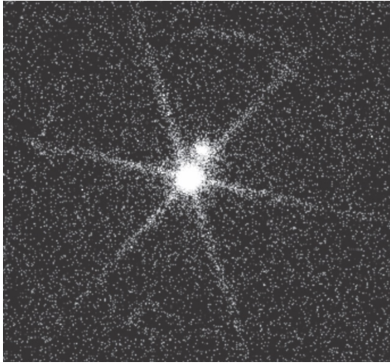
Binary Stars (+ exoplanets)

get mass from observing orbits

50% of all stars in binary (or bigger) systems

Visual Binaries

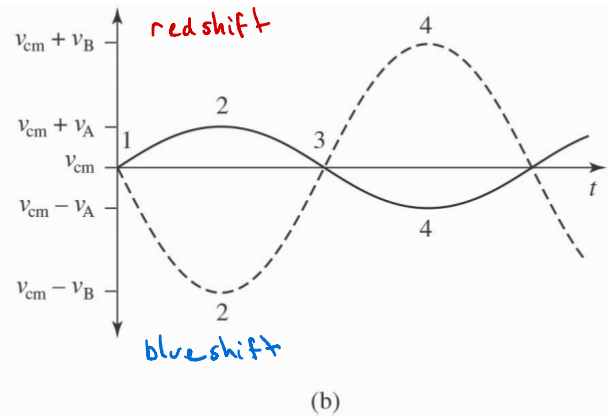
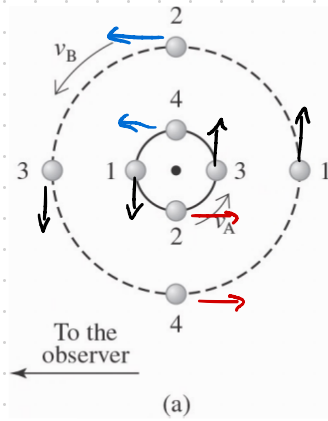
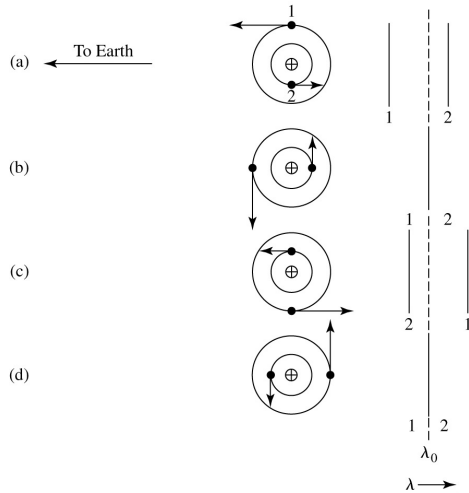
Sirius A+B



stars need to be close or far apart to resolve orbits
usually takes decades to get high quality data

Spectroscopic Binaries

observe shifting spectral features in stellar spectra to reconstruct velocity curves



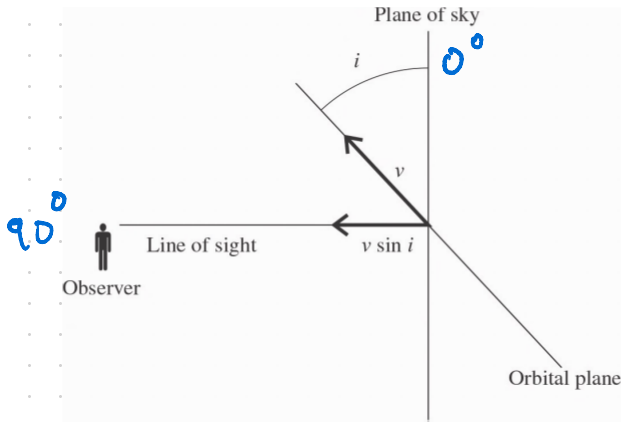
$$N_A M_A = N_B M_B \Rightarrow \frac{M_B}{M_A} = \frac{N_A}{N_B}$$

$$P = \frac{2\pi a_A}{N_A} = \frac{2\pi a_B}{N_B} \quad a = \frac{PN}{2\pi}$$

$$P^2 = \frac{4\pi^2}{G(M_A + M_B)} (a_A + a_B)^3$$

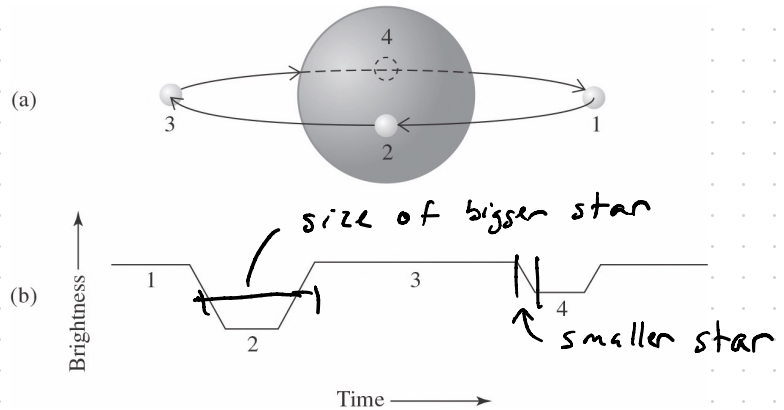
$$P^2 = \frac{4\pi^2}{G(M_A + M_B)} \frac{P^3 (N_A + N_B)^3}{(2\pi)^3}$$

$$M_A + M_B = \frac{P}{2\pi G} \frac{(N_A + N_B)^3}{\sin^3 i}$$



$$N_{true} = N \sin i$$

Eclipsing Binaries



Mass of a star is the fundamental defining property

$$L \propto M^4$$

Initial Mass Function

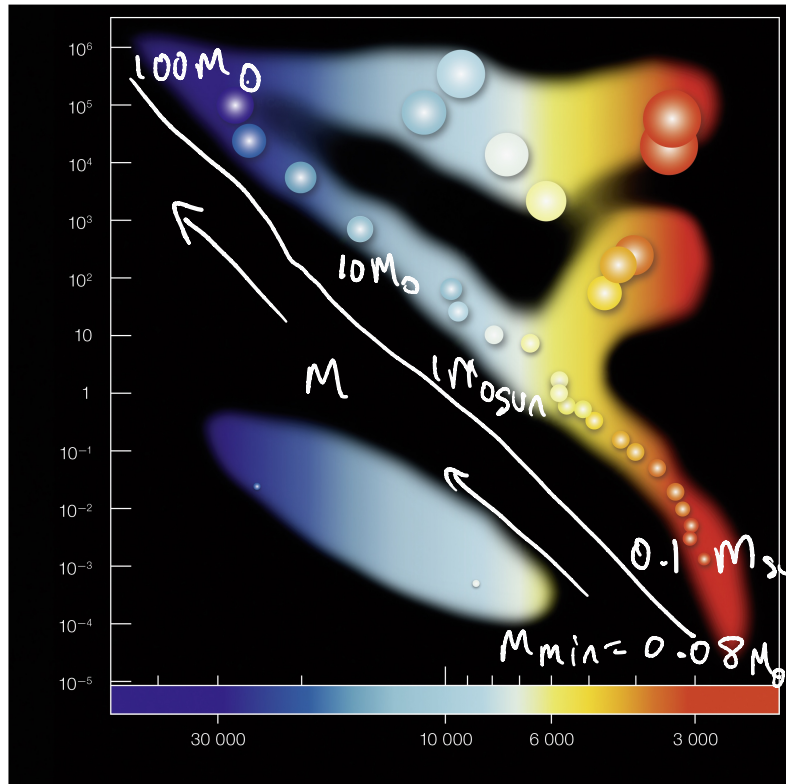
more massive stars less common L

100:1

$1 M_{\odot} : 10 M_{\odot}$

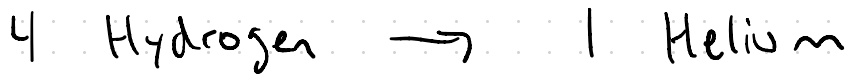
main sequence lifetime

$$t_{\text{ms}} \propto \frac{1}{M^{2.5}}$$



T

Nuclear fusion



- protons
- neutrons
- electrons

Atomic Mass Unit

$$1 \text{ AMU} = \frac{1}{12} \text{ carbon atom} = 1.66 \times 10^{-27} \text{ kg}$$

$$E = mc^2$$

$$= 931.5 \text{ million electron volts (MeV)}$$

$$1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}$$

$$M_H - M_p - M_e = -13.6 \text{ eV}$$

binding energy

H + energy = proton + electron

$$4H - 1He = +26.71 \text{ MeV} \quad 0.7\% \text{ of total mass}$$

$$\begin{aligned} E &= 0.007 (0.1 \times M_\odot) c^2 \\ &= 1.3 \times 10^{43} \text{ J} / 20 \\ &= 10^{10} \text{ years} \end{aligned}$$

Class Telescope Night Wed @ 8pm

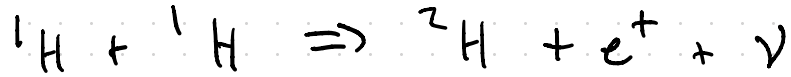
Midterm also wed in class

don't forget your "chest" sheet

Proton - Proton Chain

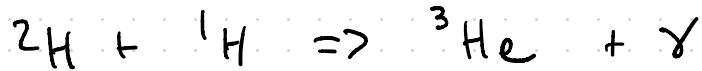
step 1

deuterium = $1p + 1n$



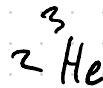
positron neutrino

step 2



= $2p + 1n$ gamma ray photon

repeat step 1 & step 2



proton \rightarrow ${}^1\text{H}$

${}^4\text{He} \rightarrow 2p + 2n$

$T > 10$ million K

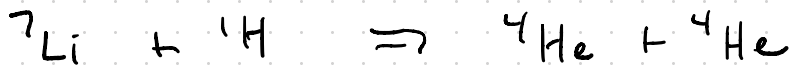
Step 3:

most common

69% of the time

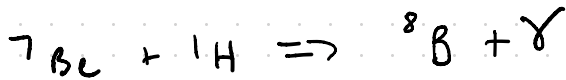


31% of time

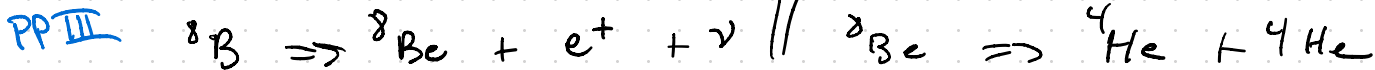


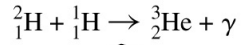
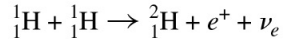
${}^4\text{He} = \text{alpha}$

0.3% of the time



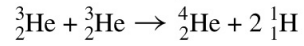
spallation?



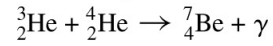


69%

31%

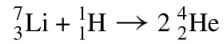
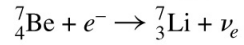


(PP I)

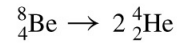
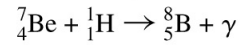


99.7%

0.3%



(PP II)



(PP III)

10^{57}

10^{56}

10^{55}

10^{45}

$10^{39} \times 26 \text{ MeV}$

10^{39} MeV / s

HW 4 now due 11/15

~~15.5~~ → 15.7

HW 5 now due 11/15

P-p chain



$T_{\text{core}} > 10 \text{ million K}$

$= 15 \text{ million K}$

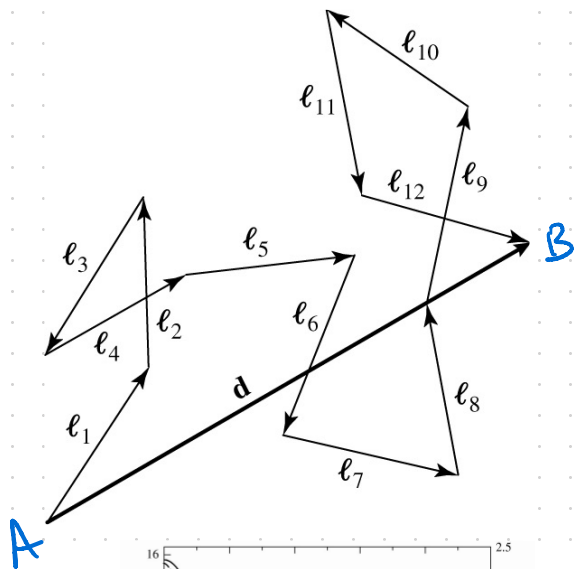
$T_{\text{surf}} = 5200 \text{ K}$

How do we go from high energy γ -rays
@ 15 million K to visible light @ $\sim 6000 \text{ K}$?

convection

radiation

random walk



mean free path l
number of steps N

$$d = l \sqrt{N}$$

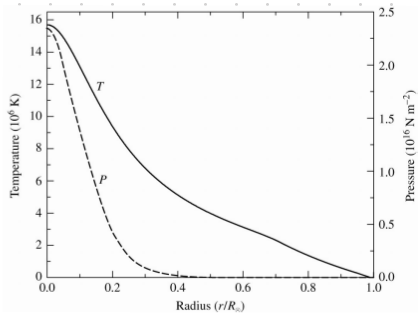
$$N = \left(\frac{d}{l}\right)^2$$

$$l = 10^{-3} \text{ m}$$

$$d = R_{\text{sun}} = 7 \times 10^5 \text{ km}$$

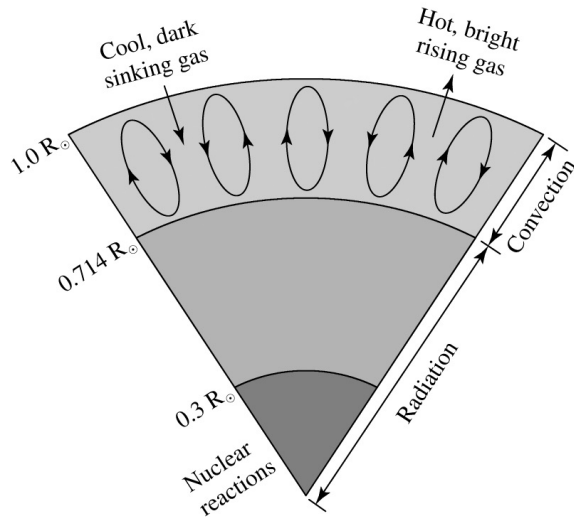
$$N = 10^{22}$$

$$t = 50,000 \text{ years}$$



convection

- hot gases rising, cool gases falling
- bulk motion of "cells" of gas
- net energy transport of energy from bottom to top
- no net transport of mass



Opacity (opaque)

mean free path depends on

- λ of light
- density
- temperature
- ionization / excitation states of atoms

inner regions dense, high T , high ionization, short λ

outer regions low density, low T , low ionization, long λ

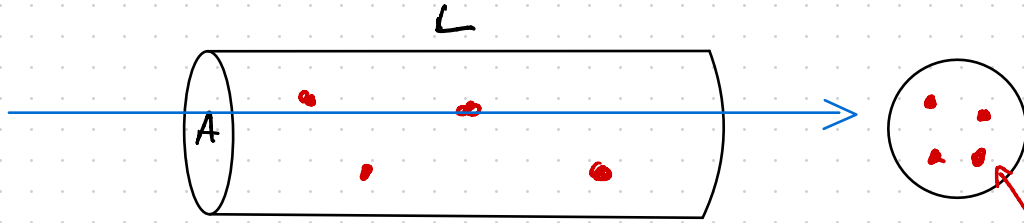
when opacity is very high, energy is more efficiently transported by convection

radiation $\frac{dT}{dr} = \frac{3 \rho(r) K(r) L(r)}{64 \pi \sigma_{SB} T(r)^3 r^2}$

← opacity

convection $\frac{dT}{dr} = \left(1 - \frac{1}{\gamma}\right) \frac{T(r)}{P(r)} \frac{dP}{dr}$

↑ adiabatic index



A = area of cylinder

L = length

r = size of absorbers

n = number density of absorbers

$$\sigma_a = \pi r^2$$

$$V = LA$$

$$N = nLA$$

$$\sigma_{\text{tot}} = nLA\sigma_a$$

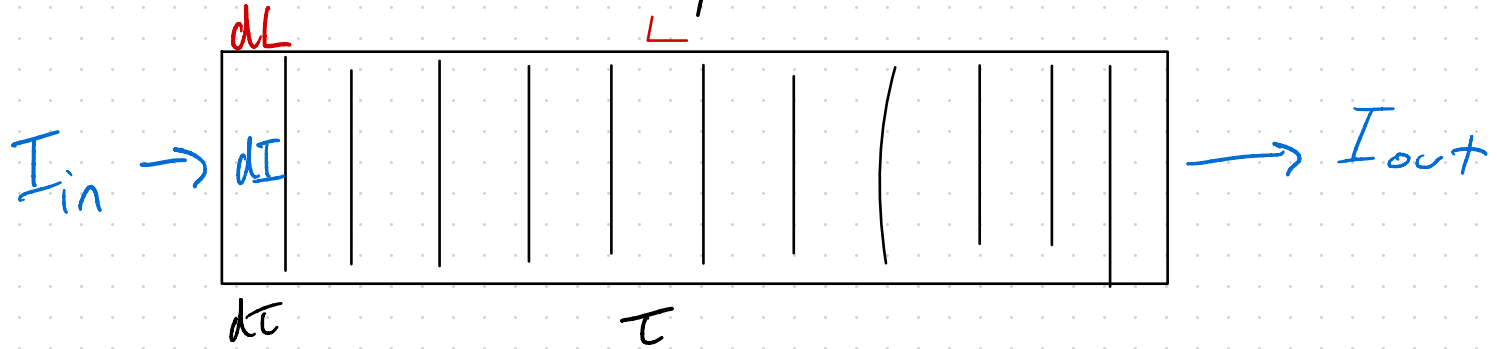
fraction absorbed

$$F_{\text{abs}} = \frac{\sigma_{\text{tot}}}{A} = nL\sigma_a = \tau$$

"optical depth"

Small τ "optically thin"

Large τ "optically thick"



$$dI = -(I)(n\sigma dL) = -I d\tau$$

$$\frac{dI}{I} = -d\tau \quad \int_{I_{in}}^{I_{out}} \frac{dI}{I} = -\int_0^{\tau} d\tau$$

$$\ln \left(\frac{I_{out}}{I_{in}} \right) = -\tau$$

$$I_{out} = I_{in} e^{-\tau}$$

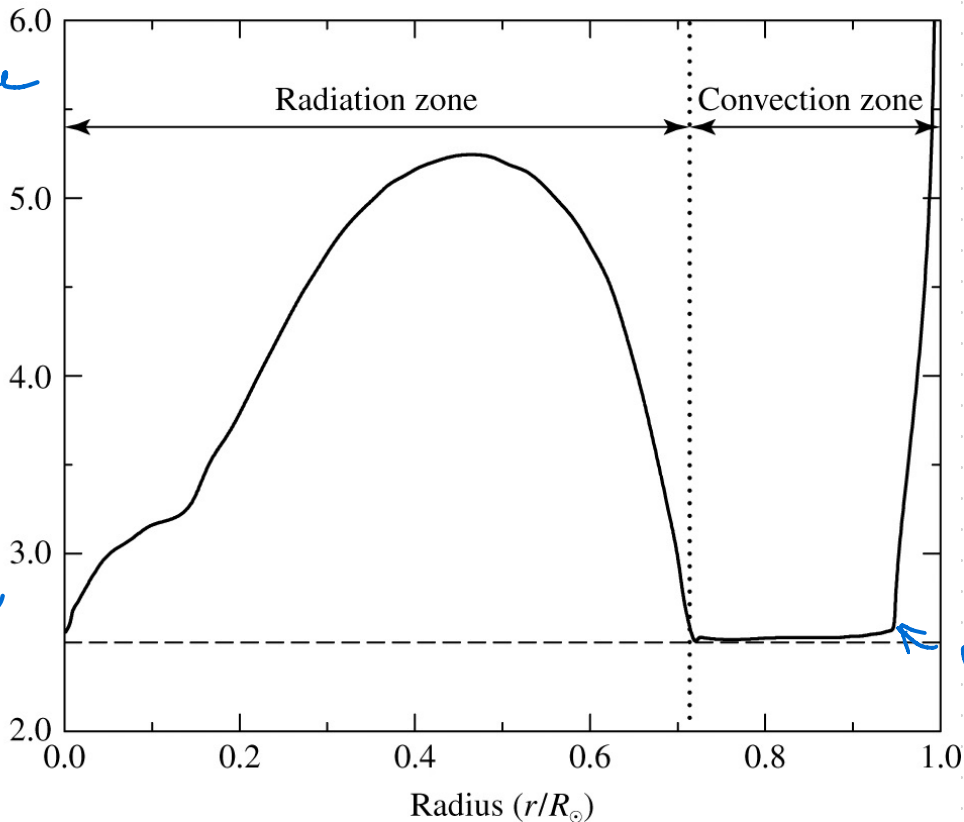
radiation
less opaque

$$\frac{1}{\tau} =$$

$d \ln P / d \ln T$

more opaque

convection



surface
 $T = 2/3$

radiation

Stellar Evolution

energy production (fusion)

energy transport (radiation, convection) **opacity**

gravity
radiation pressure } hydrostatic equilibrium $\frac{dP}{dr} = -\rho(r)g(r)$

equation of state $PV = NkT \Rightarrow \rho = \frac{\rho kT}{\mu m_H}$

chemical composition

X H 0.7

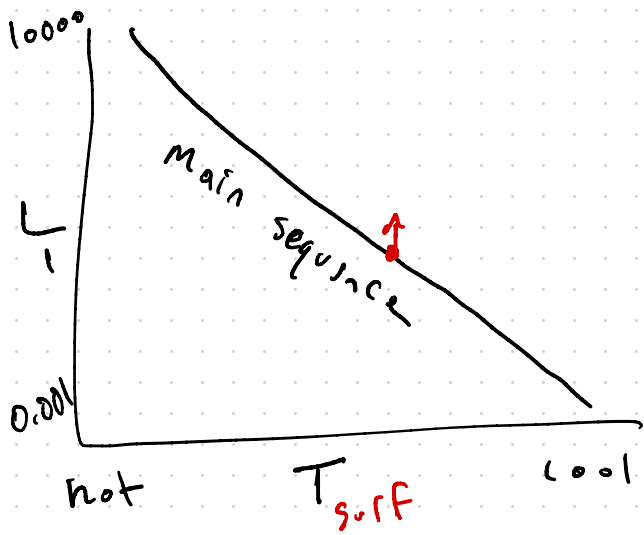
Y He 0.28

Z "metals" 0.02

"mean molecular weight"

MASS is He

most important determining factor



"period of a stars life
when it fuses H to He
in the core"

$$P = \frac{\rho k T}{\mu m_H} \quad \text{core}$$

what changes do we expect to
see as $\text{H} \rightarrow \text{He}$?

energy generation rate

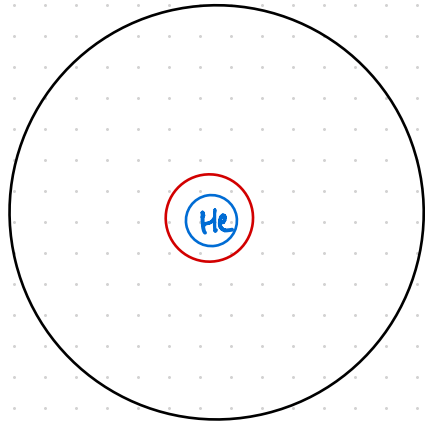
$$\epsilon_{pp} \sim T^4$$

$$L = 4\pi R^2 \sigma T_{\text{surface}}^4$$

$$L_{\text{now}} = 1.4 \times L_{\text{initial}}$$

main sequence lifetime

$$t_{\text{ms}} \approx \frac{1}{M^{2.5}} = 10 \text{ Gyr}$$



core contracts $\rightarrow T_{\text{core}}$ increases
H \rightarrow He shell burning

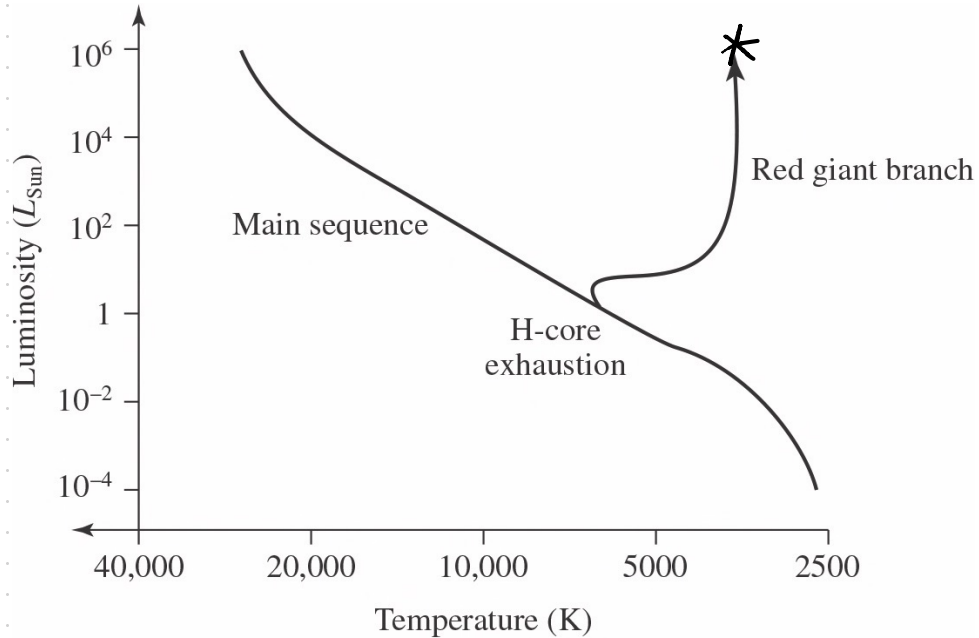
Red Giant branch

Red Giants

$L \rightarrow 100 L_{\text{sun}}$

$T \sim 4000 \text{ K}$

$R \sim 30 - 300 R_{\text{sun}}$



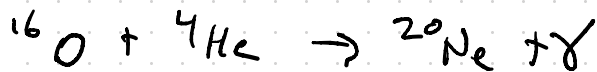
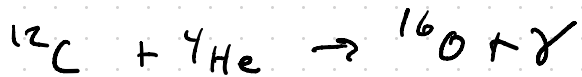
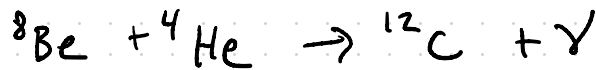
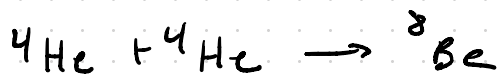
degeneracy pressure keeps core from collapsing

electrons keep core supported instead thermal pressure

$$P_e \sim \rho^{5/3}$$

helium flash @ 100 million K in core

triple alpha process



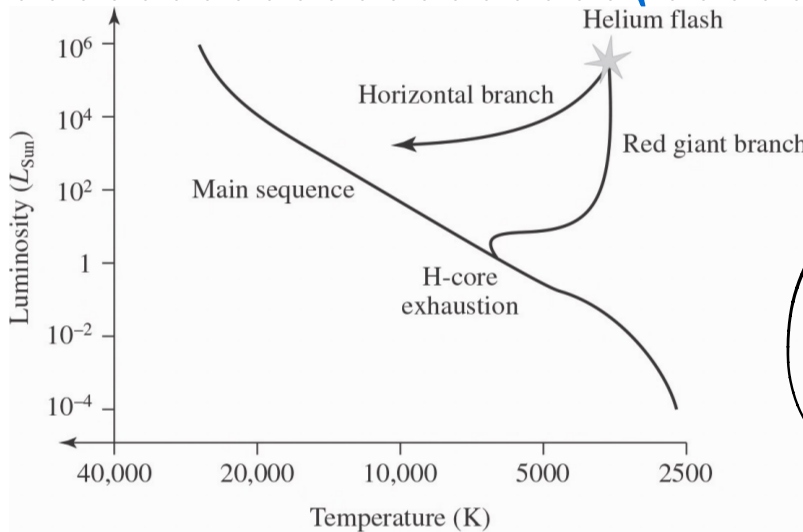
$$E_{3\alpha} \sim T^{41}$$

release $10^{11} L_{\text{sun}}$ all at once (few seconds)

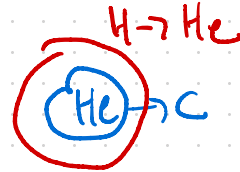
None makes it out of star

all the photons break electron degeneracy pressure, return star to ideal gas

expands core



Helium-burning main sequence = horizontal branch



What happens when you run out of Helium in the core?

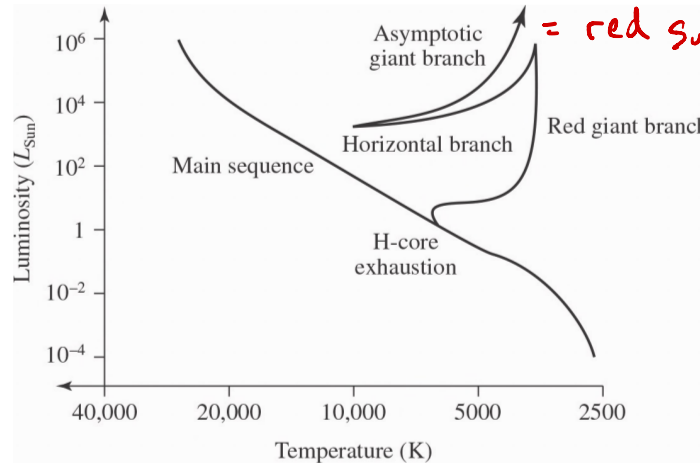
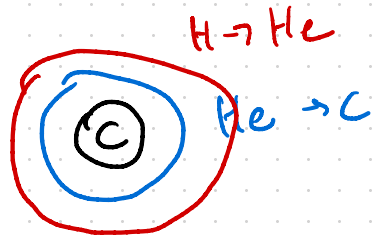
Core will contract, but supported by degeneracy pressure

Core T increases

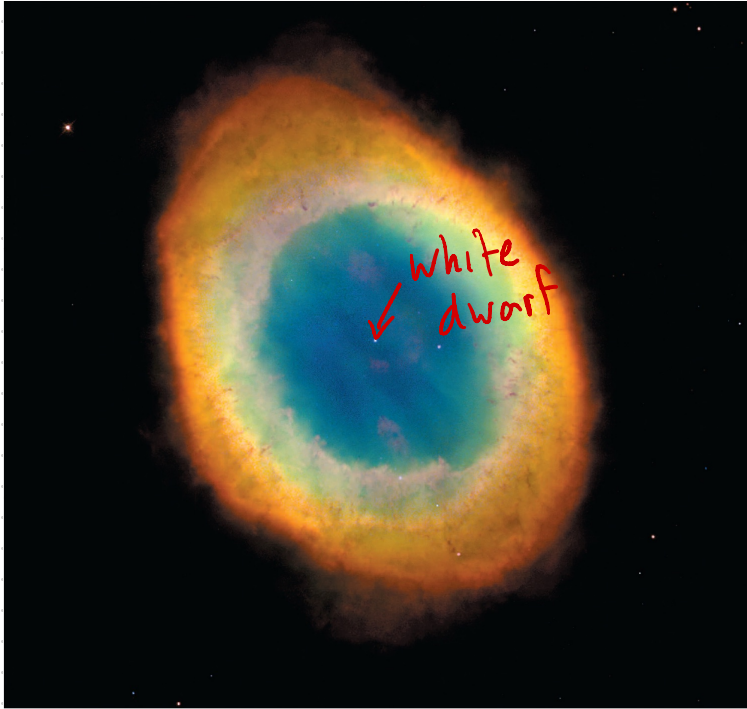
Star gets bigger, surface cools down

H^- ion

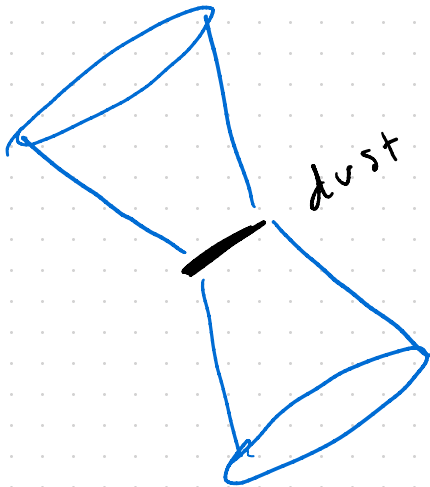
$p + 2e^-$



lose outer layers of star to helium
shell flashes



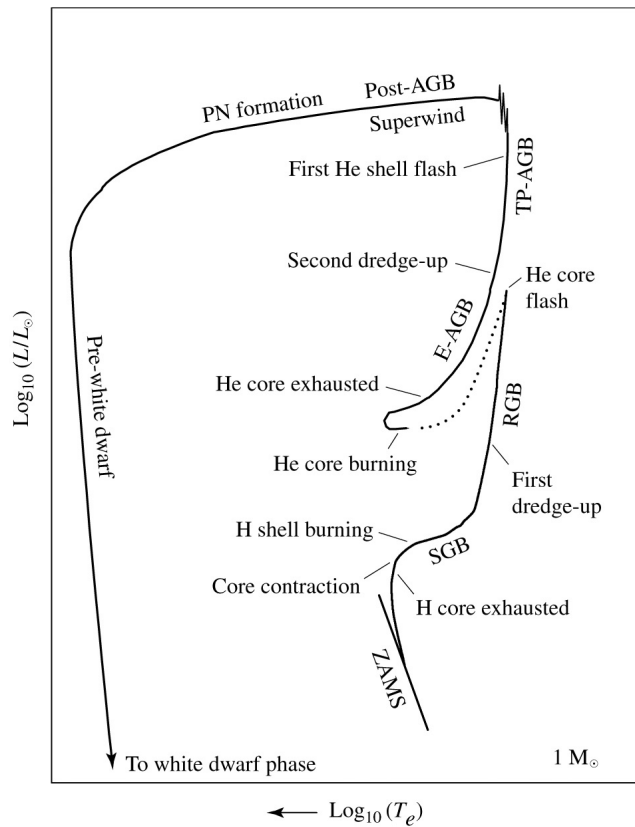
butterfly



dust disk



ring



HW 4/5 Due Monday 11/15

15.3 Mean Molecular Weights

See Ch. 14.1 Eq. 14.9

$$\mu = \left(2x + \frac{3}{4}y + \frac{1}{2}z \right)^{-1}$$

Mass M_0	MS Lifetime yrs
1	10 billion
1.5	1.5 billion
3	250 million
5	70 million
9	20 million
15	10 million
100	10,000

Why do high mass stars have such short MS lifetimes?

increased mass

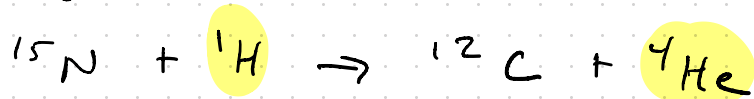
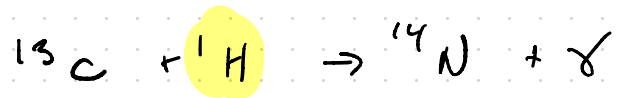
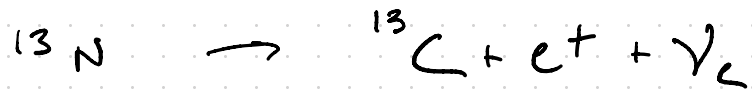
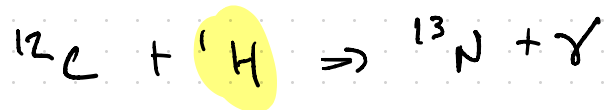
→ increased $\rho, T, \rho,$
fusion rate

CNO cycle
carbon, nitrogen, oxygen

$$E_{CNO} \sim T^{20}$$

$$E_{pp} \sim T^4$$

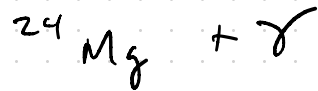
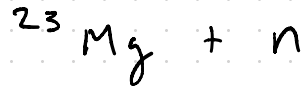
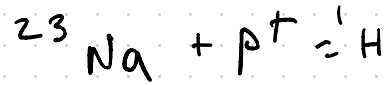
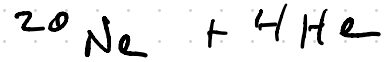
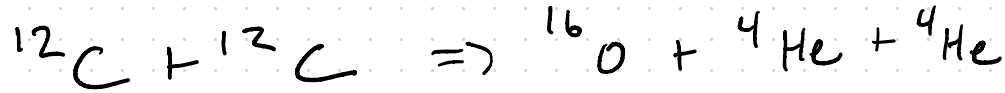
CNO



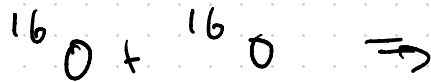
still do p-p chain in background

8 M_{\odot} and up:

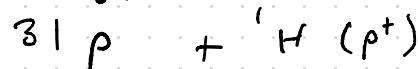
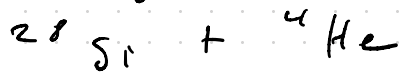
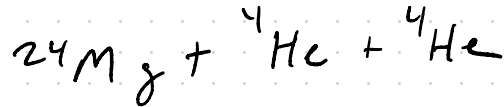
Carbon burning 600 million K



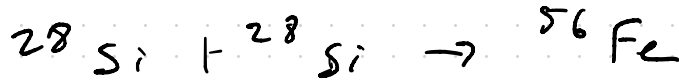
Oxygen burning



1 billion K



Silicon burning

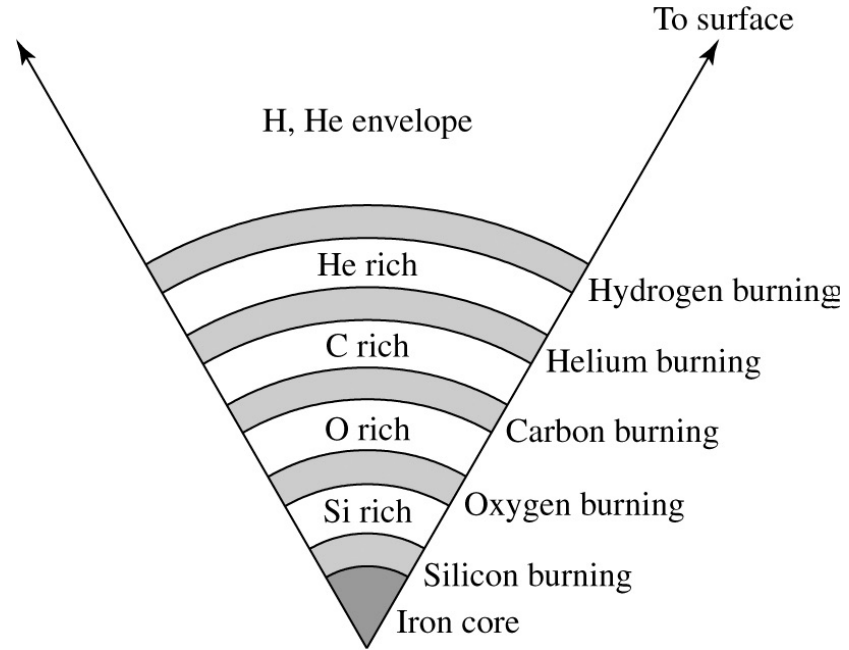


3.5 billion K

Iron cannot
be fused into
heavier elements!

Why is that a problem?

15 M _⊙	H	10 Myr
	He	1 Myr
	C	300 yr
	O	200 days
	Si	2 days



Supported by
degeneracy pressure
+ ~ 8 billion K
 $\rho \sim 10^{10} \text{ g/cm}^3$

binding
energy

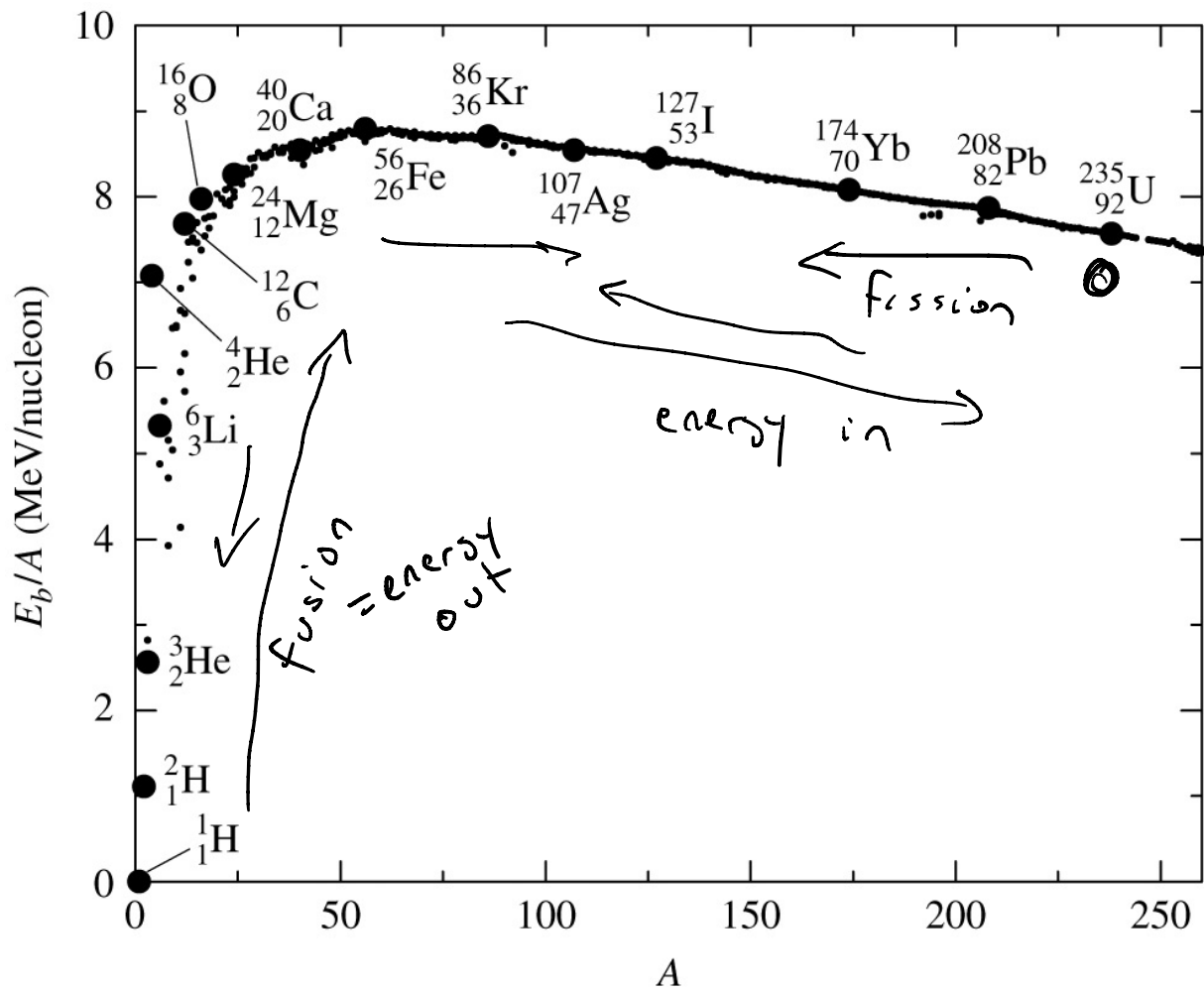
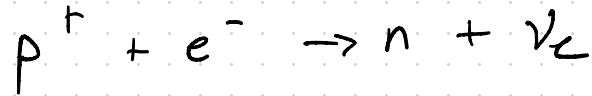
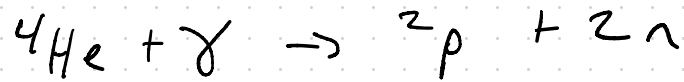
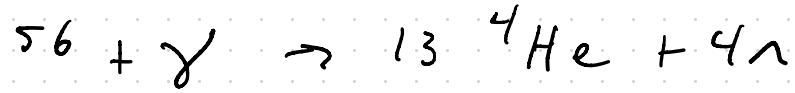


photo dissociate



core collapses

Earth sized core \rightarrow 50 km

at 10^{15} g/cm^3 1 second

collapse stops w/ neutron degeneracy
pressure

bounces off

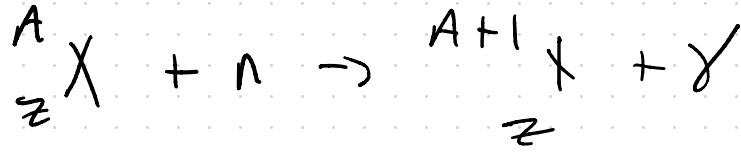
star explodes

Supernova

$10^9 L_{\text{sun}}$ @ peak brightness

$100 \times 10^9 L_{\text{sun}}$ in neutrinos

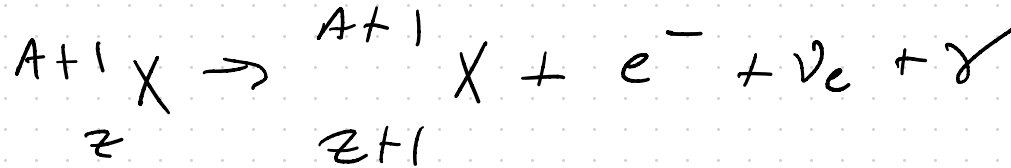
Neutron capture reactions

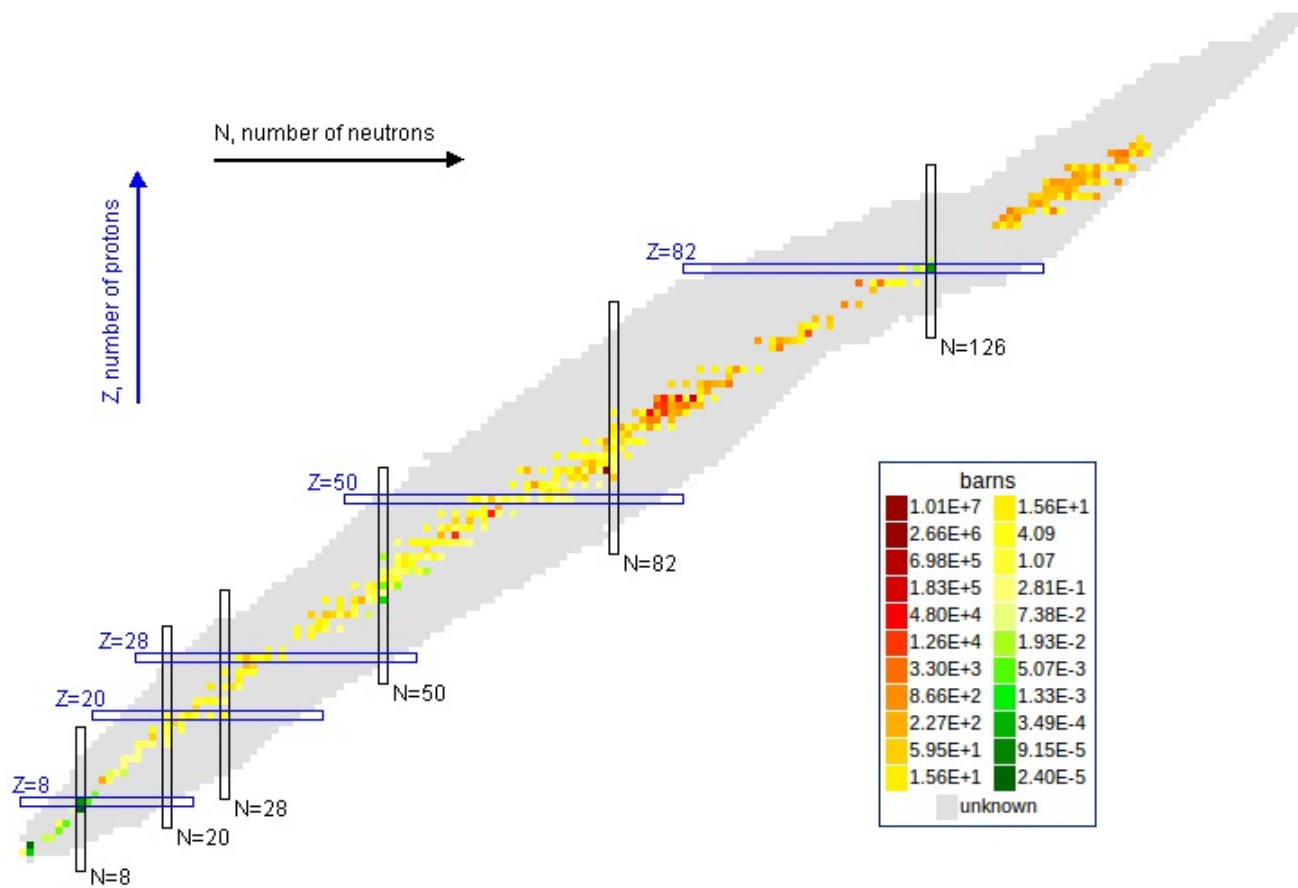


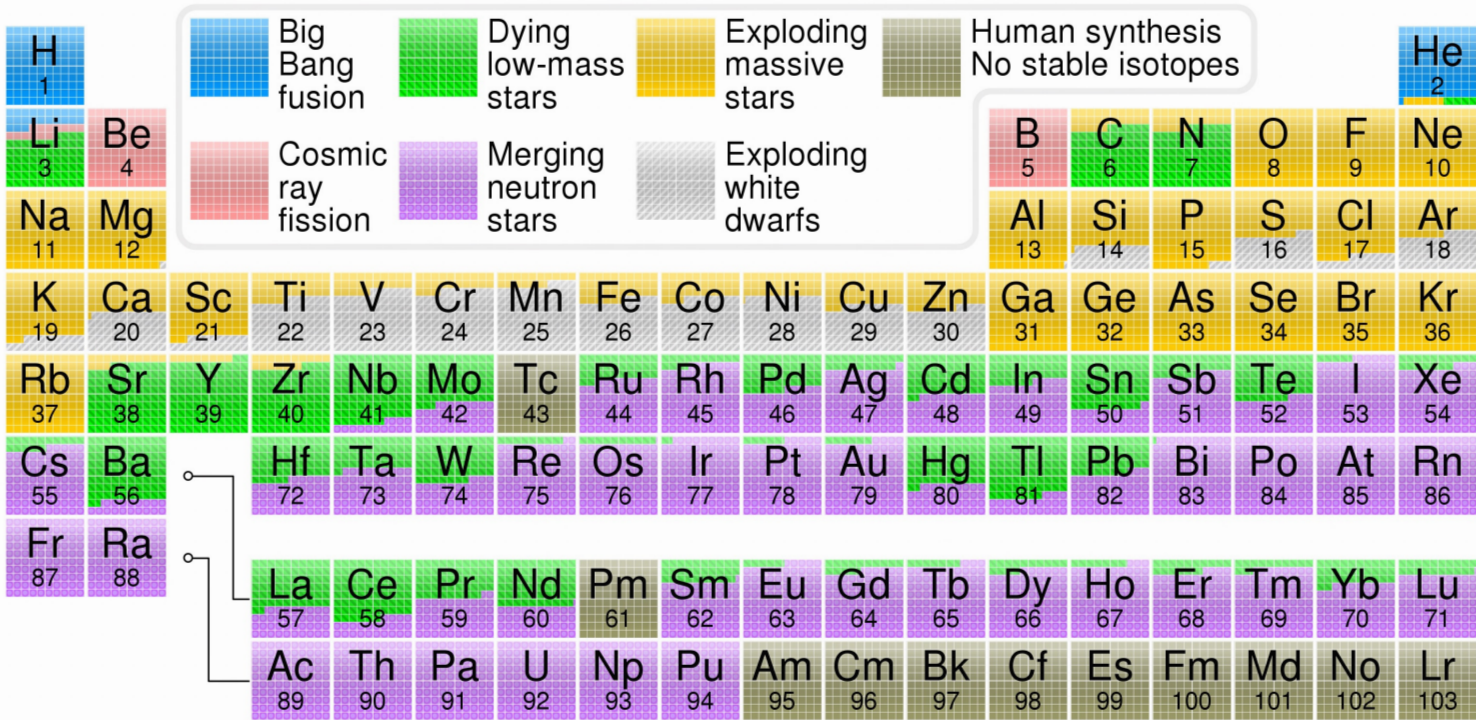
slow-process

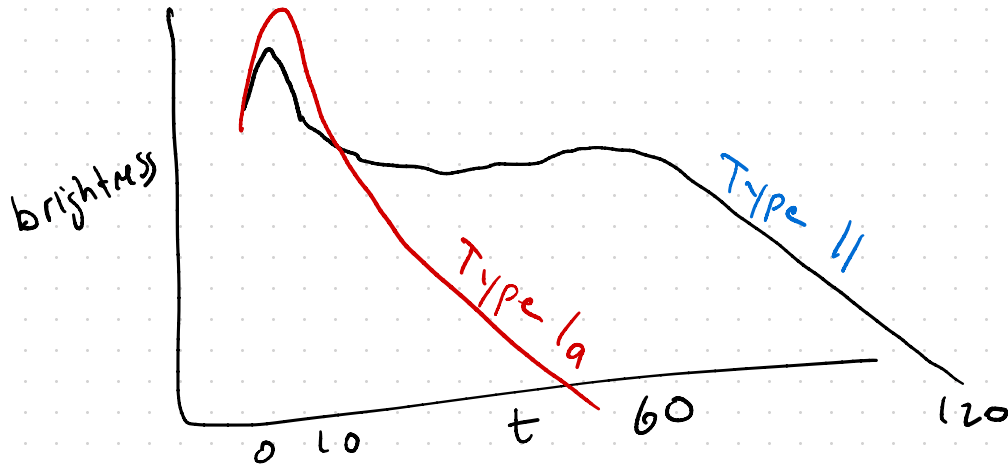
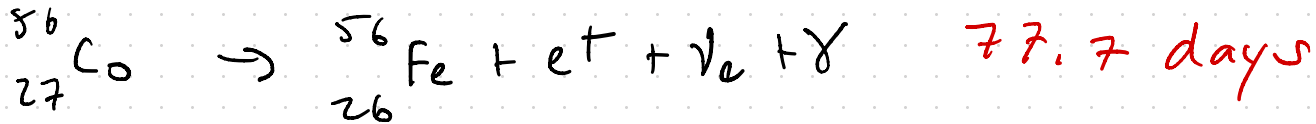
rapid-process

beta decay









Neutron Star

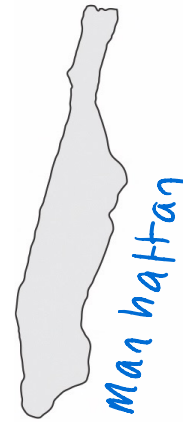
mass $\sim 1.5 - 3 M_{\odot}$
radius $10 - 15$ km
density 6×10^{14} g/cm³
v_{esc} $\sim 0.6 c$

outer crust

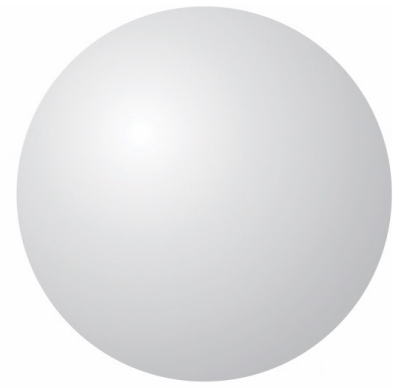
Fe, neutron rich isotopes, electrons

inner crust

elements, neutron superfluid

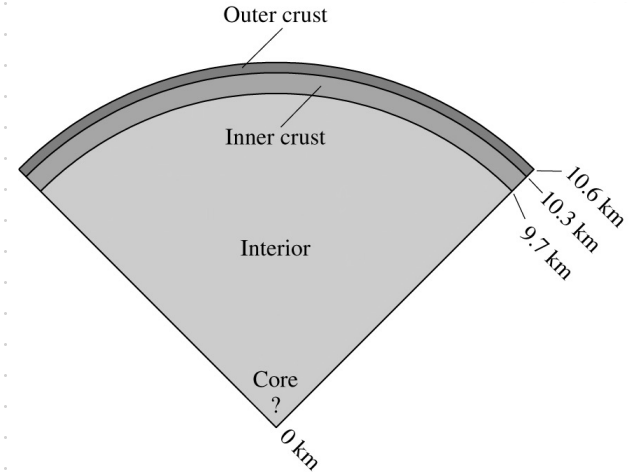


(a)



$M = 1.5 M_{\text{Sun}}$
 $R \approx 10$ km

(b)



Magnetic field

$$B_{\text{Earth}} = 0.5 \text{ Gauss}$$

$$B_{\text{sun}} = 1 - 10 \text{ Gauss}$$

$$B_{\text{NS}} = 10^{14} \text{ Gauss}$$

$$\text{Temp} \sim 10^{11} \text{ K} \rightarrow 10^6 \text{ K}$$

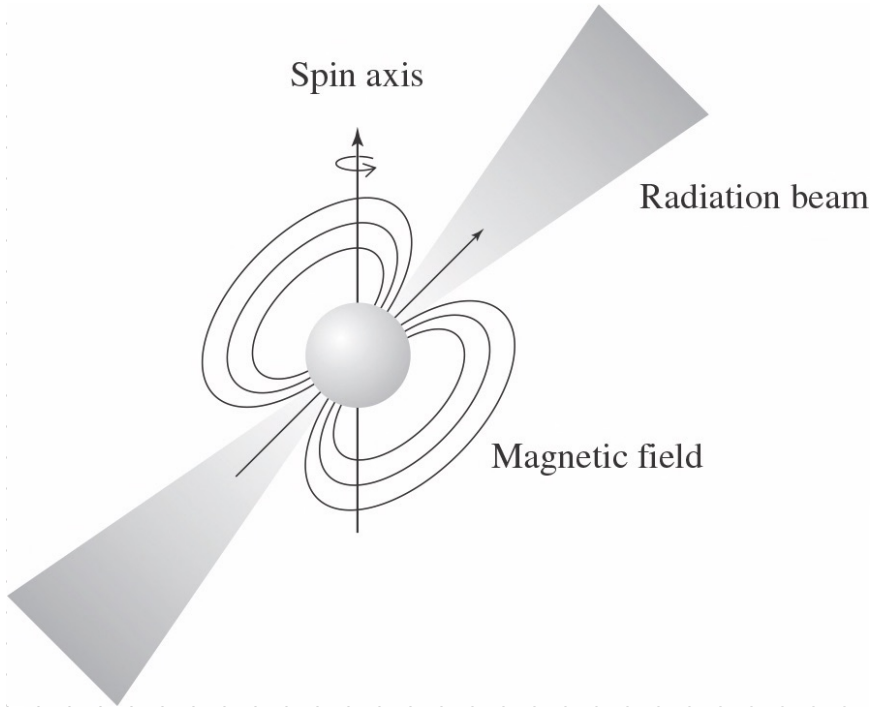
Synchrotron radiation

acceleration of charged particles around
magnetic field lines

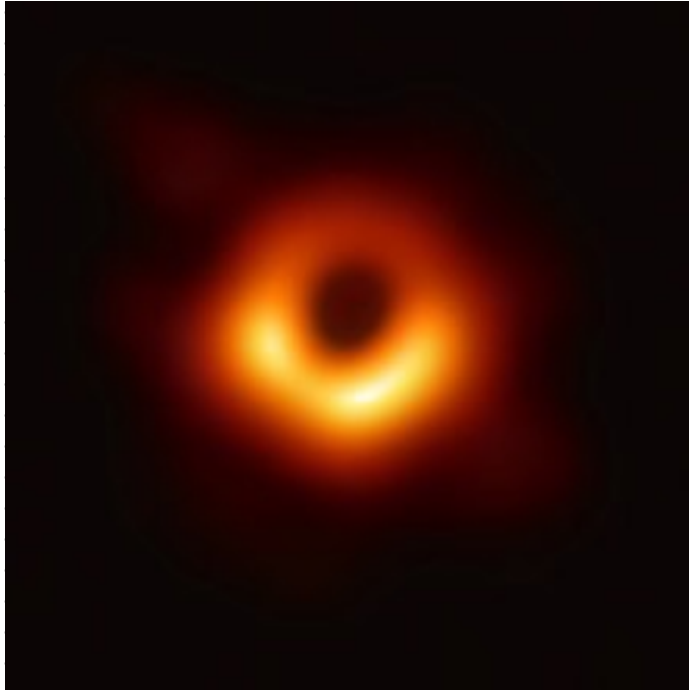
Blackbody curve peaks in X-ray

Pulsars

periods 0.25 - 2 seconds



Black Holes



Mass $3-10 M_{\text{sun}}$

Spin

electric charge

"size"

$$v_{\text{esc}}^2 = \frac{2GM}{R} = c^2$$

$$R = \frac{2GM}{c^2}$$

Schwarzschild Radius

well

White Dwarfs

leftover cores of Sun-like stars

C & O, He

$$M = 1 M_{\text{Sun}}$$

$$L = 0.03 L_{\text{Sun}}$$

$$L = 4\pi R^2 \sigma T^4$$

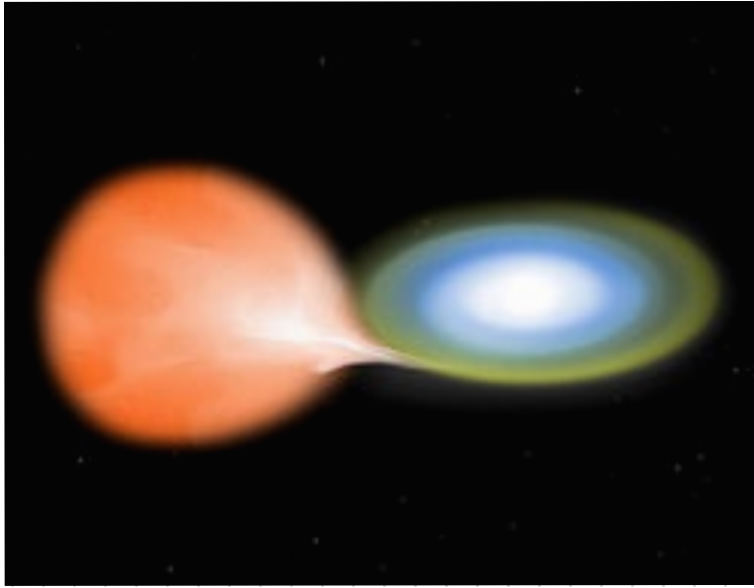
$$T \sim 27,000 \text{ K}$$

$$R \sim 0.008 R_{\text{Sun}} \sim R_{\text{Earth}}$$

$$\rho \sim 3 \times 10^6 \text{ g/cm}^3$$

$$\text{Maximum mass} = 1.44 M_{\odot}$$

Chandrasekhar
Limit



Nova

material in
accretion disk
undergoes spontaneous
 $H \rightarrow He$ fusion

recurrent nova

1.3 M_{sun} Carbon burning \rightarrow Fe \rightarrow boom!

$L > 10^9 L_{\text{sun}}$

thermal runaway supernova

Interstellar Medium

"stuff between the stars"

hydrogen $\sim 75\%$

helium $\sim 24\%$

molecular gases $\sim 1\%$

dust

neutral hydrogen (HI) 100's of kelvin

ionized hydrogen (HII) 1000's of K

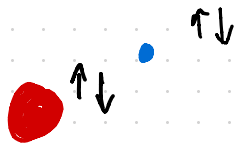
tracer for recent star formation

molecular hydrogen (H₂) 10's of K

Balmer line emission spectra

Neutral hydrogen

mostly in ground state



true ground state is up/down

up/up or down/down have a

little extra energy

$$E = \frac{hc}{\lambda}$$

$$\Delta E = 6 \times 10^{-6} \text{ eV}$$

$$\lambda = 21 \text{ cm (radio)}$$

Molecular Hydrogen

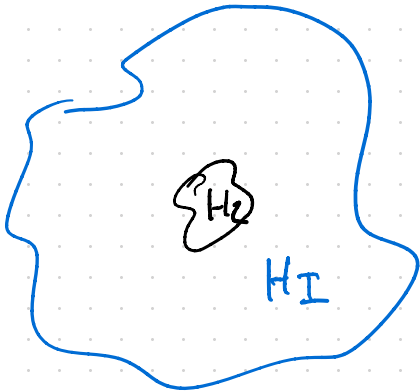
CO (2.6 mm) emits at 2.6 mm

dust

HCN

NH₃

"molecular clouds"



Temp

Density

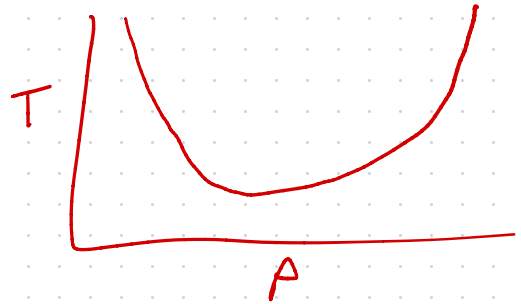
Mass

HI cloud

50 K

500 #/cm³

1-100 M_⊙



molecular cloud core

150 K

10⁷ #/cm³

10-1000 M_⊙

Virial Theorem

$$K + U = 0$$

$$E = \frac{1}{2} U$$

$$K = \frac{1}{2} U$$

$$K = N \left(\frac{3}{2} kT \right)$$

$$U = -\frac{3}{5} \frac{G M^2}{R}$$

$$3 N kT < \frac{3}{5} \frac{G M^2}{R}$$

$$M > \left(\frac{5 kT}{G m_{\text{particle}}} \right)^{3/2} \left(\frac{3}{4 \pi \rho} \right)^{1/2}$$

$$N = \frac{M}{m} \frac{\text{total}}{\text{particle mass}}$$

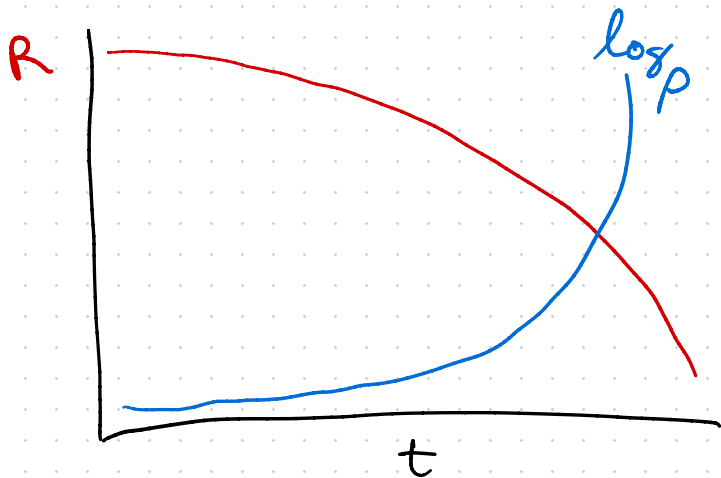
$$R = \left(\frac{3 N}{4 \pi \rho} \right)^{1/3}$$

Jeans mass

when you exceed limit
(part) of the cloud can collapse

isothermal collapse $\hat{=}$ "same temperature"

cloud is optically thin, heat radiates away



free-fall time

$$a = \frac{GM(r)}{r^2} \quad r = \frac{1}{2} a t_{ff}^2$$
$$= \frac{4\pi G r \rho}{3}$$

$$t_{ff} \sim \sqrt{\frac{1}{G\rho}}$$

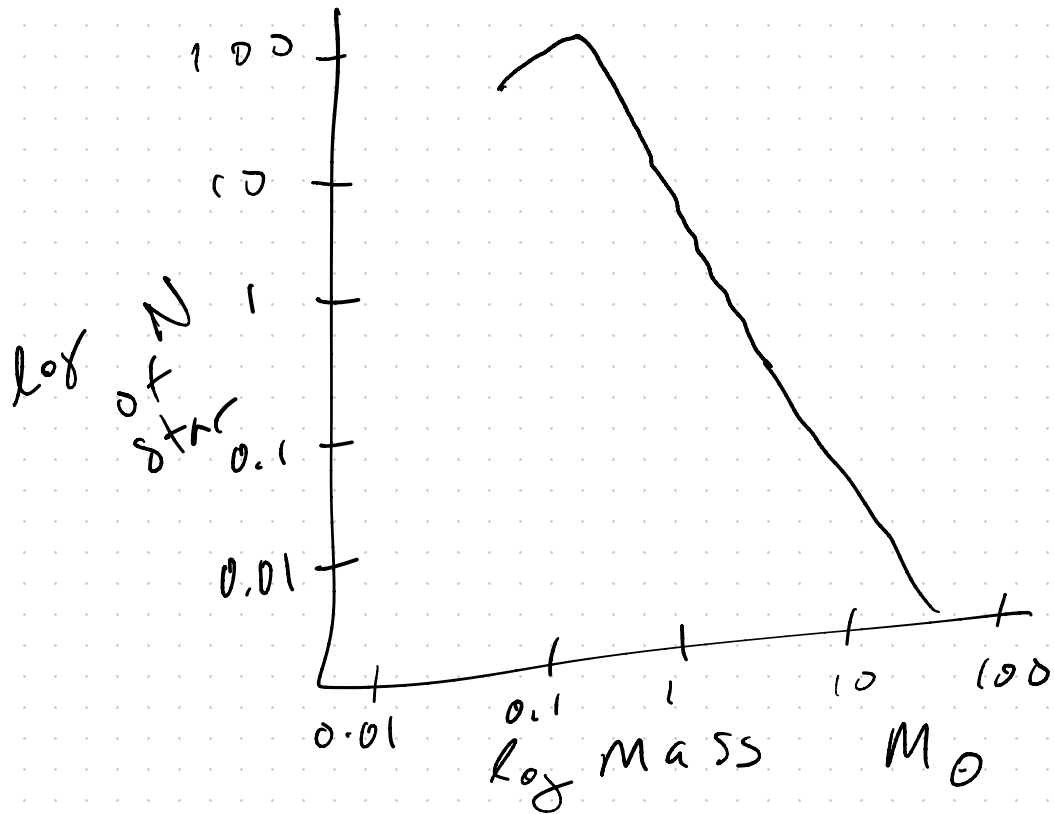
$$t_{\text{ff}} = \sqrt{\frac{1}{4\rho}} \quad M \sim \sqrt{\frac{1}{\rho}}$$

Fragmenting big cloud into smaller pieces that each collapse independently into a star

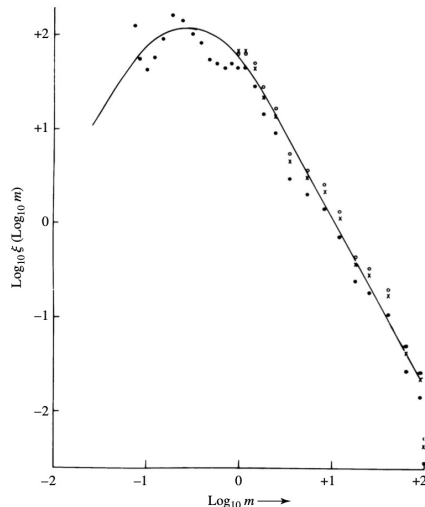
Smallest clump $\sim 1/2 M_{\odot}$

eventually cloud is too opaque

adiabatic collapse \rightarrow higher $T \rightarrow$ higher ρ



initial
mass
function





η & γ persei



h & χ Persei

blue

not dense

irregular shapes

differences?

M13

stars more red
red giants?

denser distribution

spherical

open clusters

bluer, younger stars

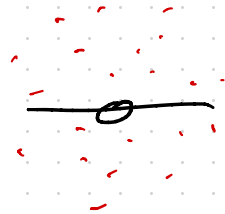
low densities

~1000 stars

10-100 million years old

found in areas of recent star formation

found in disks of spiral galaxies



globular clusters

cool, red stars

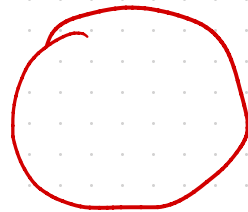
old 13-14 billion years old

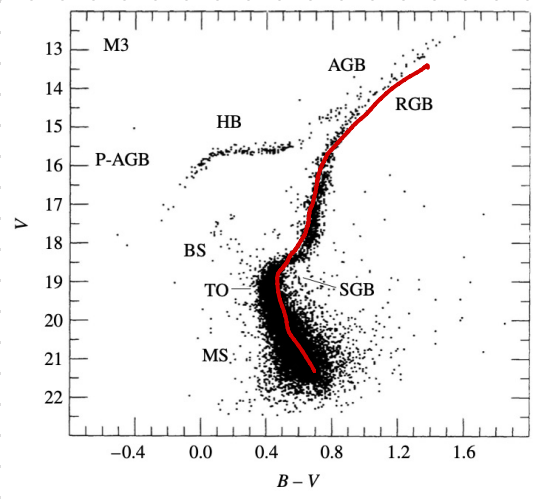
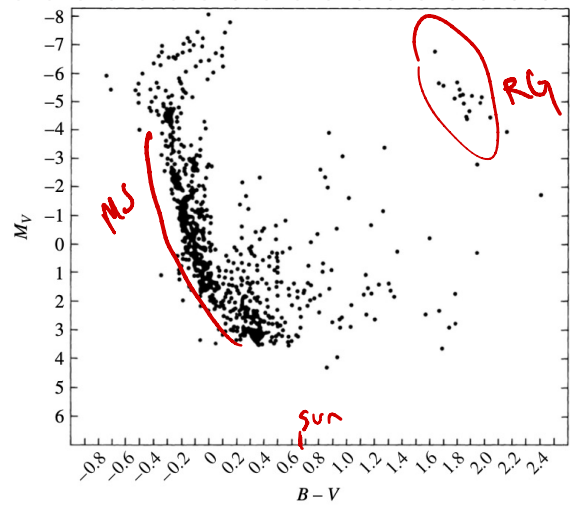
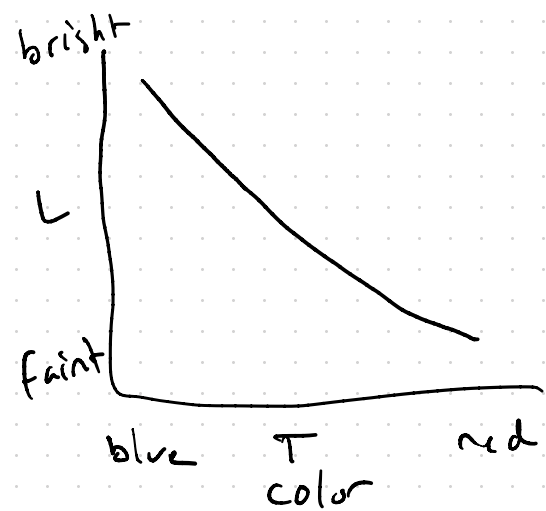
high density

100,000 stars

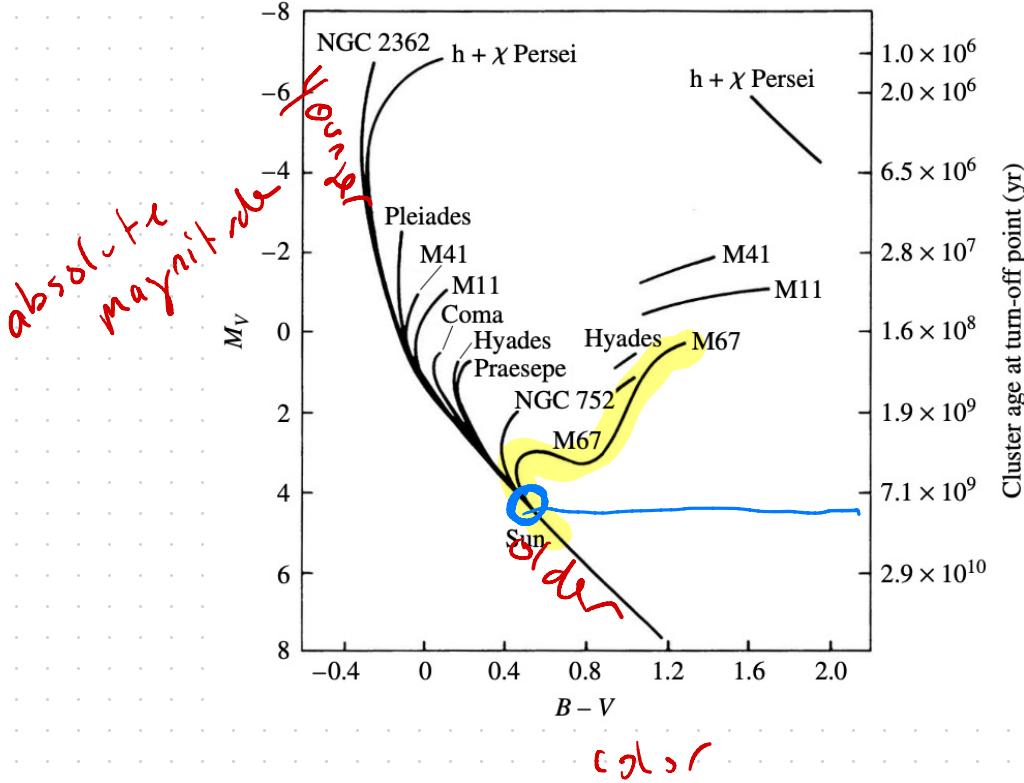
mainsequence, red giant stars

found around galaxies of all types





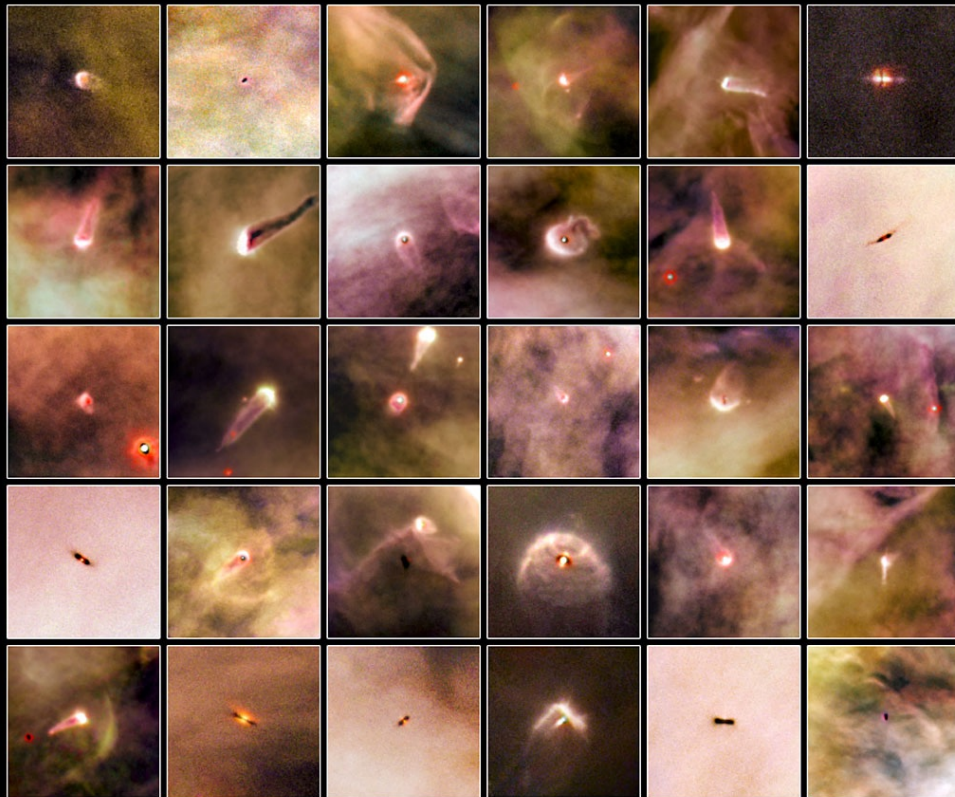
isochrones = same age

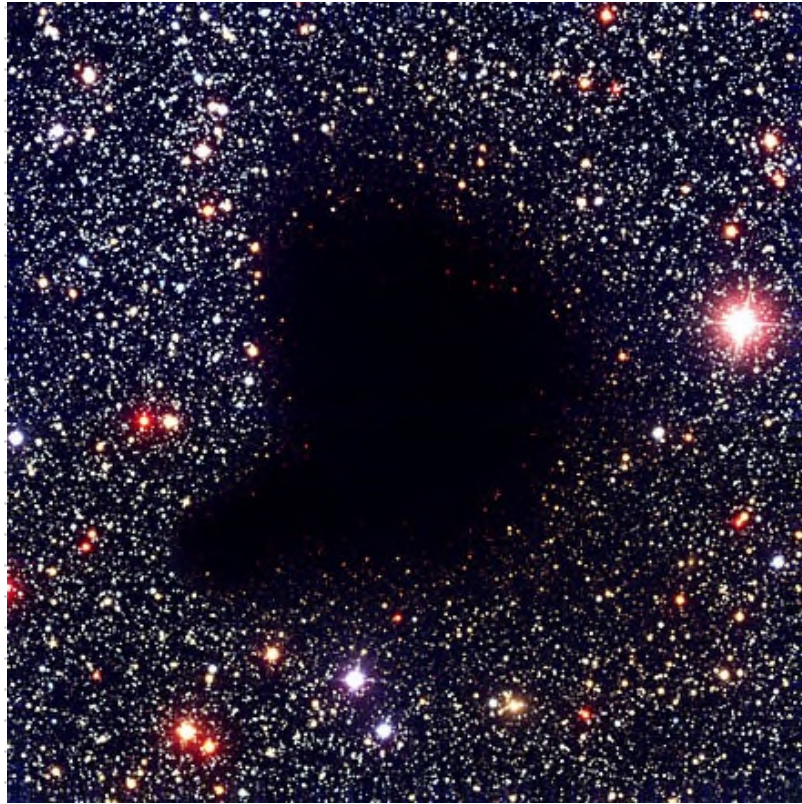


distance modulus

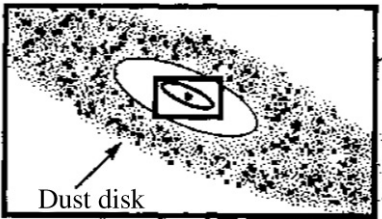
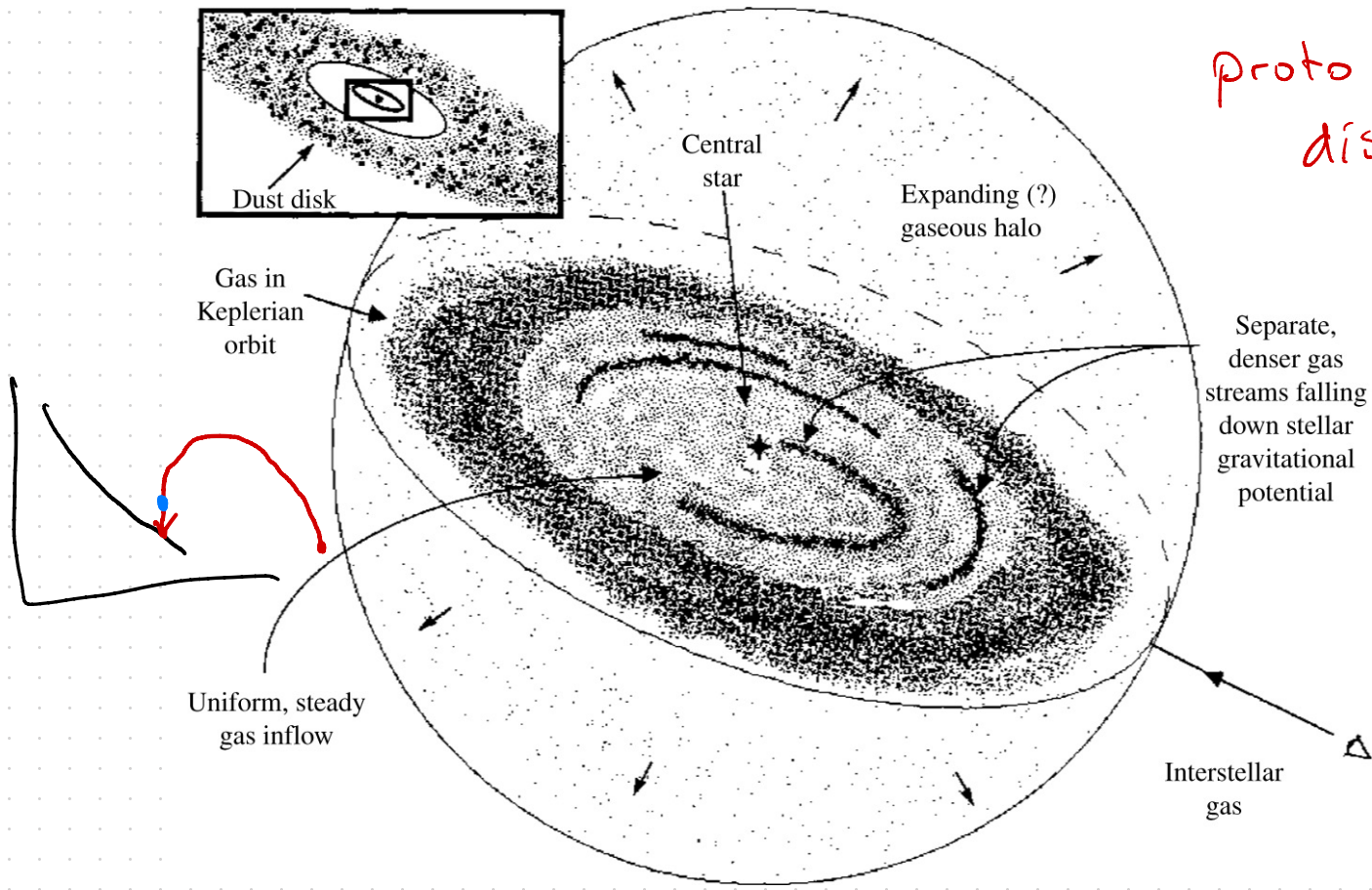
$$m - M = 5 \log_{10} d(\text{pc}) - 5$$

proto
star





proto planetary
disk



Central star

Expanding (?) gaseous halo

Gas in Keplerian orbit

Separate, denser gas streams falling down stellar gravitational potential

Uniform, steady gas inflow

Interstellar gas

Galilean Satellites of Jupiter (1610)

	Mass <small>x Earth moon</small>	Radius	Density
Io	1.2	1.1	3500 kg/m ³
Europa	0.65	0.9	3000
Ganymede	2.0	1.5	1900
Callisto	1.5	1.4	1800

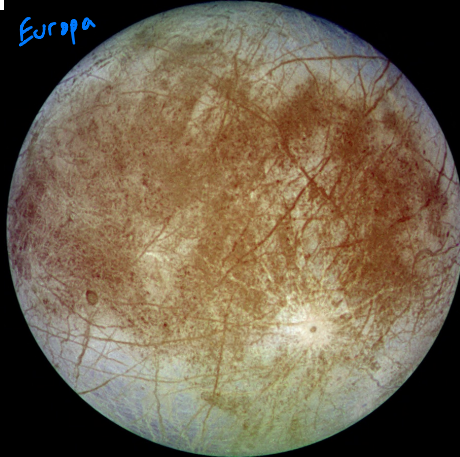
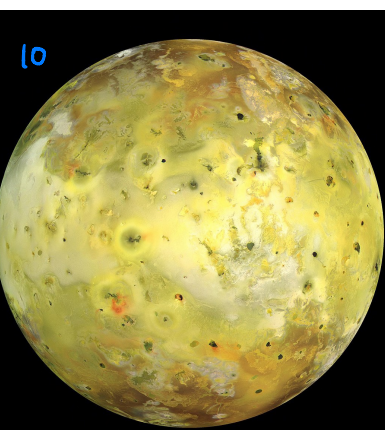
kg/m³

Iron ~ 7000

Rock ~ 3000

H₂O ice ~ 1000

$\rho_{\text{Earth}} \sim 5500$



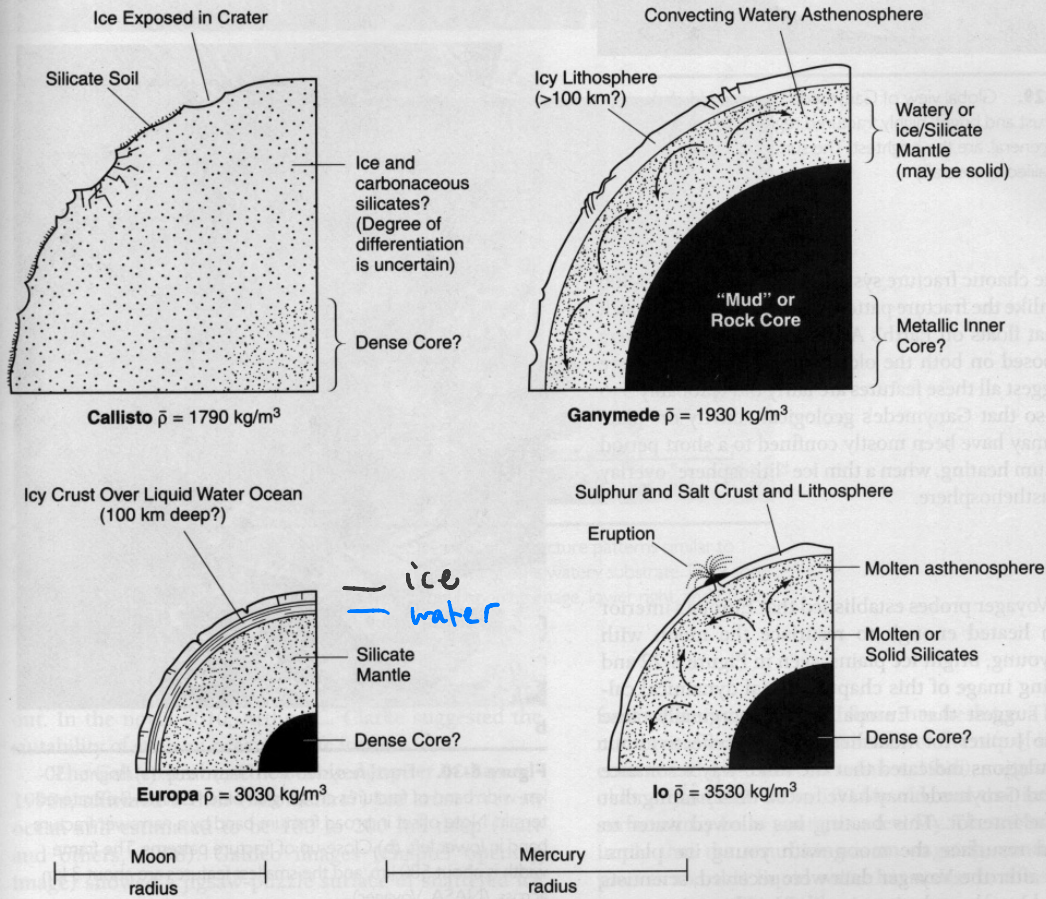
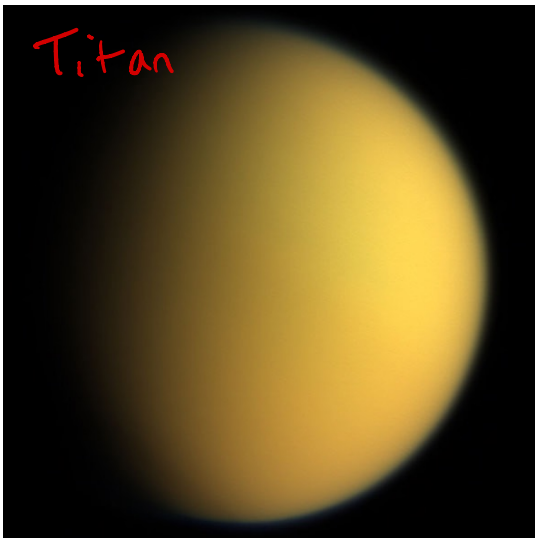


Figure 8-28. Schematic models of the Galilean satellite interiors based on thermal calculations and data from Voyager and Galileo probes. (Adapted from data reviews by Torrence Johnson, plus recent references mentioned in text)

Titan



Atmosphere!

Second largest Moon

Methane

surface pressure

Nitrogen

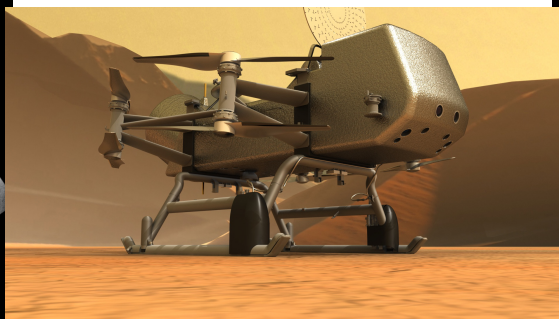
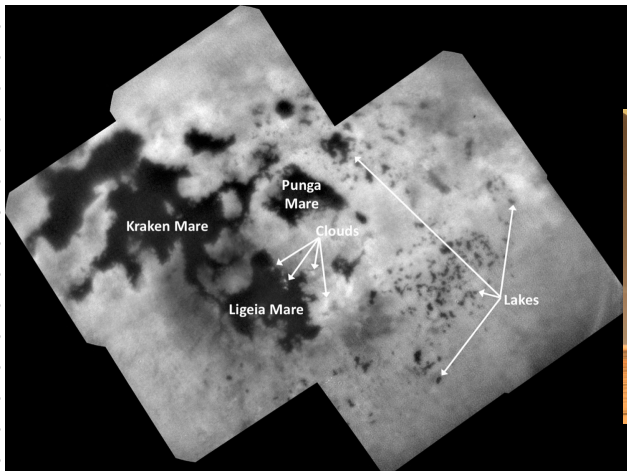
1.5 atm

Argon

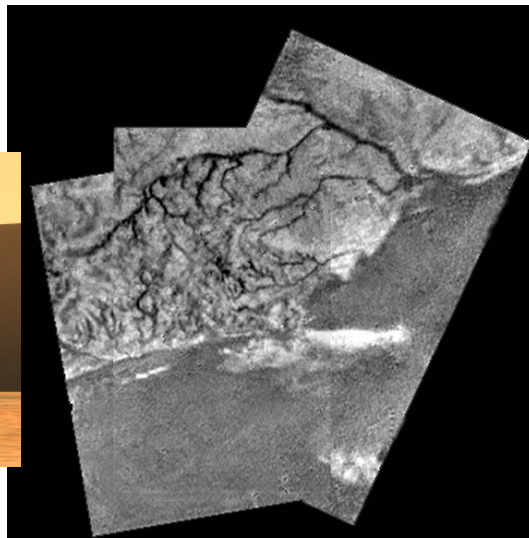
Ethane, Propane, other Organics

Cold surface 94 K

methane triple point
= 91 K



Drone mission launch 2027



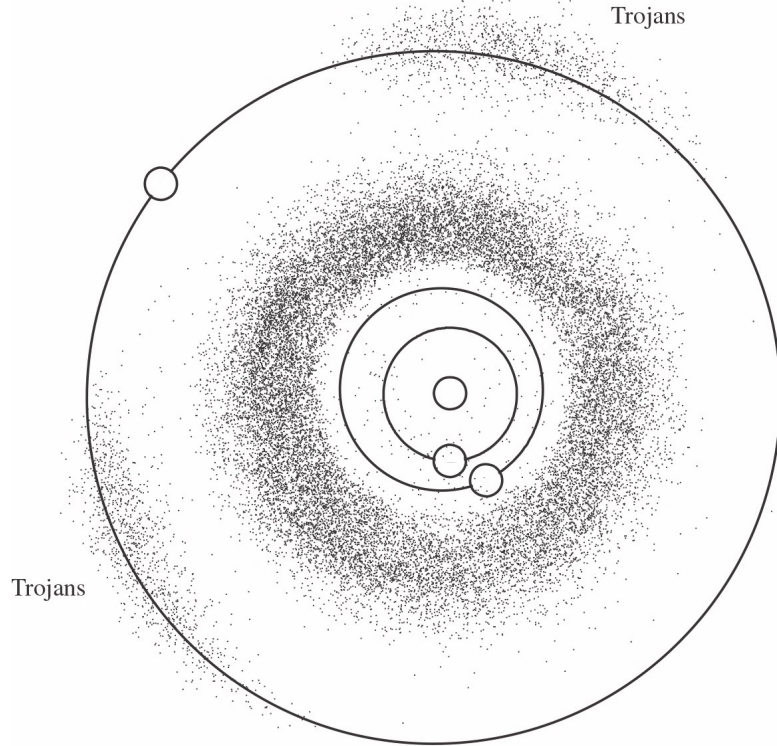
Asteroids

Small rocky bodies "mostly" between Jupiter & Mars

↳ Asteroid belt



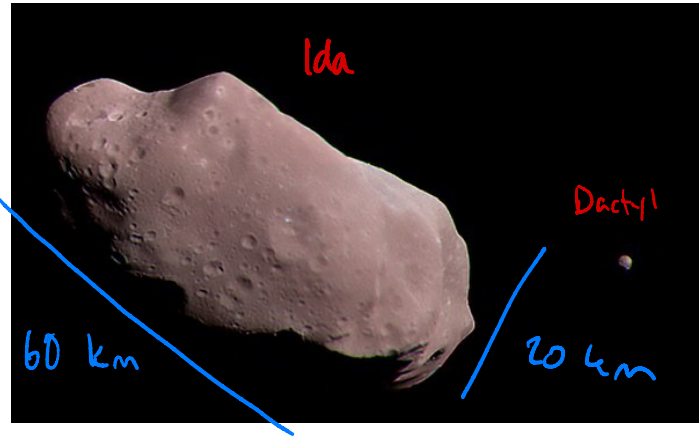
What are asteroids?



$N(R) \propto 1/R^2$ size distribution

biggest = Ceres 900 km

only 26 bigger than 200 km



material was never able to form a planet

add up to less than mass of Earth's moon

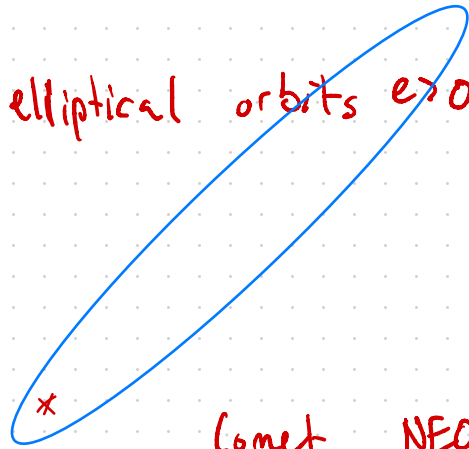
10-30% of asteroids have moons
"satellites"

Comets

"Dirty Space Snowballs"

- mostly water ice
- ammonia
- silicates (dust)
- organic material

highly elliptical orbits $e > 0.9$



Comet NEOWISE

Nucleus ~ a few km

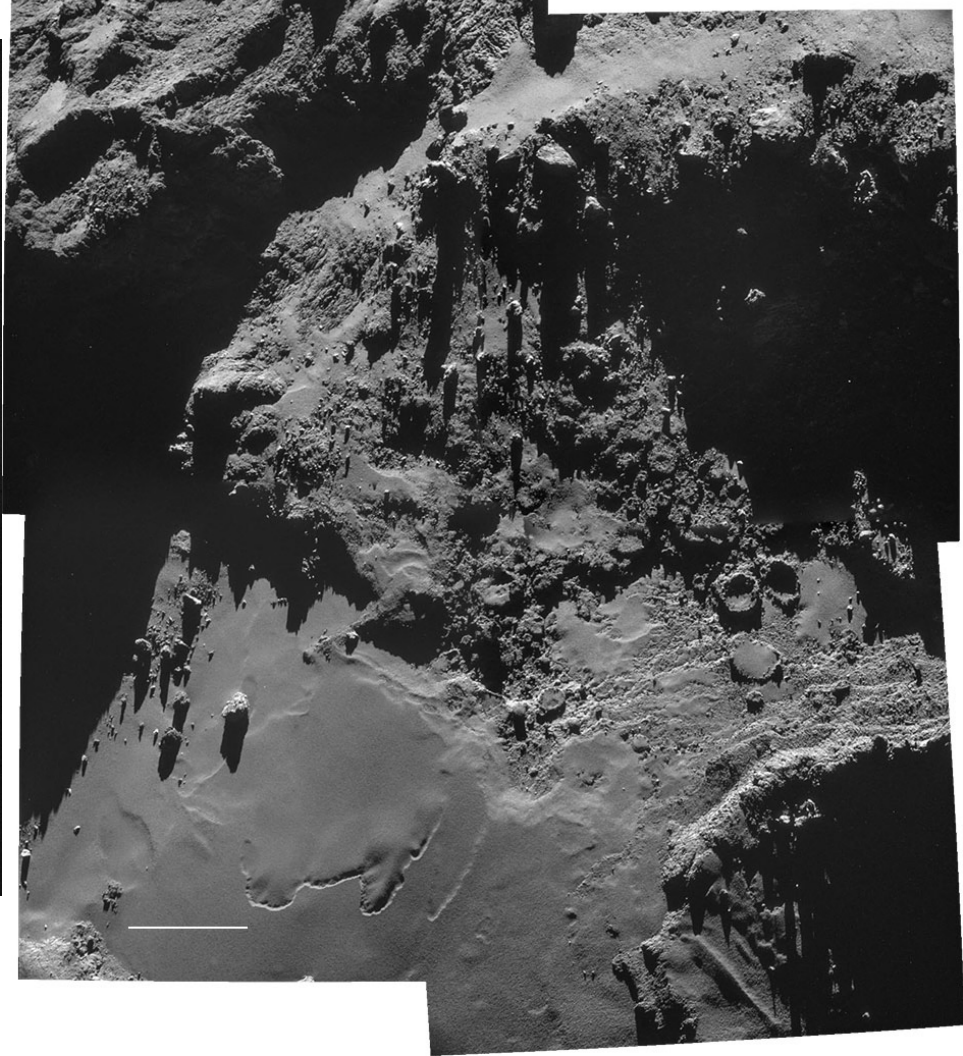
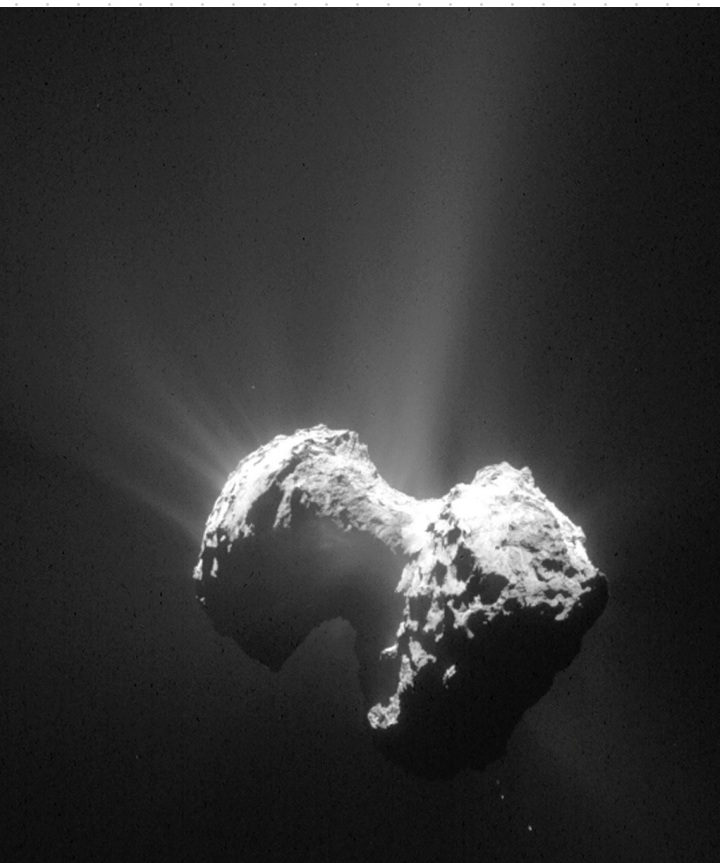
Coma heated cloud of gas/dust
~ 10,000 km

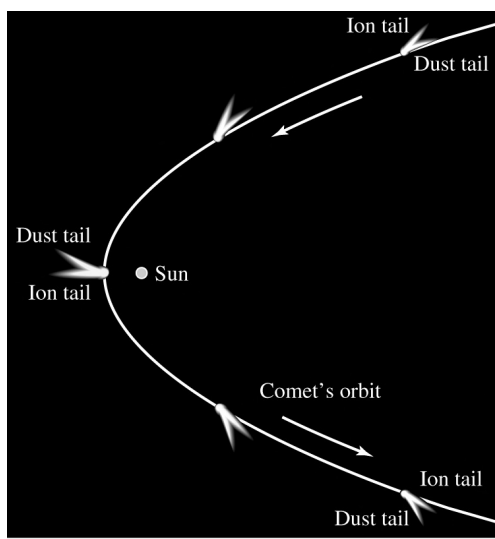
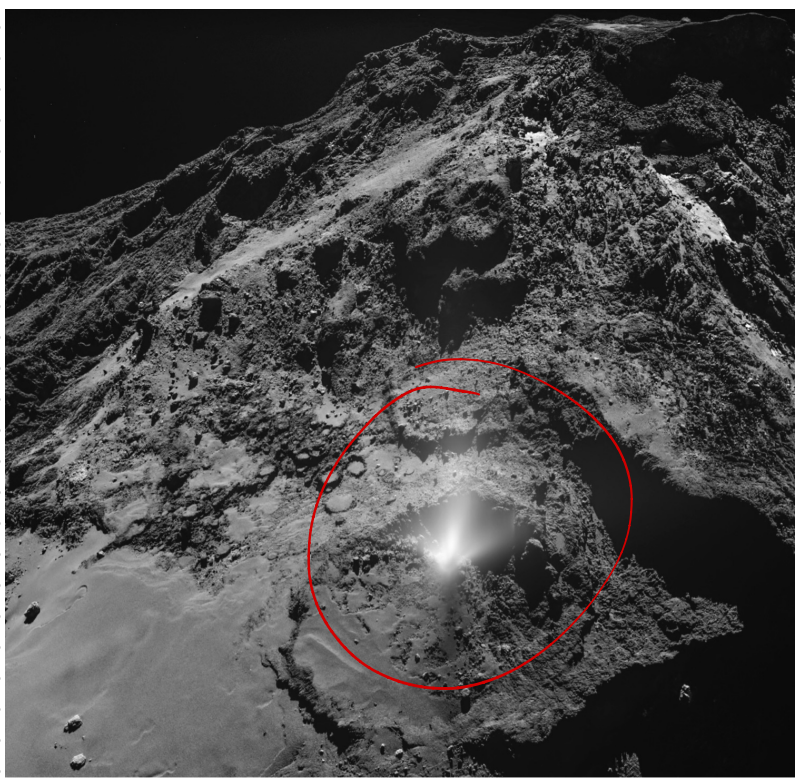
Tail ~ a few million km long

ion tail solar wind, magnetic field lines

dust tail trailing particles pushed by radiation pressure







Radiation Pressure

photons
can
carry
momentum

$$P = \frac{dP}{c}$$

Luminosity

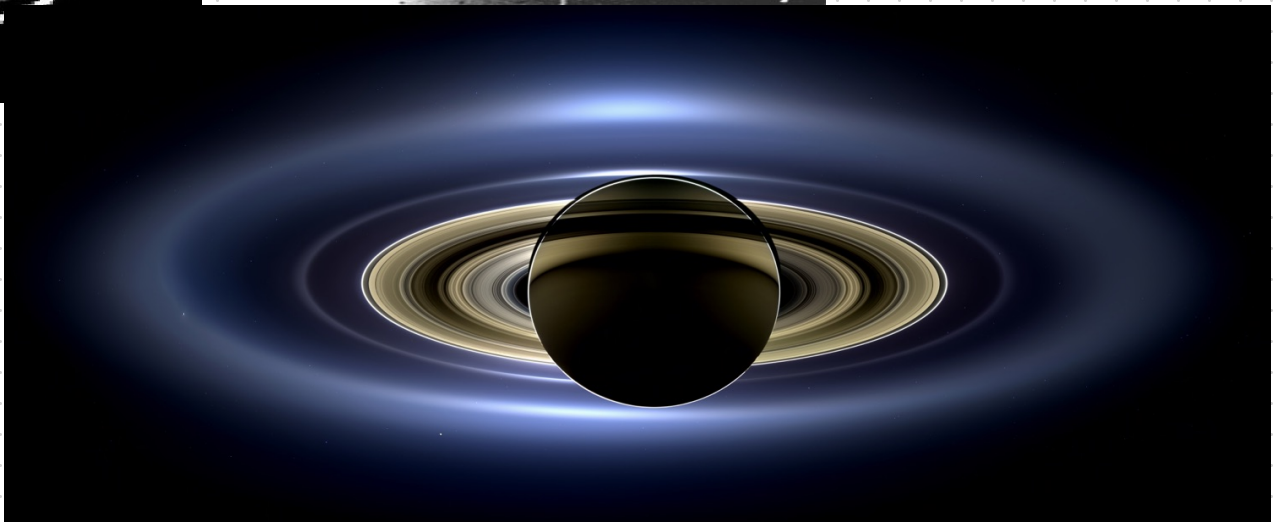
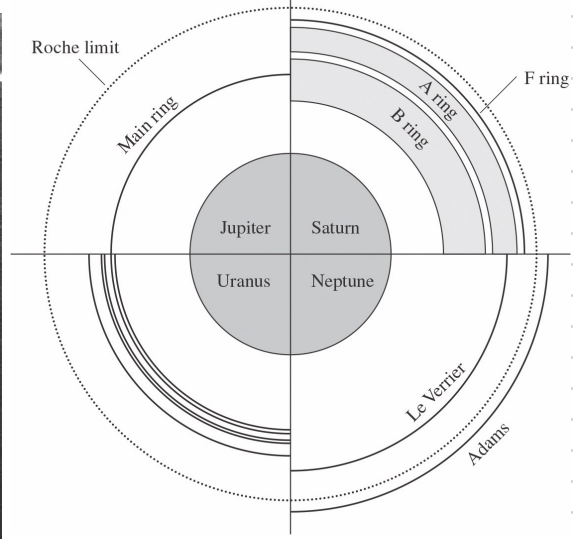
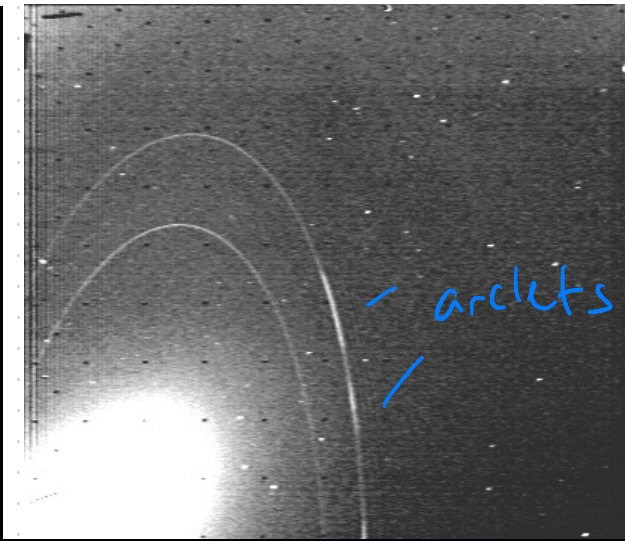
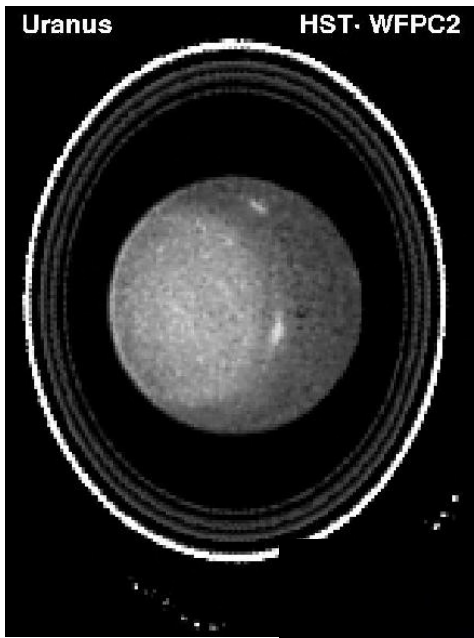
$$F = \frac{dP}{dt} = \frac{1}{c} \frac{dE}{dt}$$

consider a shell of radius R

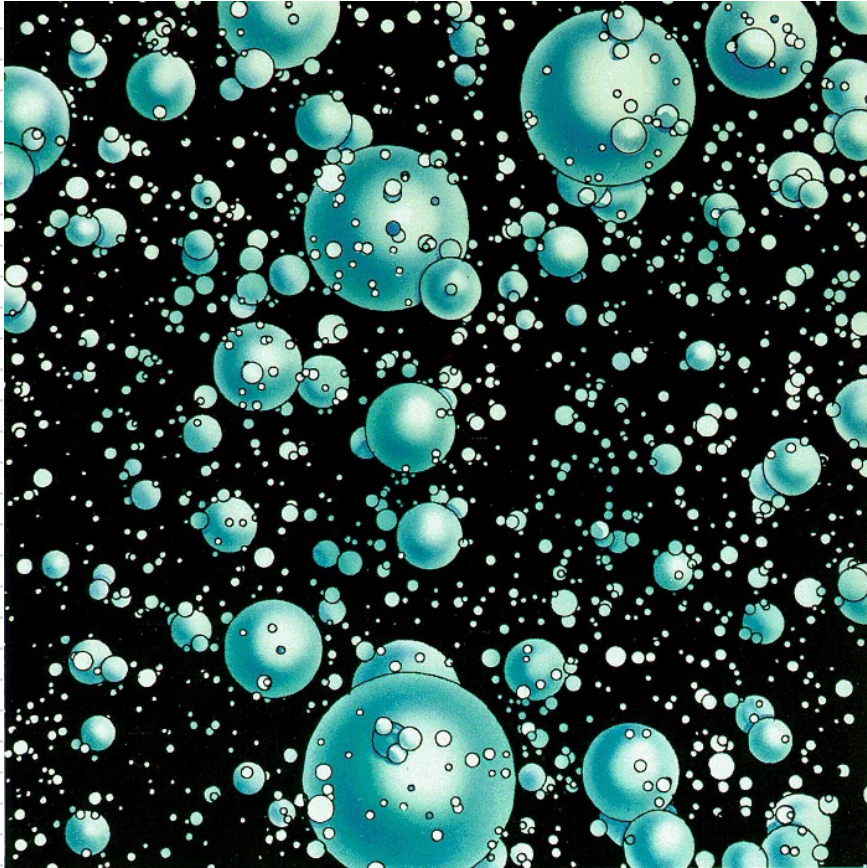
$$\text{pressure} = \text{force/area} = \frac{1}{c} \frac{dE}{dt} / 4\pi R^2$$

$$P_{\text{rad}} = \frac{L_{\odot}}{4\pi R^2 c}$$

↑
distance from Sun



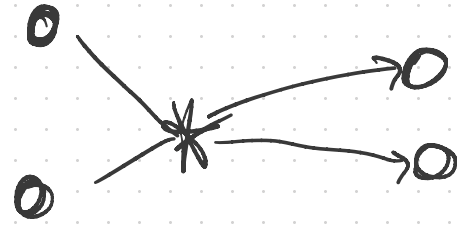
what are rings?



ice particles!

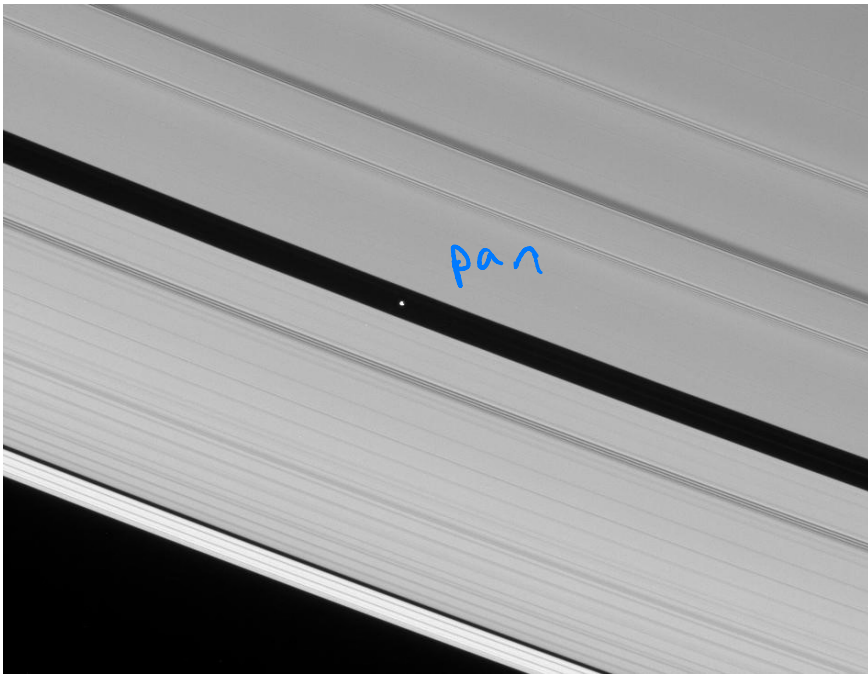
sizes between

1 cm & 3 m

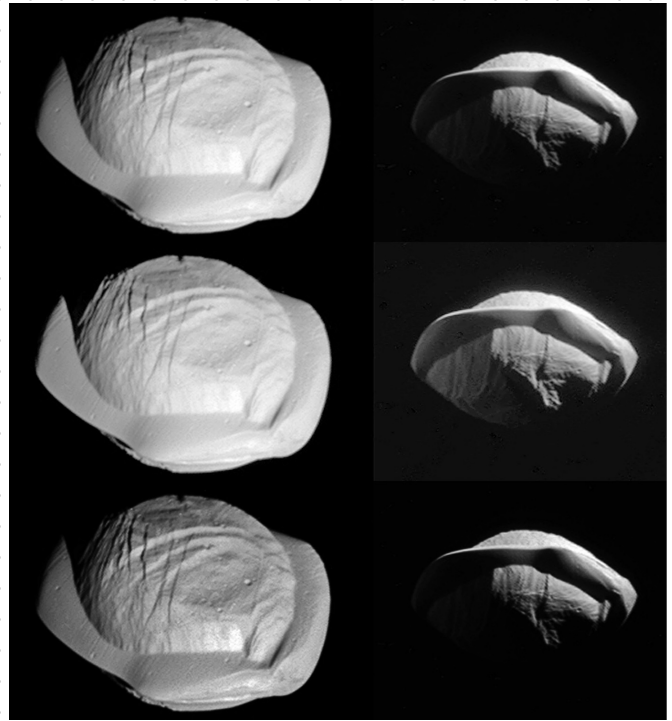


only a "few dozen" = 30 m
meters thick

gaps come from orbital
resonances, "shepherd moons"

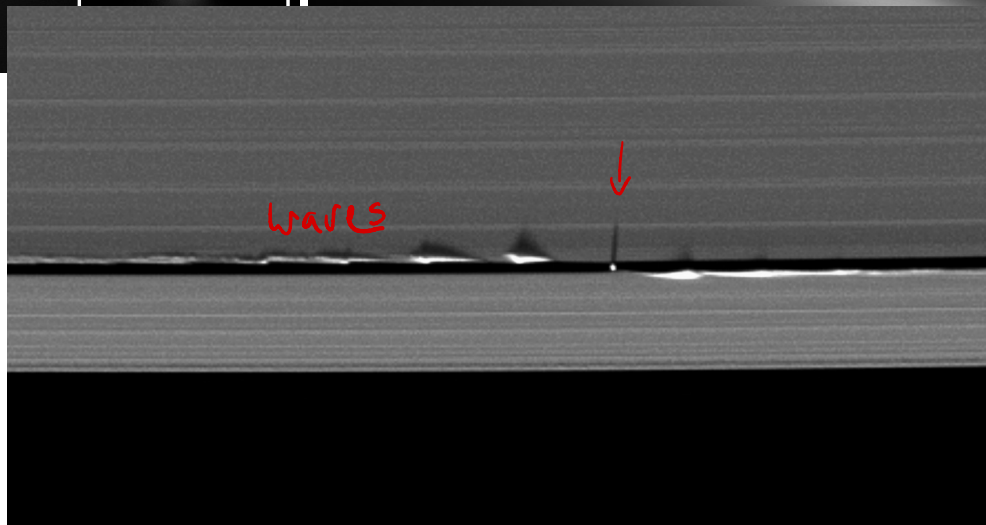
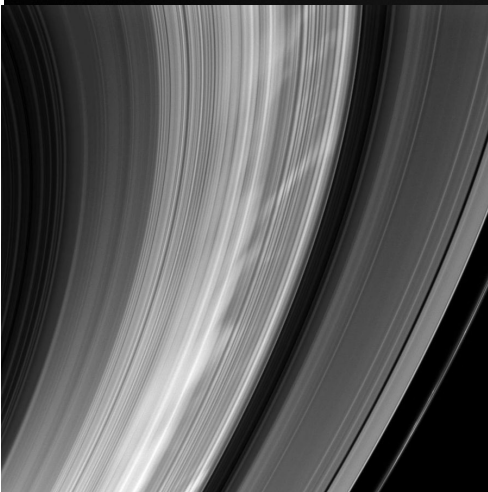
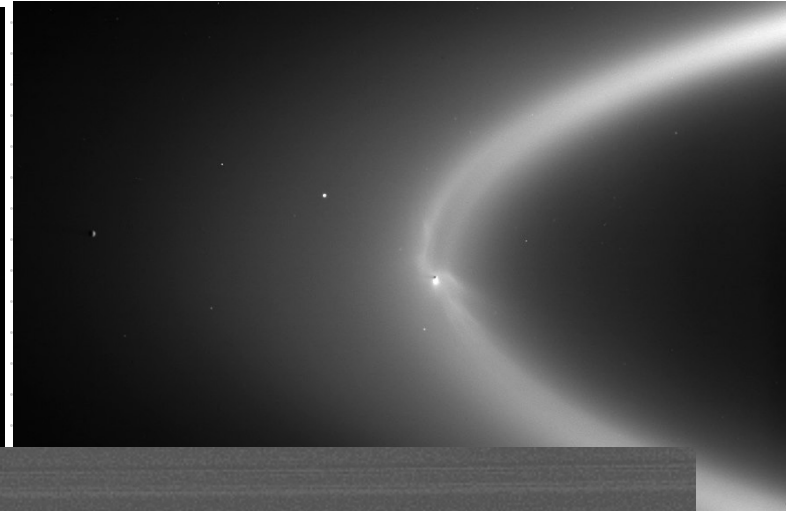
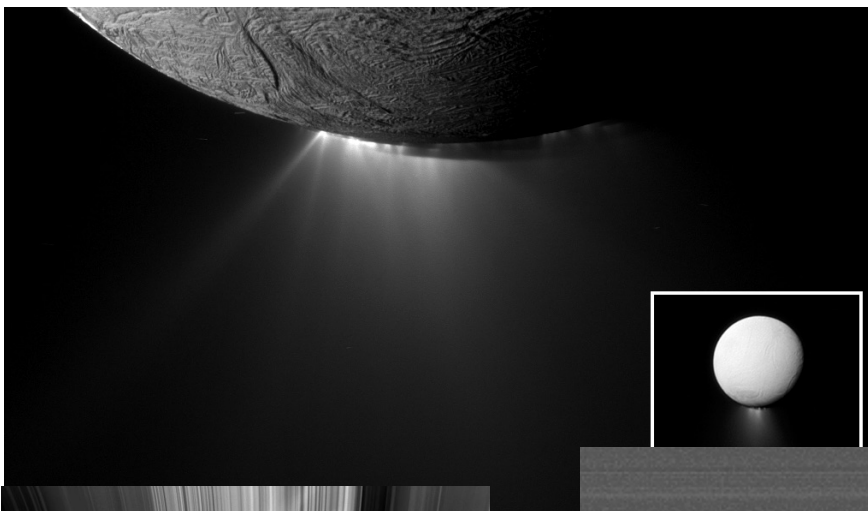


why are rings?



Pan up close

Space ravioli



Kuiper Belt Objects

outside of Neptune's orbit

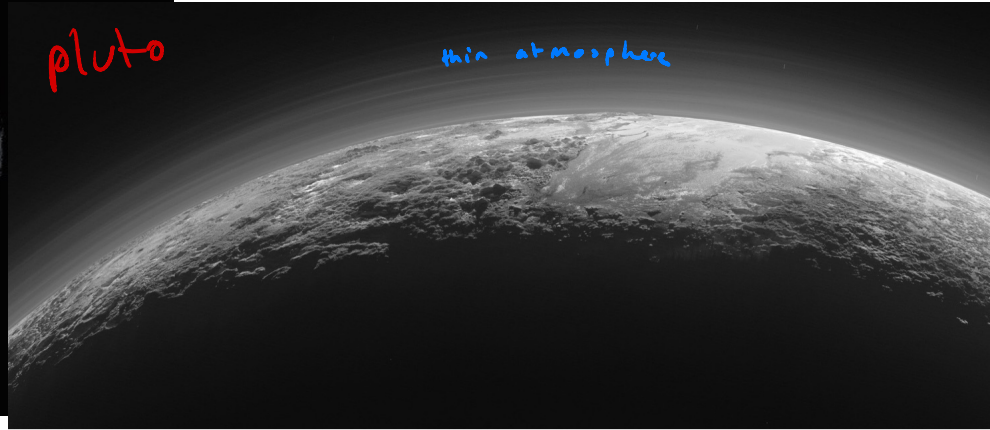
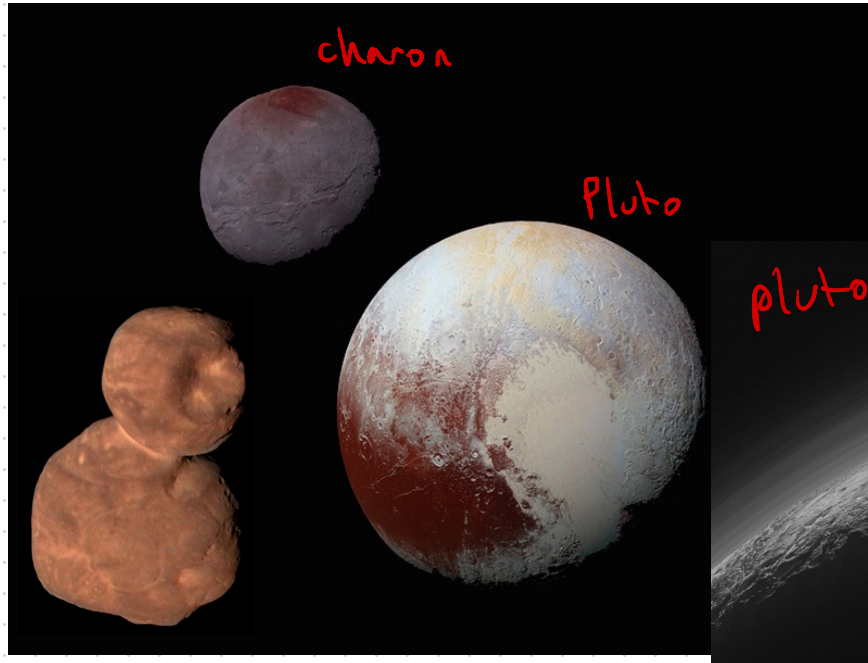
Pluto and Friends

dwarf planet

rock and ice combined

Oort cloud (spherical)

source of comets



Earth's Atmosphere	
% by #	#
78%	N_2
21%	O_2
1%	Ar
0.04%	CO_2
trace	Ne, He, CH ₄ , Kr

pressure gradient follows
ideal gas Law + hydrostatic
equilibrium

$$P(r) = P_0 e^{-\frac{r-R_0}{H}}$$

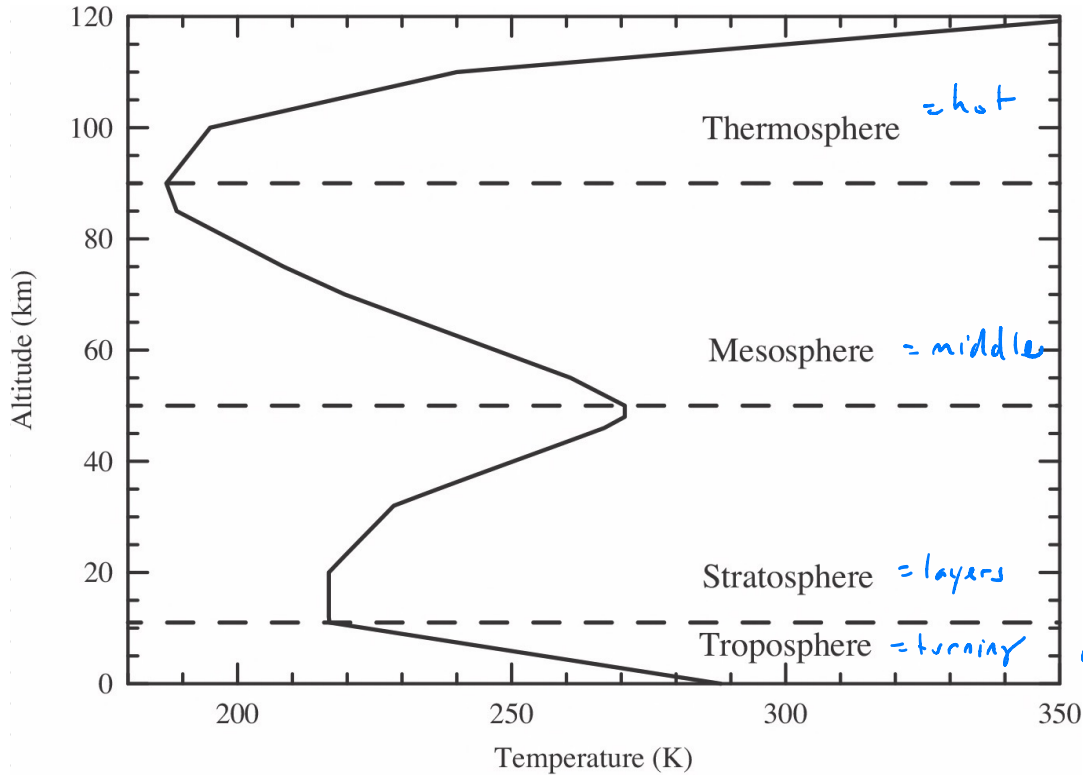
$$P_0 = \text{sea level pressure} = 1 \text{ atm} = 10^5 \text{ N/m}^2$$

$$R_0 = \text{radius} = 6378 \text{ km}$$

$$H = \text{scale height} = \frac{kT}{\mu m_p}$$

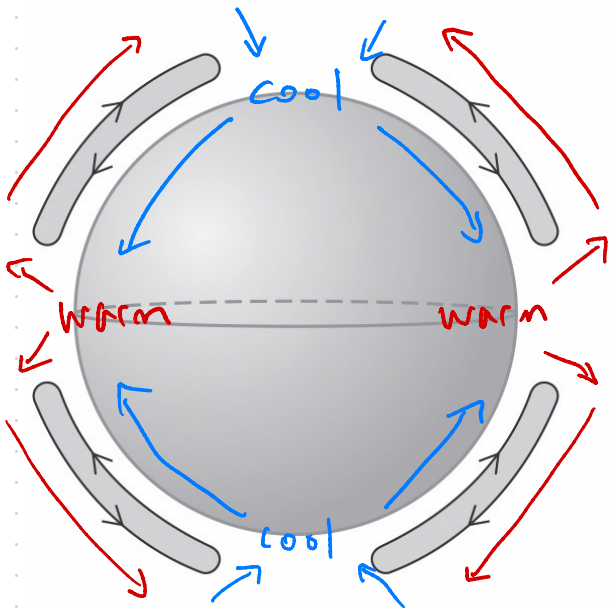
(P drops to 37%)

$$= 8 \text{ km} \sim \text{Mt Everest}$$



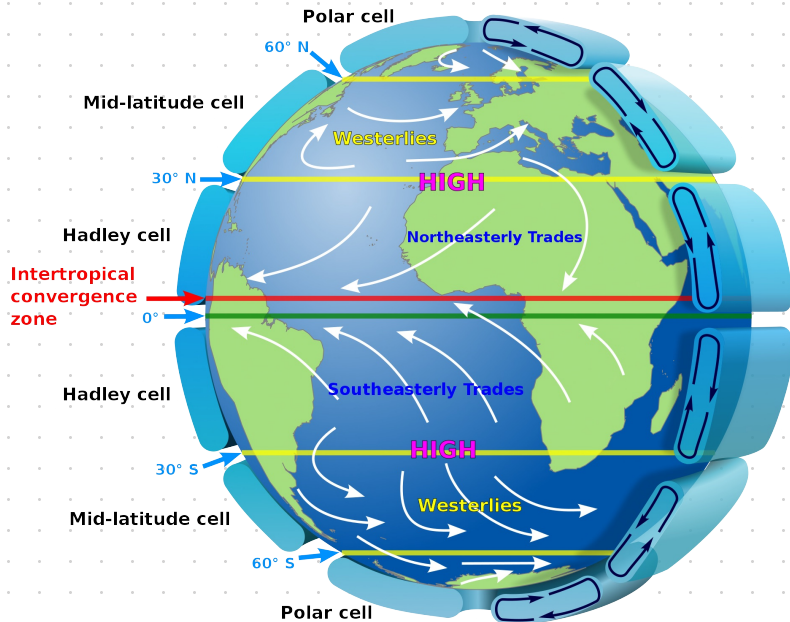
Hadley circulation

simple



(a)

+ Coriolis effect



Jupiter

Saturn

Uranus

Neptune

Radius $\sim 70,000 \text{ km}$

1

0.85

0.36

0.35

Mass $\sim 1 \times 10^{27} \text{ kg}$

1

0.3

0.045

0.053

Density $\text{H}_2\text{O} = 1,000$ 1,330 kg/m^3 690 kg/m^3 1,270 kg/m^3 1,640 kg/m^3

Distance from Sun

5.2 AU

9.5 AU

19.2 AU

30.1 AU

 T_{eq}

110 K

80 K

60 K

45 K

 T_{obs}

125 K

95 K

60 K

60 K

Notes

cloud patterns

cloud patterns

featureless

cloud patterns

faint rings

rings!

tiny rings

"arclets"

20+ moons

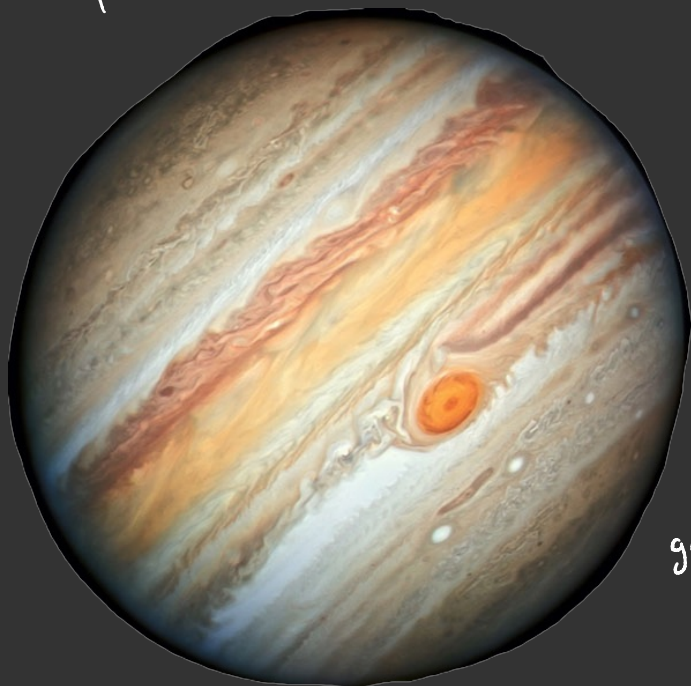
50+ moons

20+ moons

20+ moons

 $t_{\text{rot}} = 10 \text{ hr}$ $t_{\text{rot}} = 10.6$ $t_{\text{rot}} = 17.3 \text{ hr}$ $t_{\text{rot}} = 19.2 \text{ hours}$ axis tilt $\sim 90^\circ!$

Jupiter



atmosphere composition

Hydrogen, Helium

Ammonia (NH_3), Methane (CH_4)

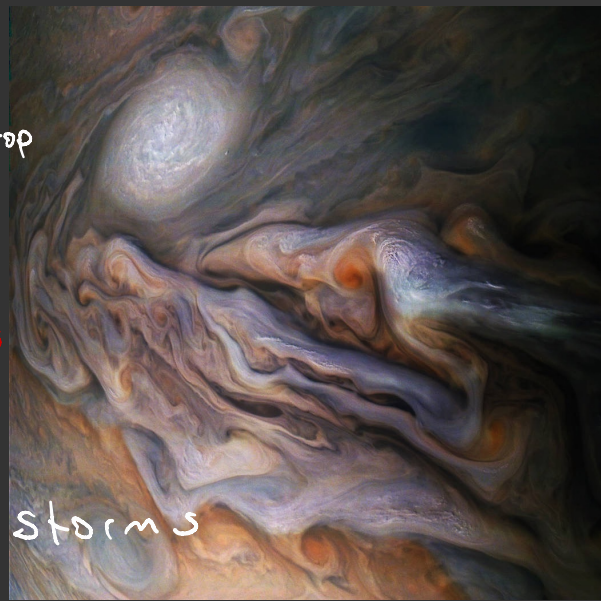
Ammonia Hydrosulfide (NH_4HS)

bright "zones" =
gas moving \uparrow , see cool top

dark "bands" =
gas moving \downarrow , darker inner
layers

Stripes = convection bands

shear between cloud bands causes cyclonic storms



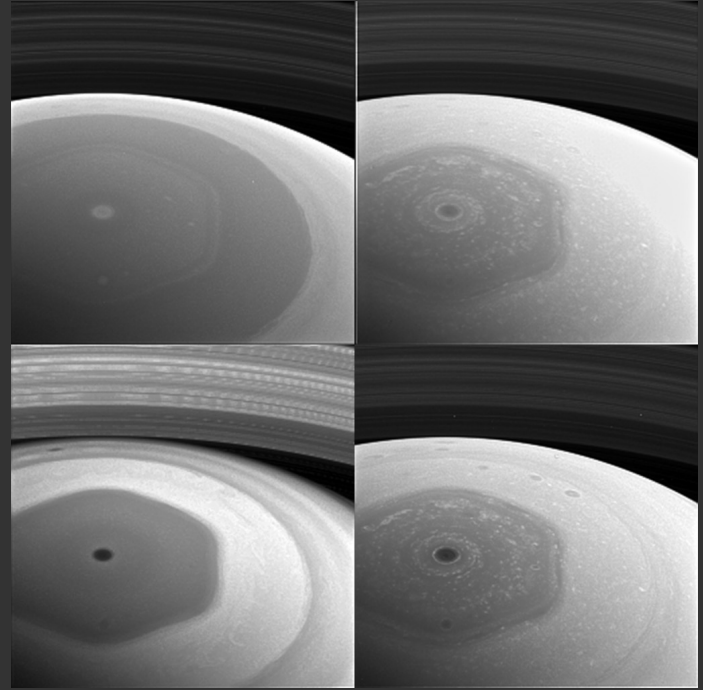
Saturn



polar hexagon!

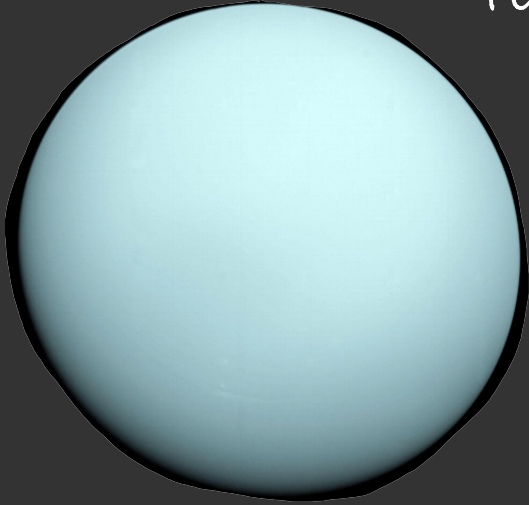
composition

H, He, methane, ammonia, water ice



video

Uranus

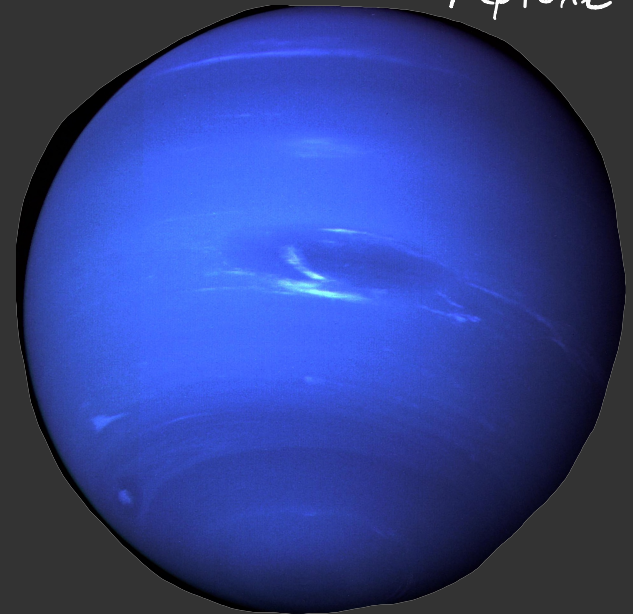


relatively featureless surface

due to lack of convection

Uranus is @ equilibrium temp!

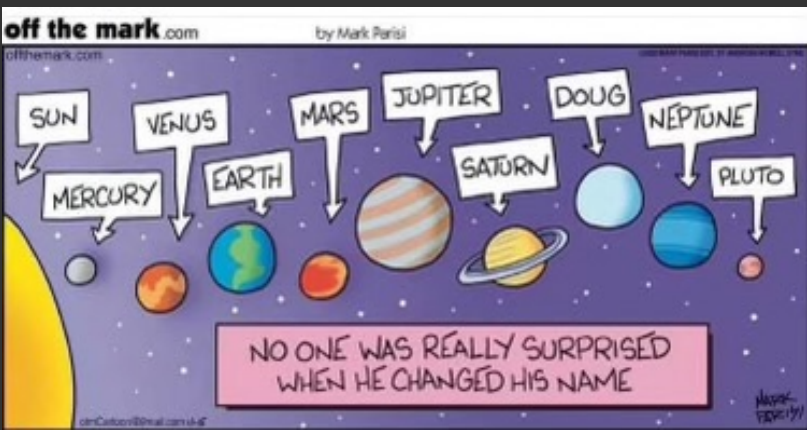
Neptune



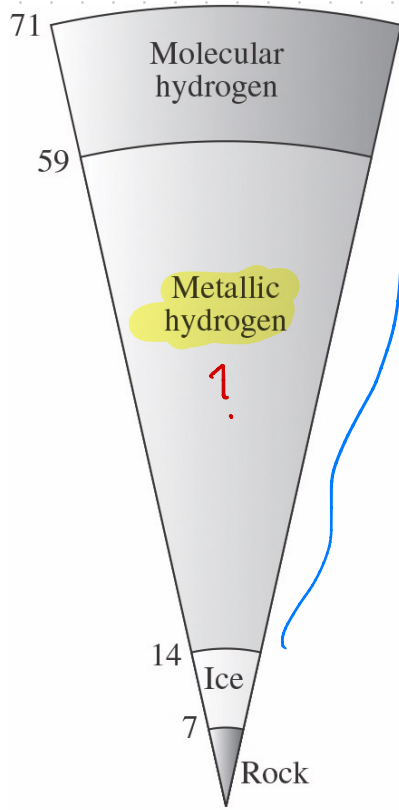
great dark spot

color differences due to molecular differences

T, UV light → ammonia, methane, etc
yellow blue red

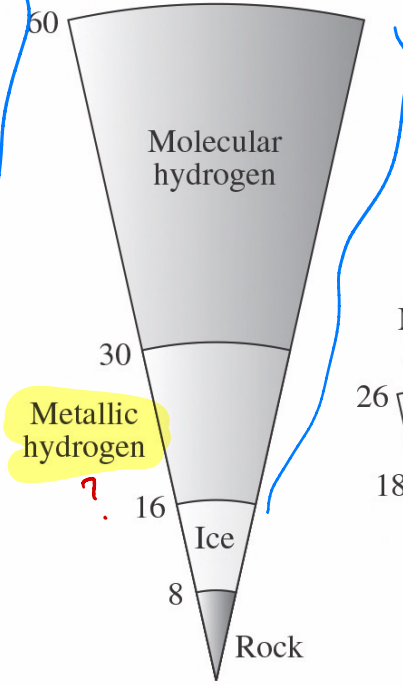


interior structures

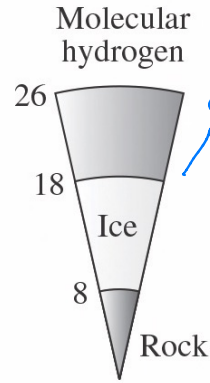


(a) Jupiter

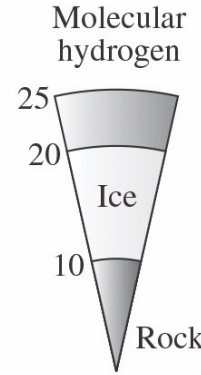
"metallic" = lattice structure + free e^- → generates magnetic field



(b) Saturn



(c) Uranus



(d) Neptune

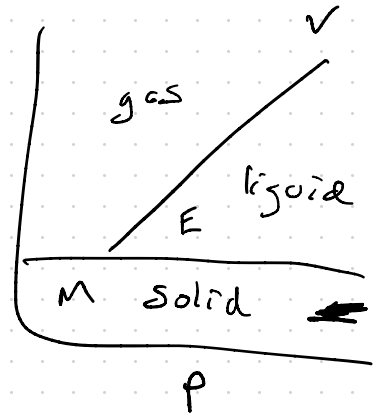
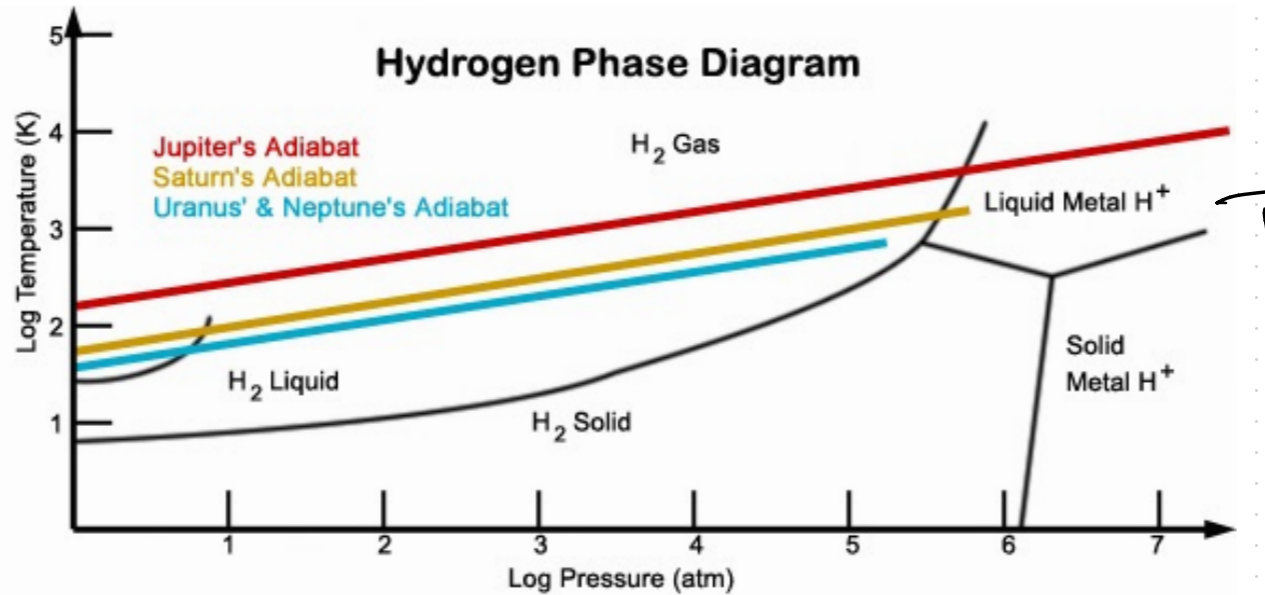
explain relative amounts?

atmospheres

ice / rock

cores

"adiabat" = temp/pressure gradient



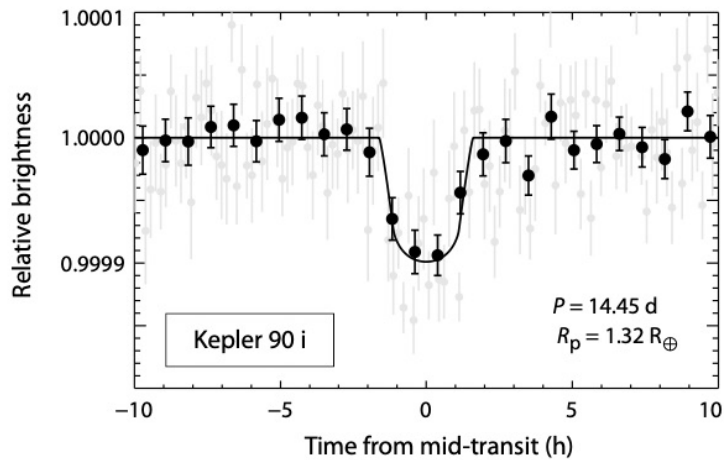
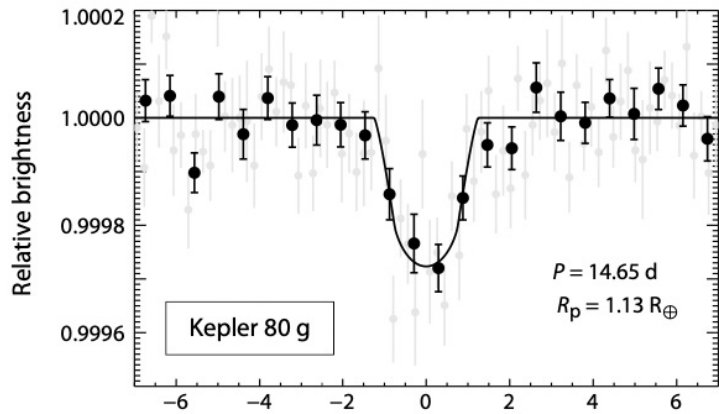
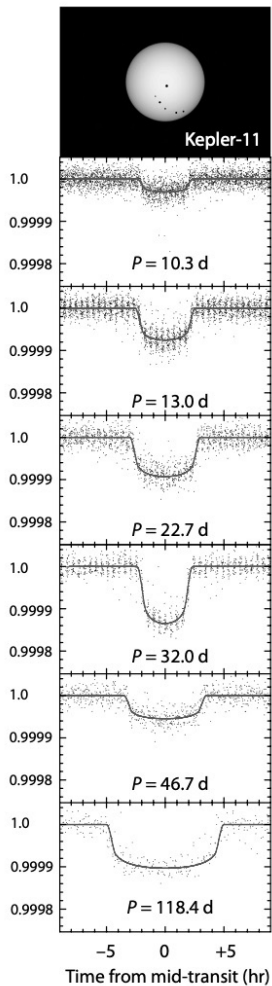
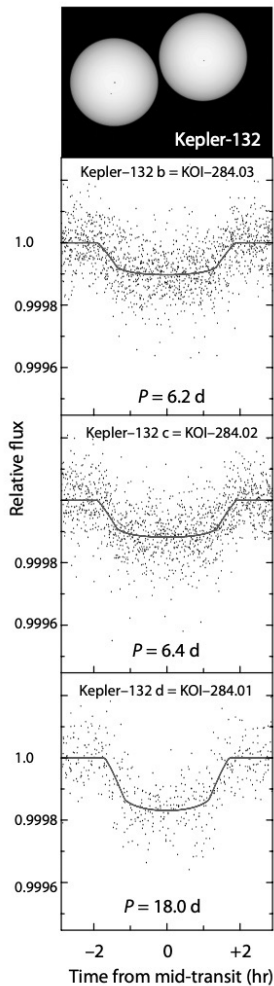
sources of internal heat? excess heat drives convection/cloud patterns

heavy element radioactivity

gravitational contraction / material differentiation

greenhouse gases (methane; Neptune)

cooling time



Equilibrium Temperature

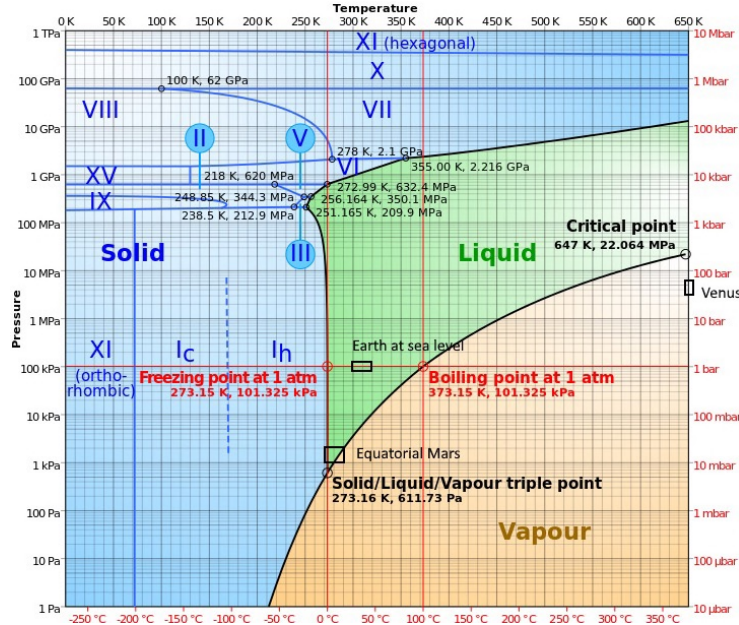
$$T_{eq} = T_* \sqrt{\frac{R}{2a}} (1 - A_B)^{1/4}$$

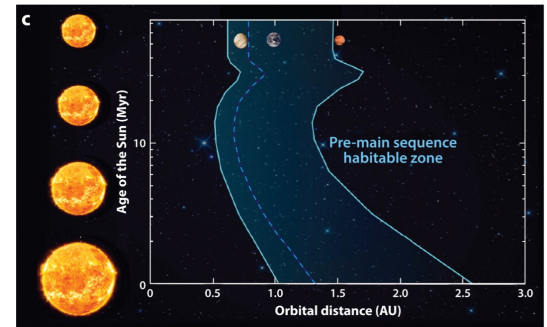
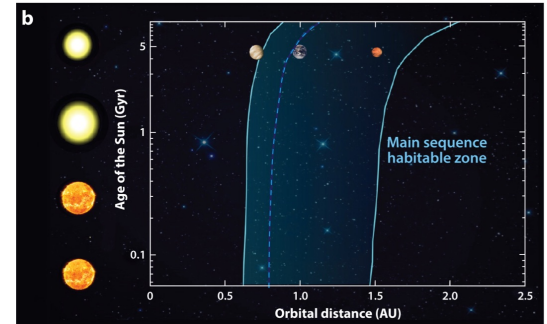
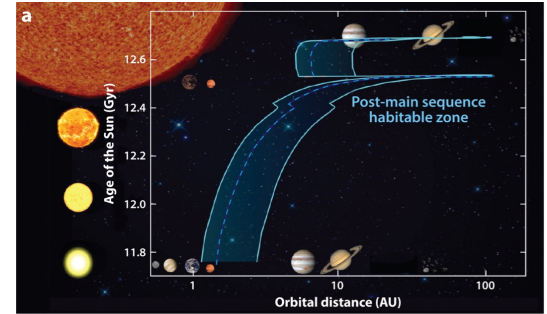
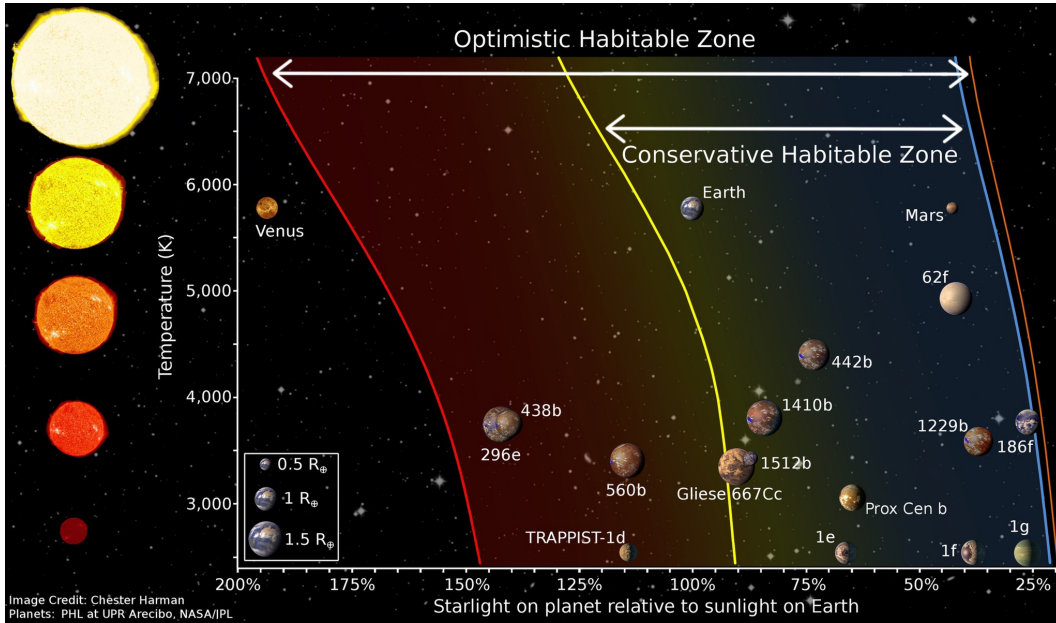
ability to retain heat affected by presence of atmosphere, greenhouse gases, internal heating

a = semimajor axis
 R = star radius
 T_* = star temp
 A_B = "albedo"
 \Rightarrow % light reflected

Habitable Zone

range of orbits around a star within which a planetary surface can support liquid water given sufficient atmospheric pressure



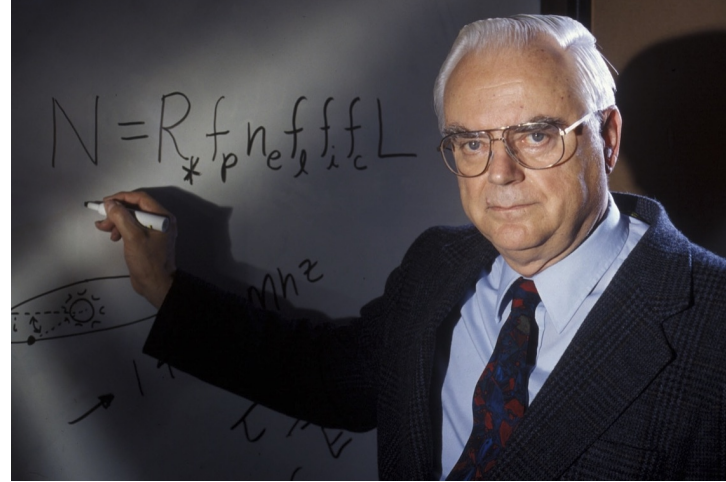


what about moons?

The Drake Equation

30 Nov 1961

60 years ago!



Frank Drake

The number of detectable civilizations in the Milky Way galaxy

The fraction of stars that host planets

The fraction of those planets on which life evolves

The fraction of intelligent life that develops communicative technologies

$$N = R_* \times f_p \times n_e \times f_l \times f_i \times f_c \times L$$

The rate at which stars are born

The number of habitable planets per planetary system

The fraction of life that evolves intelligence

The average length of time civilizations are detectable

	N	R*	f _p	n _e	f _L	f _i	f _c	L
1.	10 ⁻¹⁹	1	0.1	10 ⁻²	10 ⁻⁶	10 ⁻⁴	10 ⁻¹⁰	10 ⁴
2.	10 ⁻⁸	1	0.1	0.1	0.001	0.001	0.0001	5,000
3.	10 ⁻⁹	1	0.1	1.5	0.01	10 ⁻⁶	0.0001	1000
4.	10 ⁻⁴	1	0.1	4	0.01	10 ⁻⁷		50,000
5.	10 ⁻⁶	1	0.1	3	1/3	0.19	5 × 10 ⁻⁷	200
6.	10 ⁻⁹	1	0.1	2	1/5000	1/10 ⁶	1/50	2000
Ray	0.002	1	0.2	2	1	10 ⁻⁵	1	500
Bill	200	1	0.1	2	1	1	1	1000