

The Radial Acceleration Relation of Galaxies



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In collaboration with:

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Outline:

1. The SPARC Galaxy Database
2. Results for Late-Type Galaxies (S & dIrr)
3. Results for Early-Type Galaxies (E, S0, dSph)

SPARC

Spitzer Photometry & Accurate Rotation Curves



Database for 175 late-type galaxies (S & dlrr):

www.astroweb.cwru.edu/SPARC

Lelli, McGaugh, Schombert 2016, AJ

- **HI Rotation Curves for 175 galaxies**
 - 30 years of HI obs with WSRT, VLA, ATCA.
 - PhD theses from the University of Groningen
 - Begeman 1987; Broeils 1992; Verheijen 1997; de Blok 1997; Swaters 1999; Noordermeer 2005; Lelli 2013 + other studies
 - Hybrid H α /HI rotation curves for ~30% sample
 - McGaugh+2001; Kuzio de Naray+2006, 2008 + other studies.



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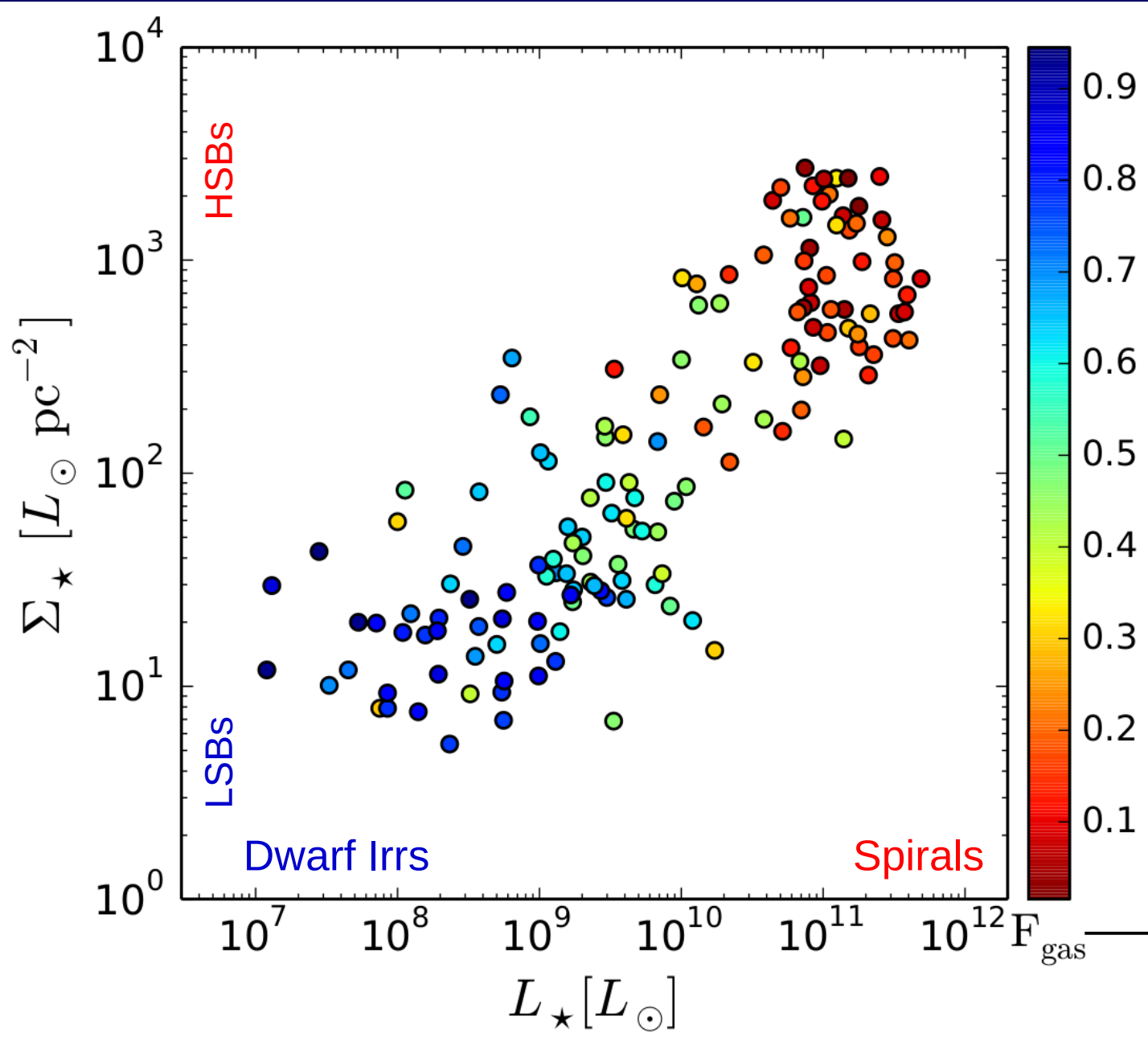


● Homogeneous Photometry at 3.6 μm

- Optimal tracer of the stellar mass: $M_* = Y_* L$
- Smaller variations of Y_* in the NIR than optical
Bell & de Jong 2001; Martinsson+2013; Meidt+2012, 2014;
McGaugh & Schombert 2014; Schombert & McGaugh 2014;
Querejeta+2015; Röck+2015; Herrmann+2016; Norris+2016.



Widest possible range of disk properties



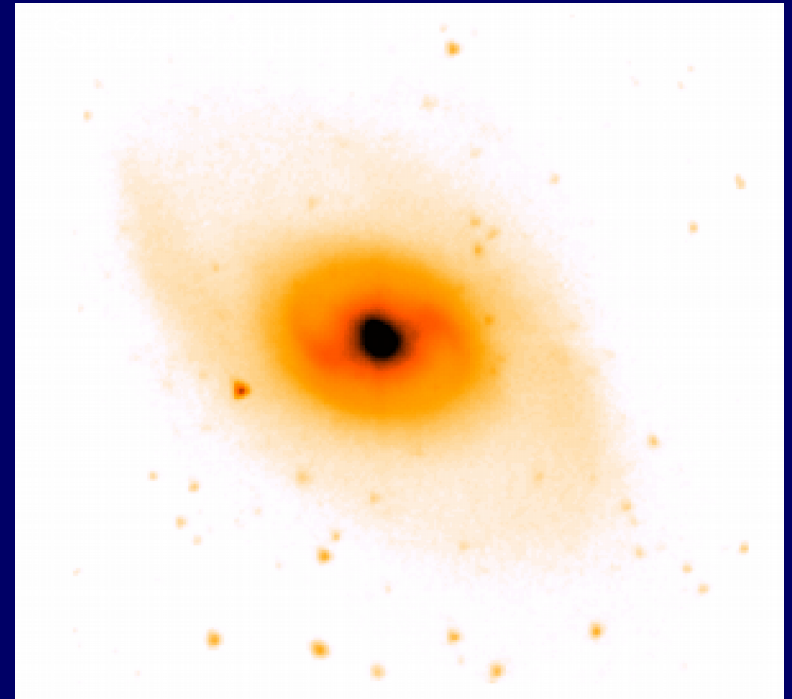
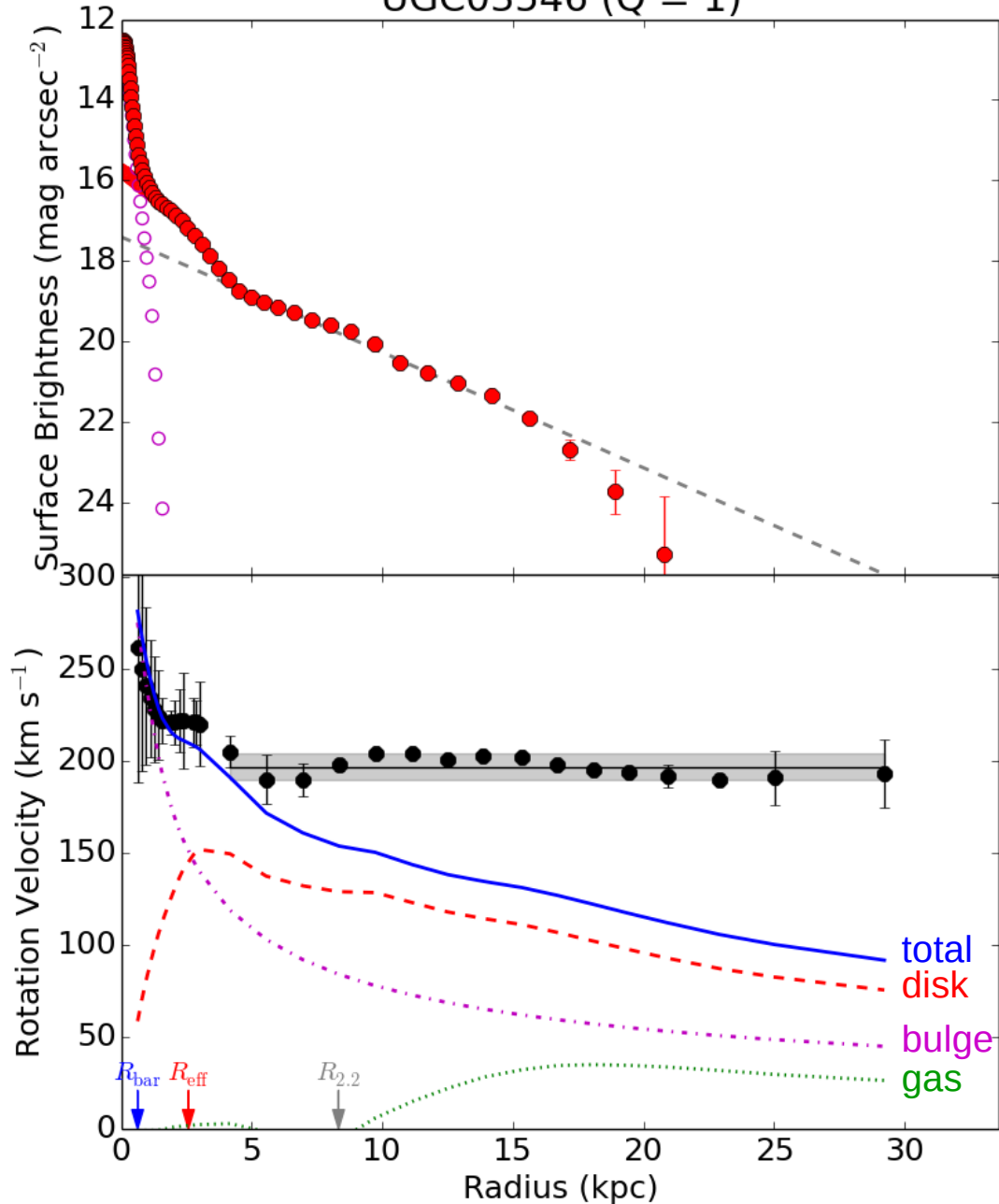
Basically any known galaxy type with a rotating HI disk!



$M_{\text{gas}}/M_{\text{bar}}$

Example: High-Mass HSB Spiral

UGC03546 (Q = 1)



$$\nabla^2 \Phi_{\text{bar}}(R, z) = 4\pi G \rho_{\text{bar}}(R, z)$$

- Vertical Structure:

Disks: $\exp(-z/h_z)$ with $h_z \propto h_R$

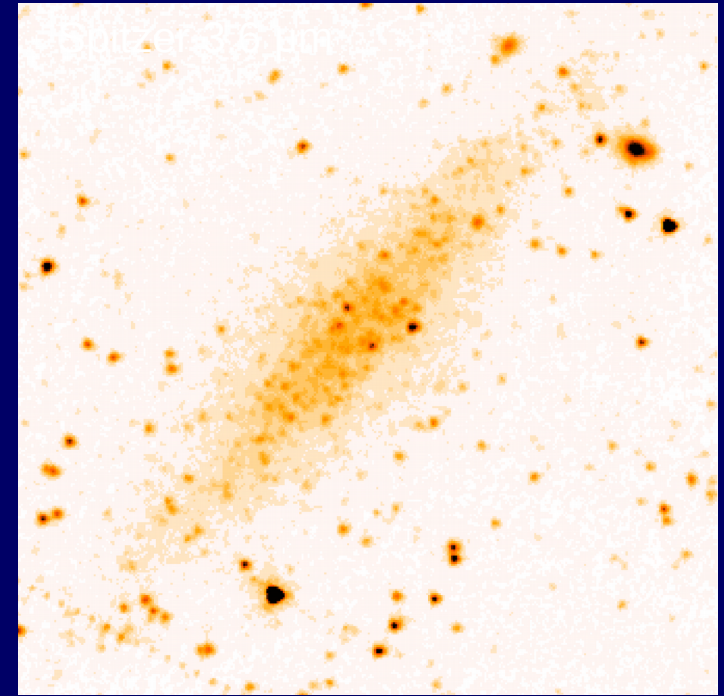
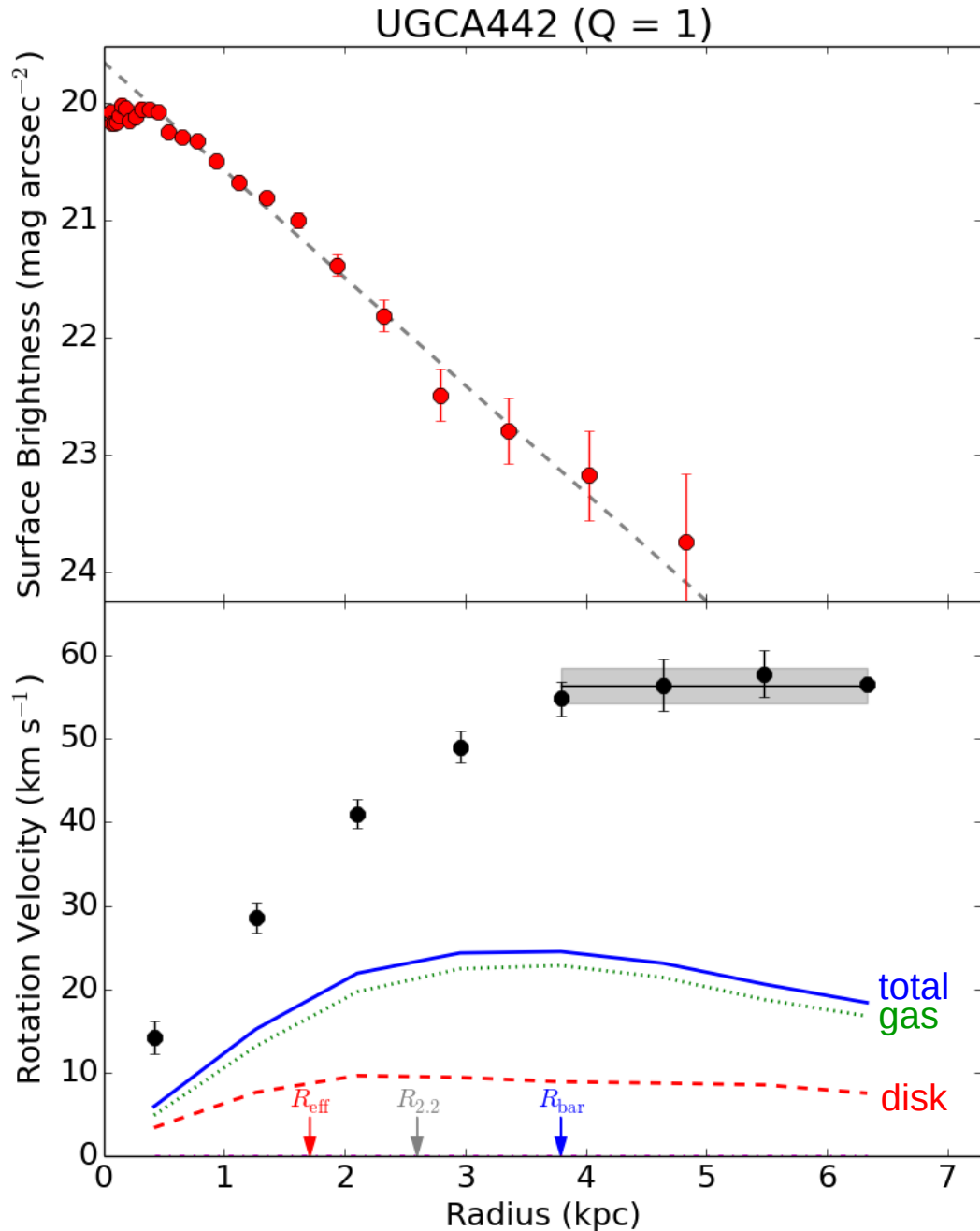
Bulges: spherical symmetry

- Stellar mass-to-light ratio:

$\Upsilon_* = 0.5 M_\odot/L_\odot$ for disks

$\Upsilon_* = 0.7 M_\odot/L_\odot$ for bulges

Example: Low-Mass LSB Dwarf



$$\nabla^2 \Phi_{\text{bar}}(R, z) = 4\pi G \rho_{\text{bar}}(R, z)$$

- Vertical Structure:

Disks: $\exp(-z/h_z)$ with $h_z \propto h_R$

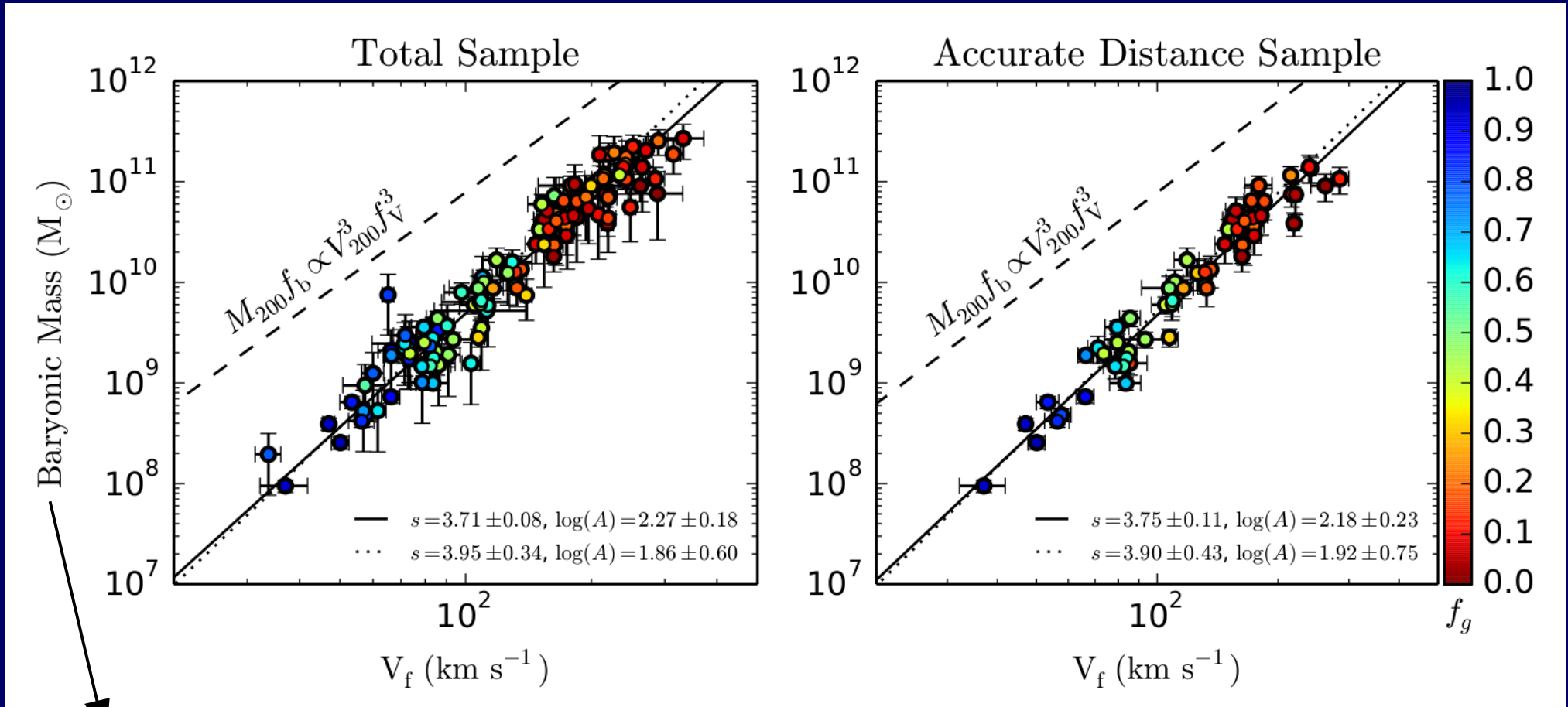
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Baryonic Tully-Fisher Relation (BTFR)



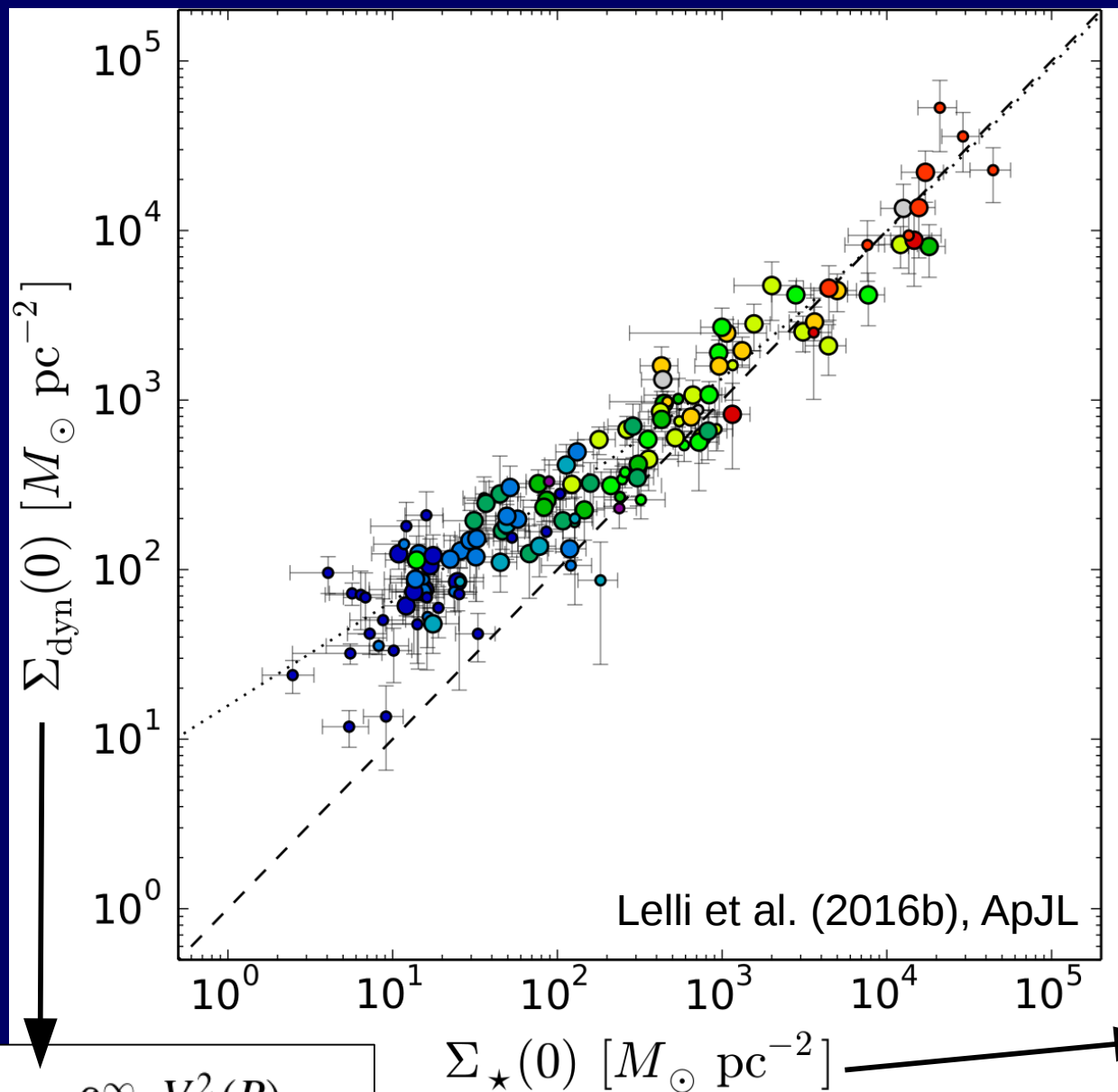
$$M_* + M_{\text{gas}} \propto D^2$$

Lelli, McGaugh, Schombert (2016a), ApJL

GOLDEN RULE: As the data quality increases, the BTFR scatter decreases!

Upper limit on the intrinsic scatter: <0.11 dex (~25%)

Central Density Relation (for $R \rightarrow 0$)



For all galaxies:

$$\Upsilon_{\text{disk}} = 0.5 M_{\odot}/L_{\odot}$$

$$\Upsilon_{\text{bulge}} = 0.7 M_{\odot}/L_{\odot}$$

$$\Sigma_{\text{dyn}}(0) = \frac{1}{2\pi G} \int_0^{\infty} \frac{V^2(R)}{R^2} dR,$$

Toomre (1963): Central Dynamical Density for a Self-Gravitating Disk.

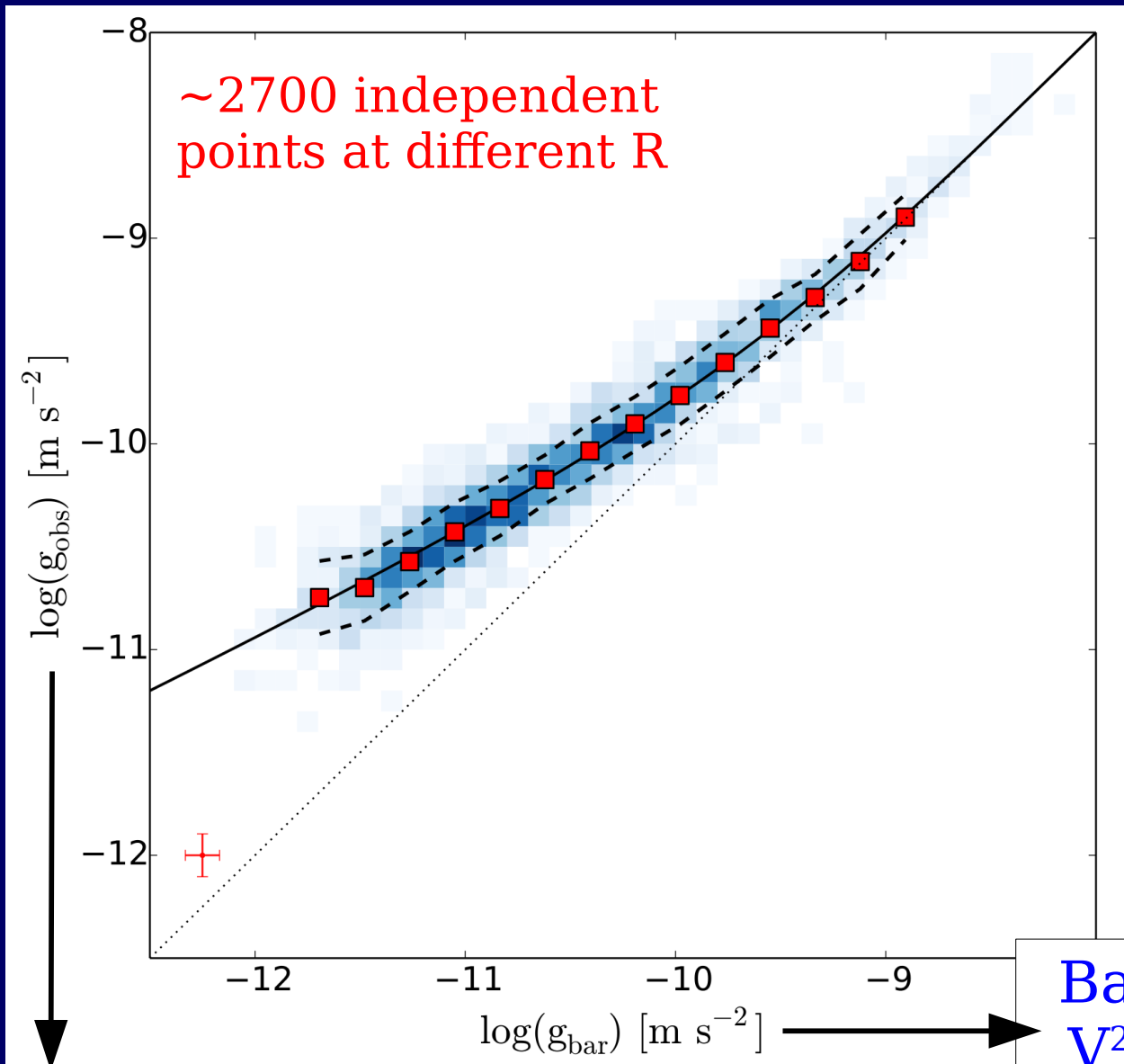
Central Stellar Surface Density

2. Radial Acceleration Relation of Late-Type Galaxies

McGaugh, Lelli, Schombert 2016, PRL

Lelli, McGaugh, Schombert, Pawlowski 2017, ApJ

Local link between baryons and DM



For all galaxies:

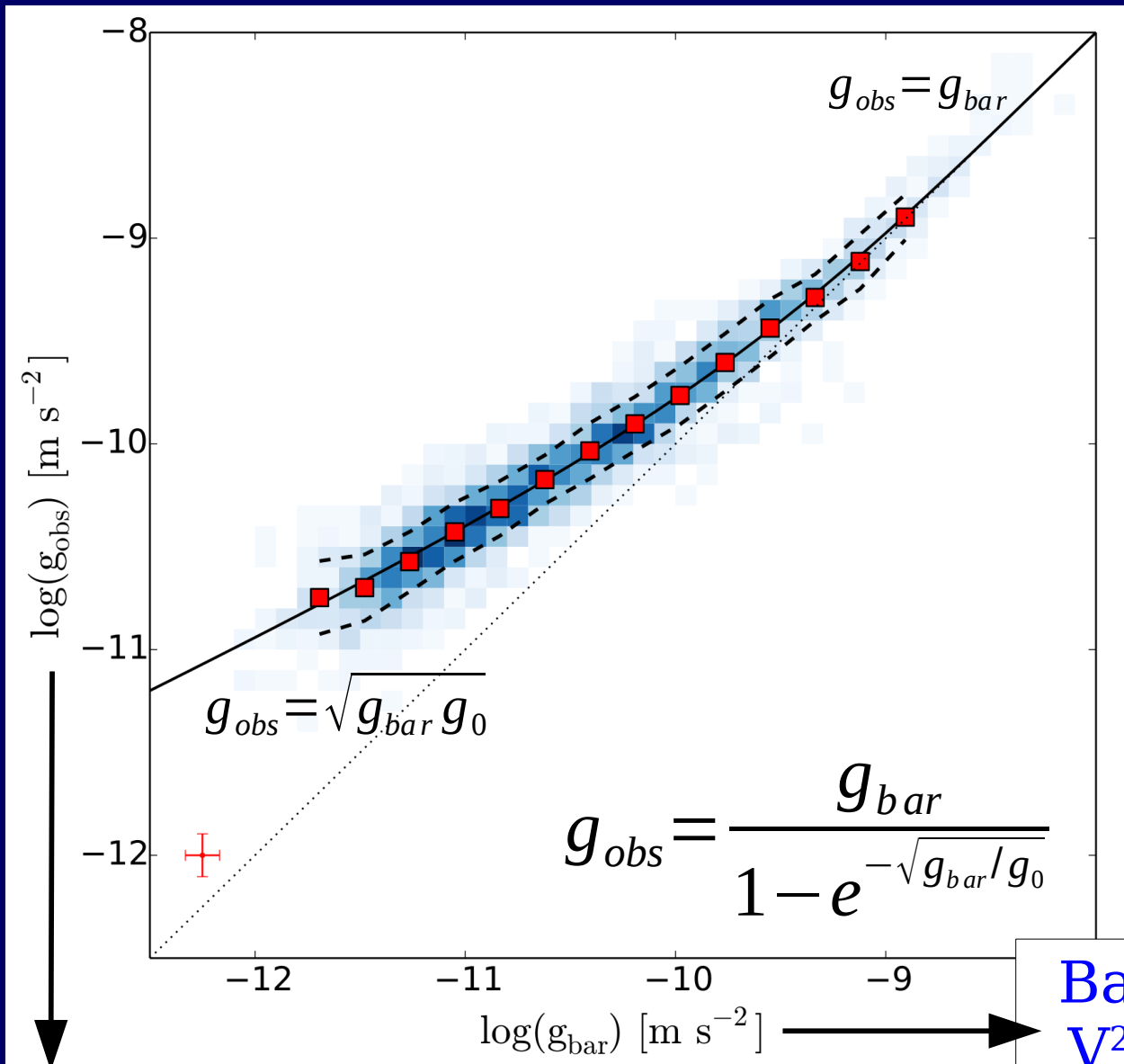
$$\Upsilon_{\text{disk}} = 0.5 M_{\odot}/L_{\odot}$$

$$\Upsilon_{\text{bulge}} = 0.7 M_{\odot}/L_{\odot}$$

Total Acceleration: $V_{\text{obs}}^2 / R = -\nabla\Phi_{\text{tot}}$

Baryonic Force:
 $V_{\text{bar}}^2 / R = -\nabla\Phi_{\text{bar}}$
 $\nabla^2\Phi_{\text{bar}} = 4\pi G \rho_{\text{bar}}$

Local link between baryons and DM



For all galaxies:

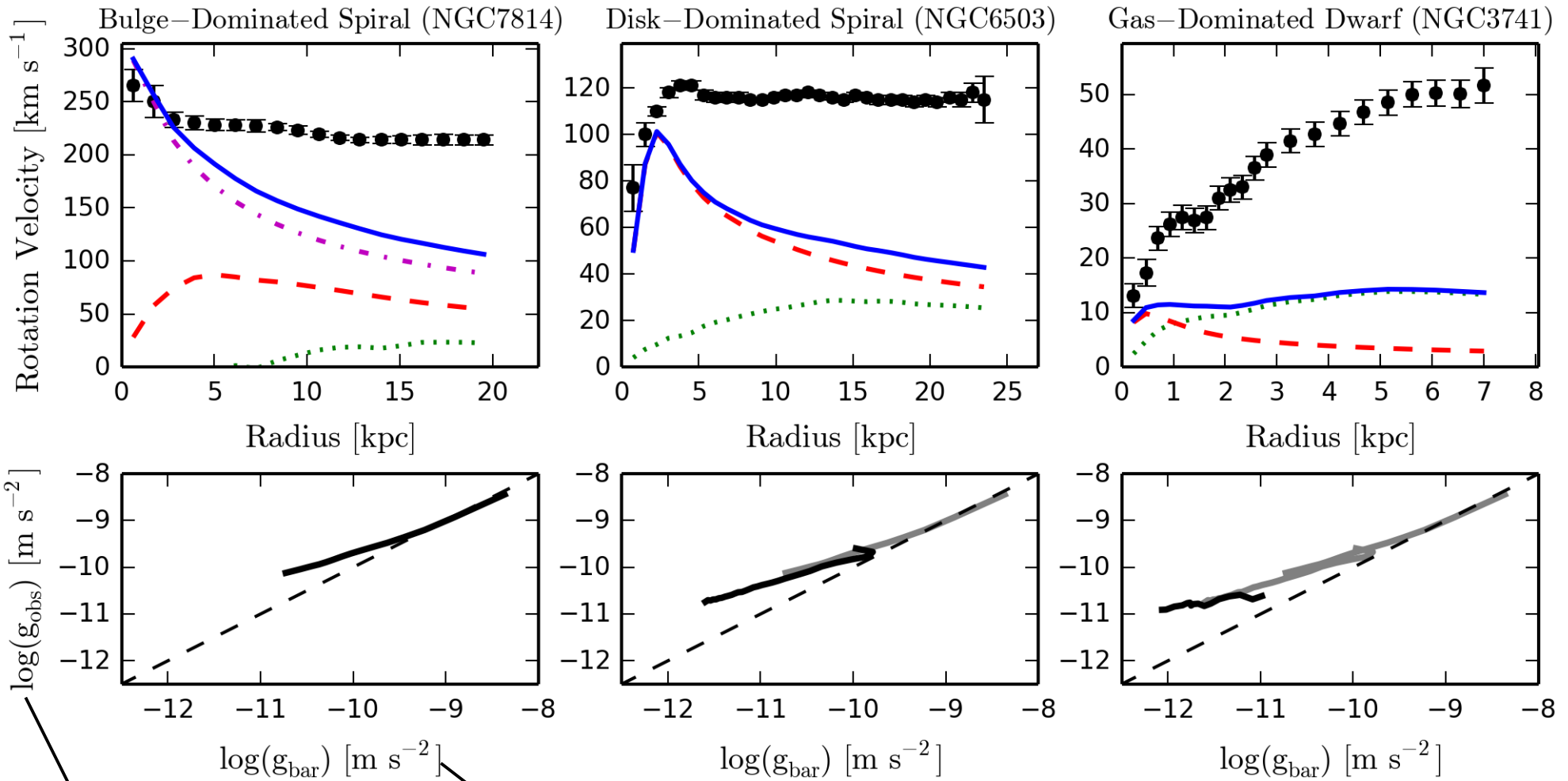
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Very different galaxies but ONE relation



$$V_{\text{obs}}^2 / R = -\nabla\Phi_{\text{tot}}$$

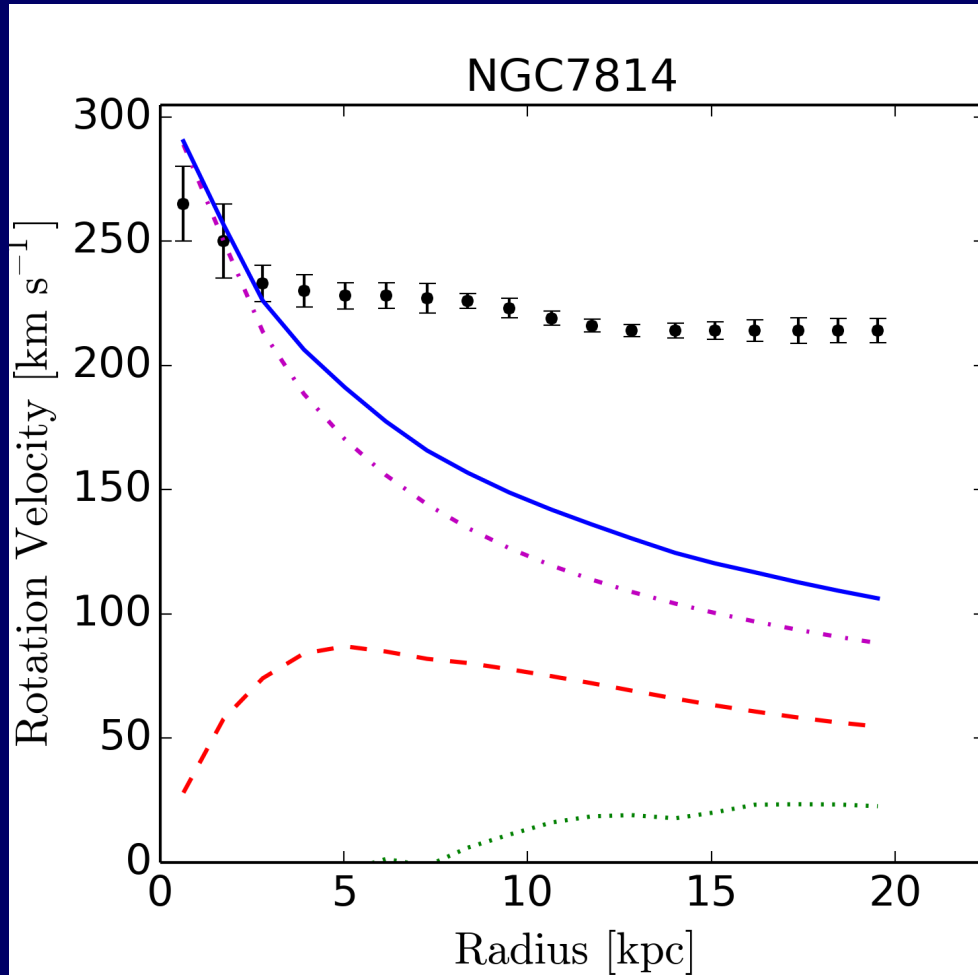
$$V_{\text{bar}}^2 / R = -\nabla\Phi_{\text{bar}}$$

$$\nabla^2\Phi_{\text{bar}} = 4\pi G \rho_{\text{bar}}$$

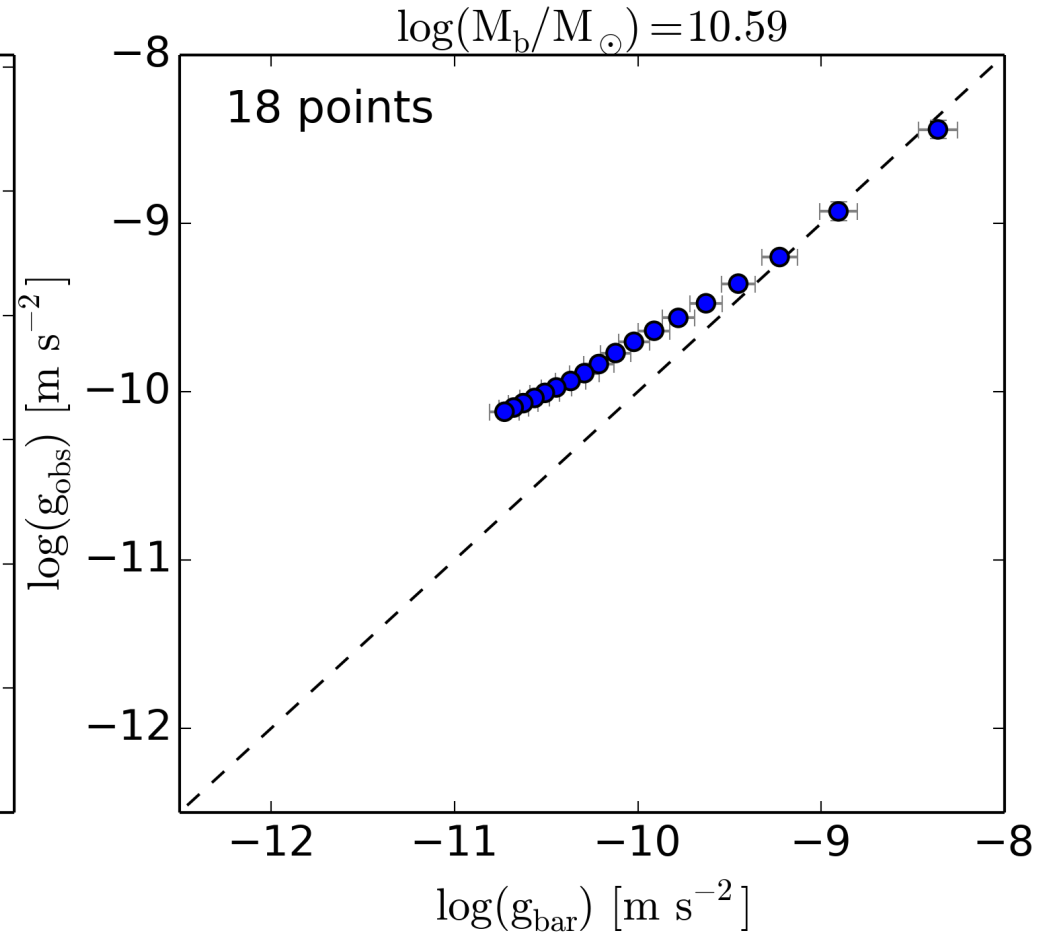
McGaugh, Lelli, Schombert (2016)

Building up the Radial Acceleration Relation

Large Diversity in Rotation Curves



Regularity in Acceleration Plane



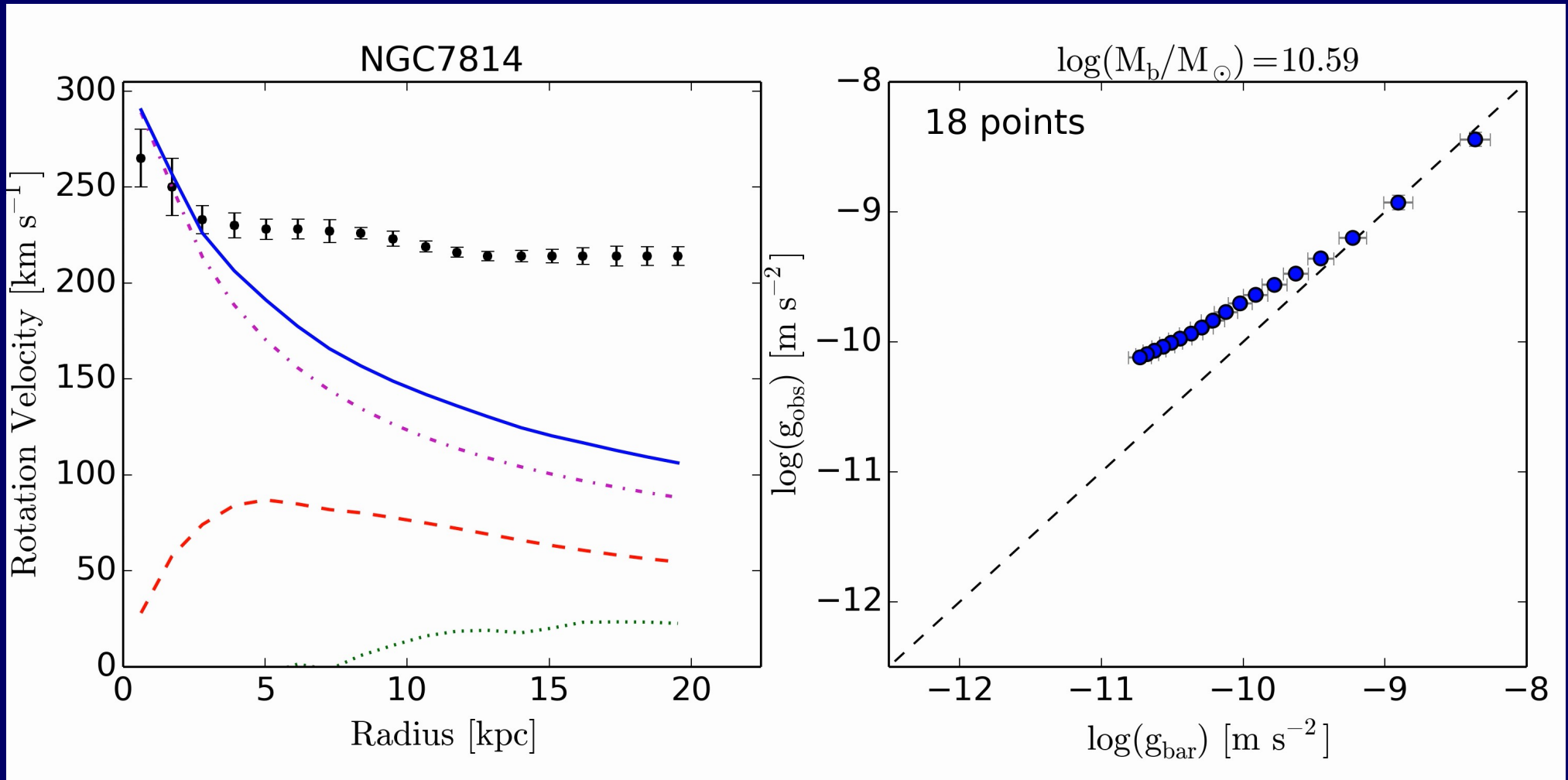
Lelli, McGaugh, Schombert, Pawlowski 2017, ApJ

Video available at astroweb.cwru.edu/SPARC/

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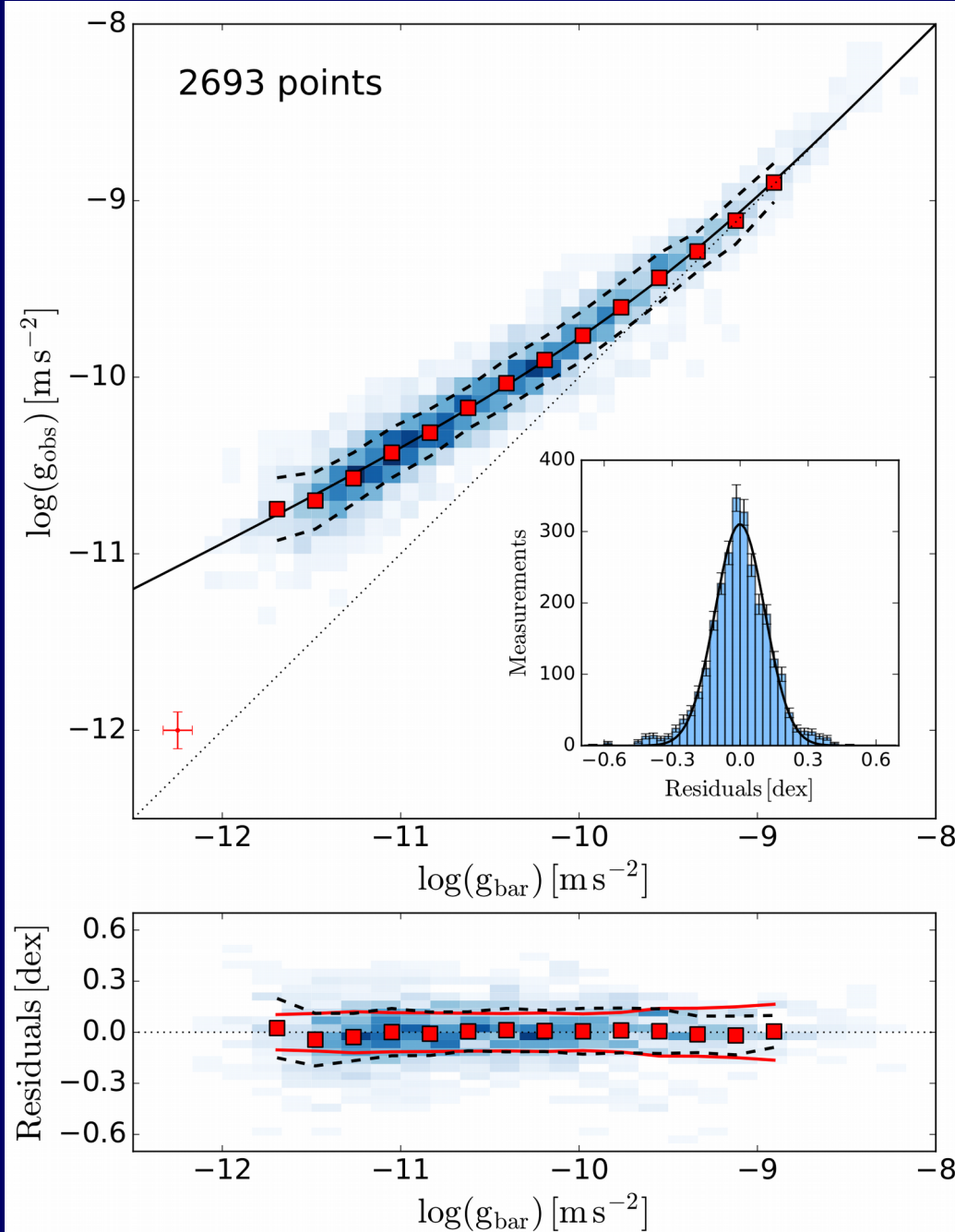
Regularity in Acceleration Plane



Lelli, McGaugh, Schombert, Pawlowski 2017, ApJ

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Is There Any Intrinsic Scatter?



Uncertainties drive scatter!

$\text{err}(g_{\text{bar}}) \rightarrow \Upsilon_*$, 3D geometry

$\text{err}(g_{\text{obs}}) \rightarrow \text{Dist, Inc, } V_{\text{rot}}$

$$\sigma_{\text{obs}}^2 = \sigma_{\text{err}}^2 + \sigma_{\text{int}}^2$$

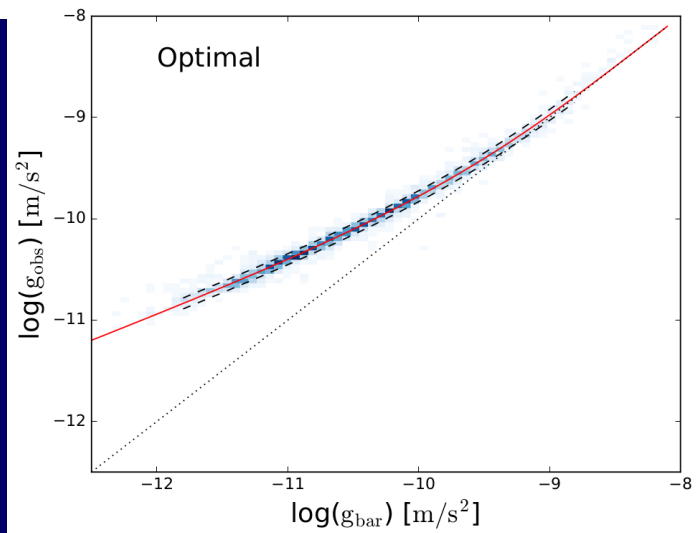
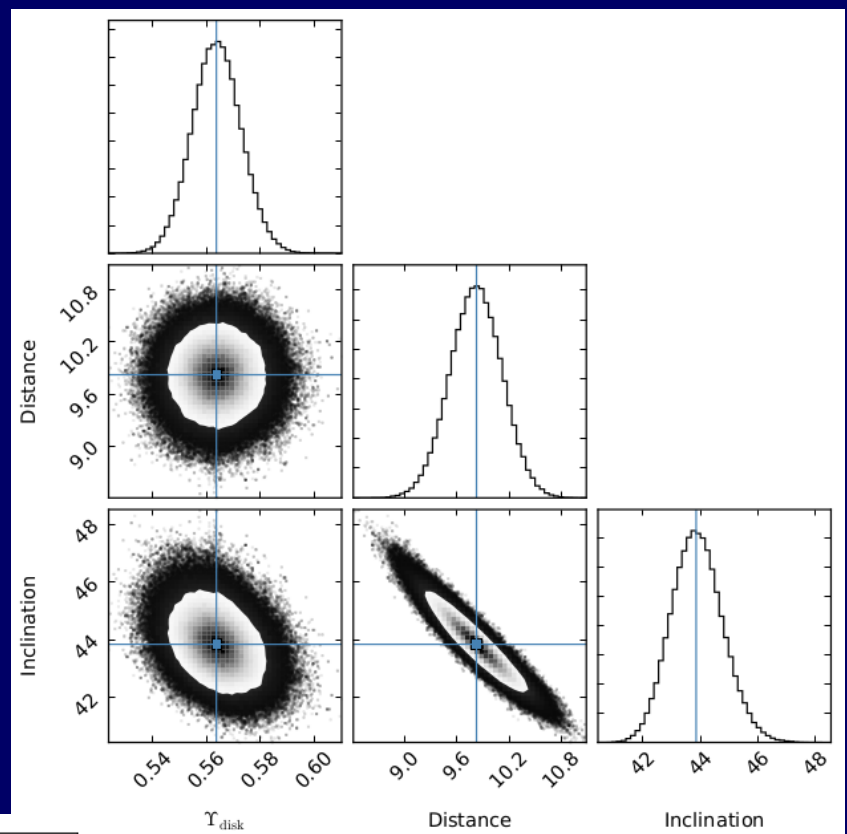
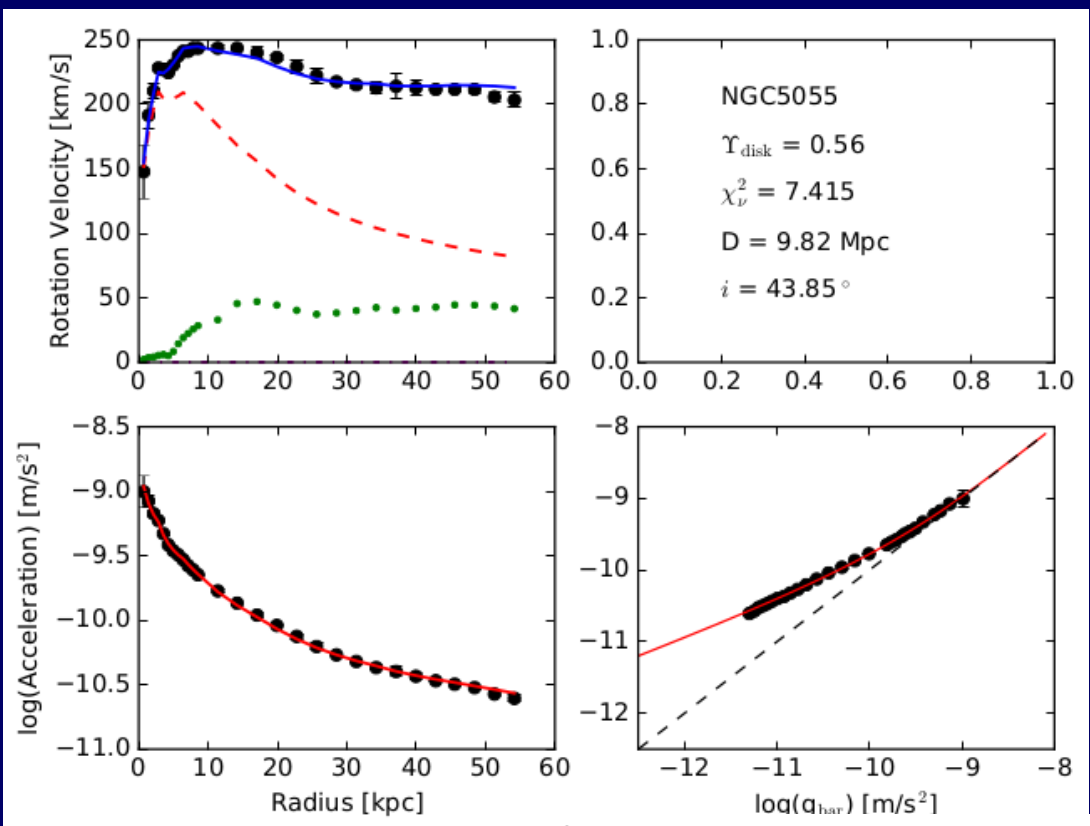
$\sigma_{\text{obs}} \rightarrow$ measured rms

$\sigma_{\text{err}} \rightarrow$ error propagation

$\sigma_{\text{int}} \rightarrow$ consistent with zero!

McGaugh+2016, PRL; Lelli+2017, ApJ

MCMC Fits to Individual Galaxies



Extremely tight relation!

$$\sigma_{\text{obs}} = 0.054 \text{ dex } (\sim 10\%)$$

$$\text{err}(V_{\text{rot}}) \sim 10\%$$

Pengfei Li et al. (submitted)

Three Laws of Galactic Rotation:

1. **Global Law:** $V_{\text{flat}} \propto M_{\text{bar}}$

2. **Central Law:** $\Sigma_{\text{dyn}}(0) \propto \Sigma_{\text{bar}}(0)$

3. **Local Law:** $g_{\text{obs}}(R) \propto g_{\text{bar}}(R)$

Only inputs are the Poisson Equation and the M_*/L .

Observed scatter is tiny. No residual correlations.

We can infer the DM distribution from g_{bar} !

From the observations: $g_{DM} = g_{tot} - g_{bar} = F(g_{bar})$

For a spherical DM halo: $M_{DM}(R) = \frac{R^2}{G} F(g_{bar})$

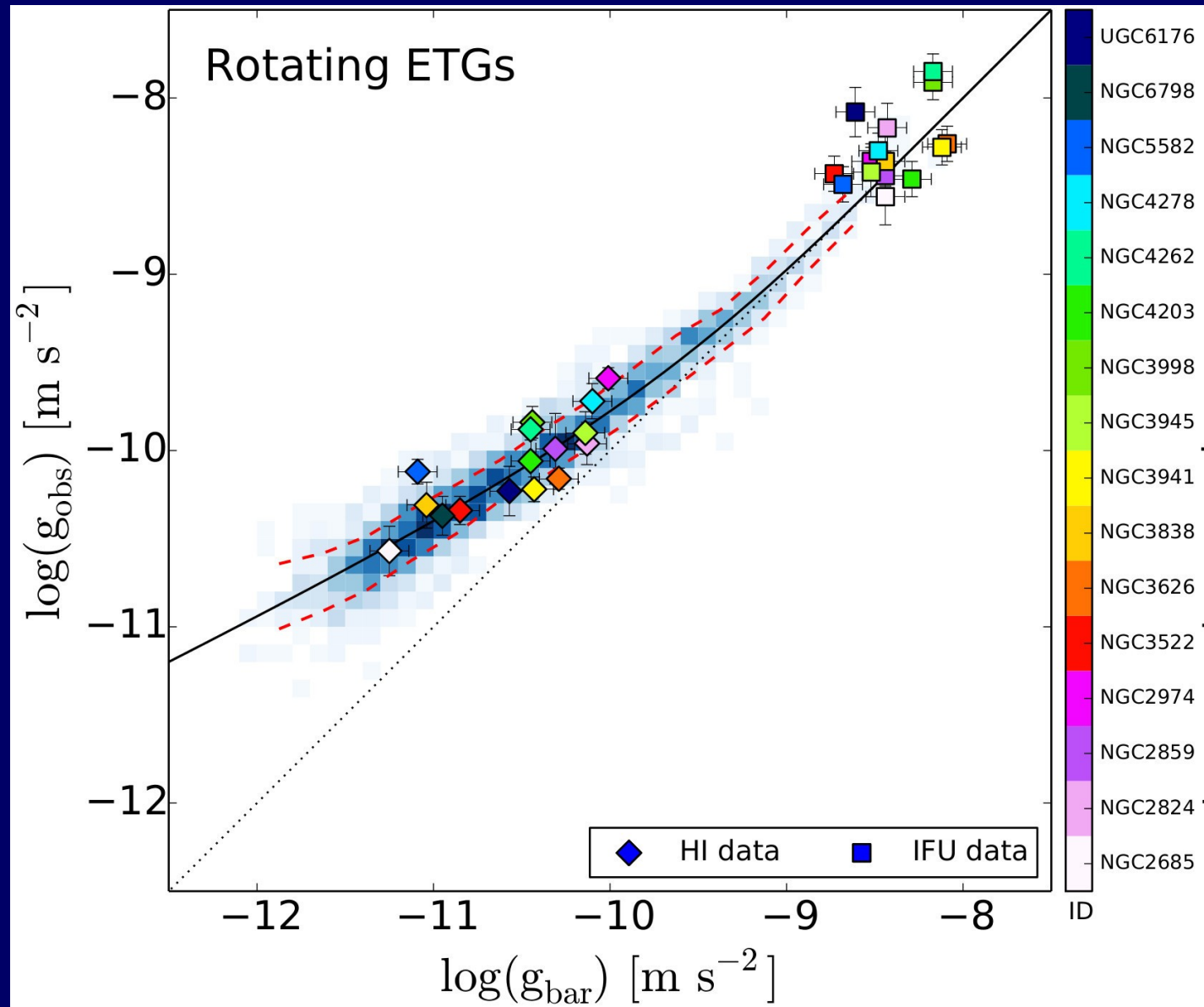
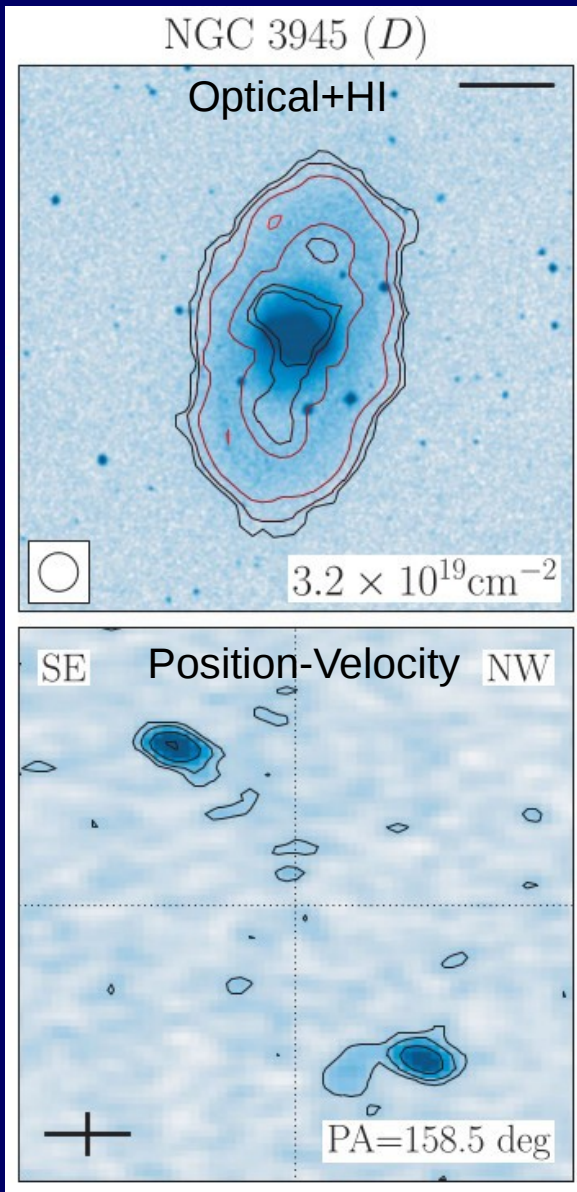
For our fiducial fitting F: $M_{DM}(R) = \frac{R^2}{G} \frac{g_{bar}}{\exp(\sqrt{g_{bar}/g_0}) - 1}$

Purely empirical relations (accuracy $\sim 30\%$).

3. Radial Acceleration Relation of Early-Type Galaxies

Lelli, McGaugh, Schombert, Pawlowski 2017, ApJ

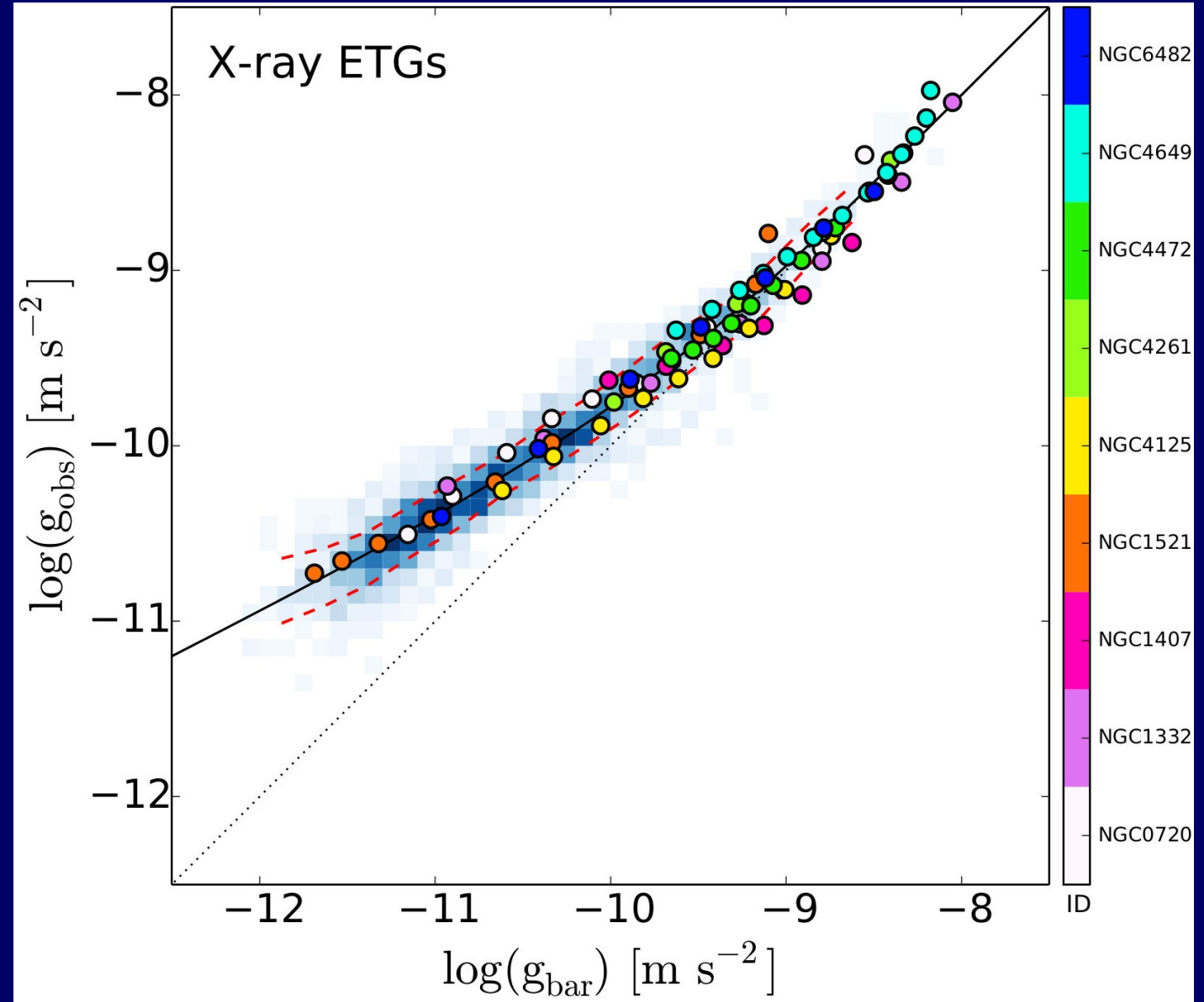
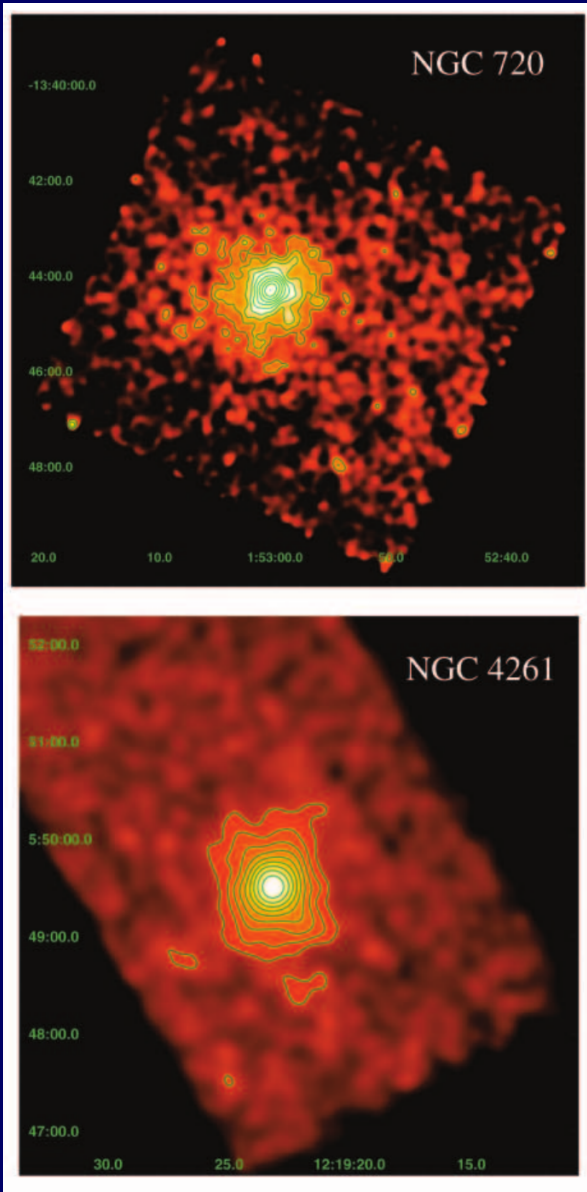
16 Rotating ETGs with outer HI rings/disks



ATLAS^{3D} project: Cappellari+2010; Serra+2012, 2016

Lelli+2017, ApJ

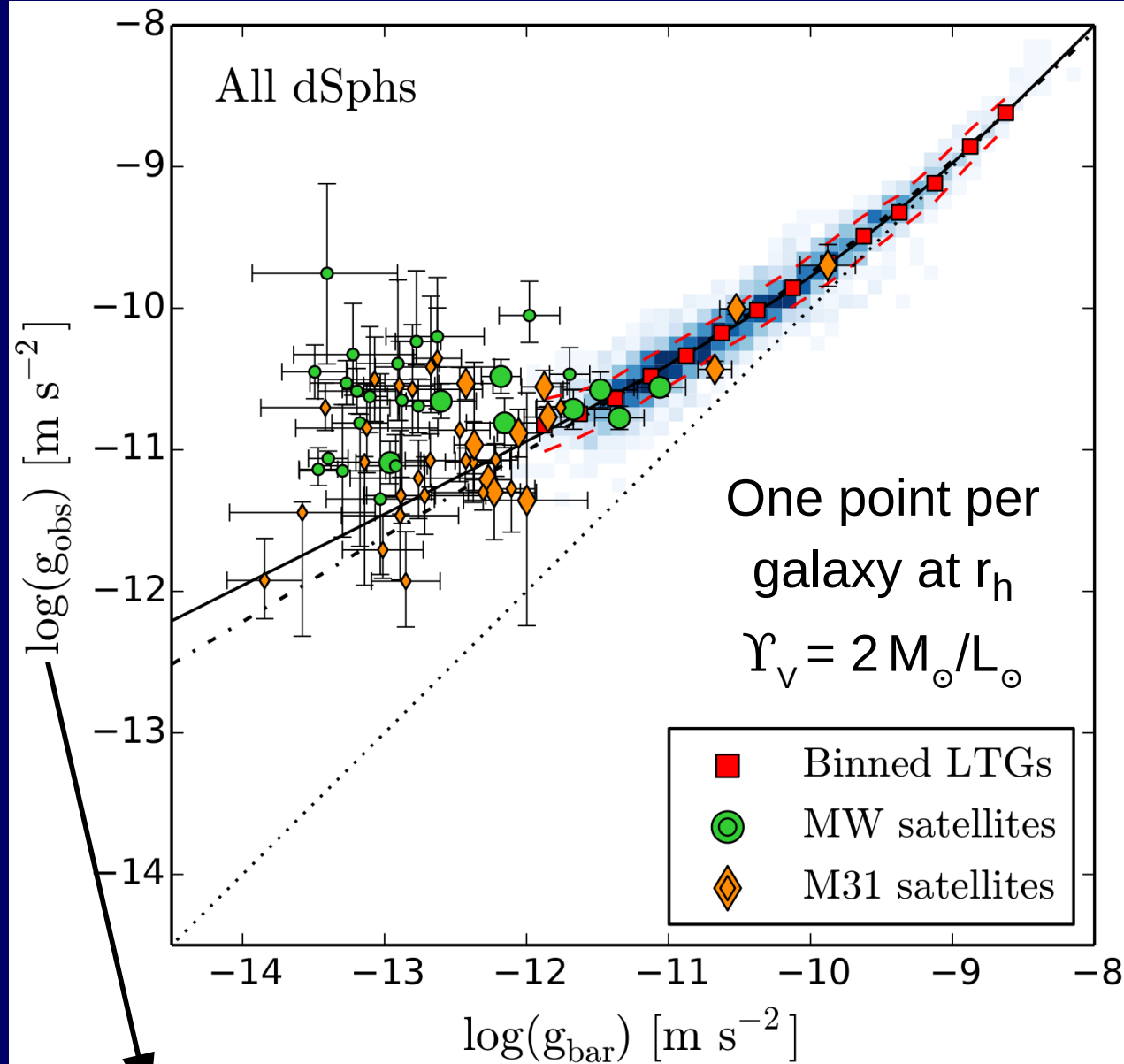
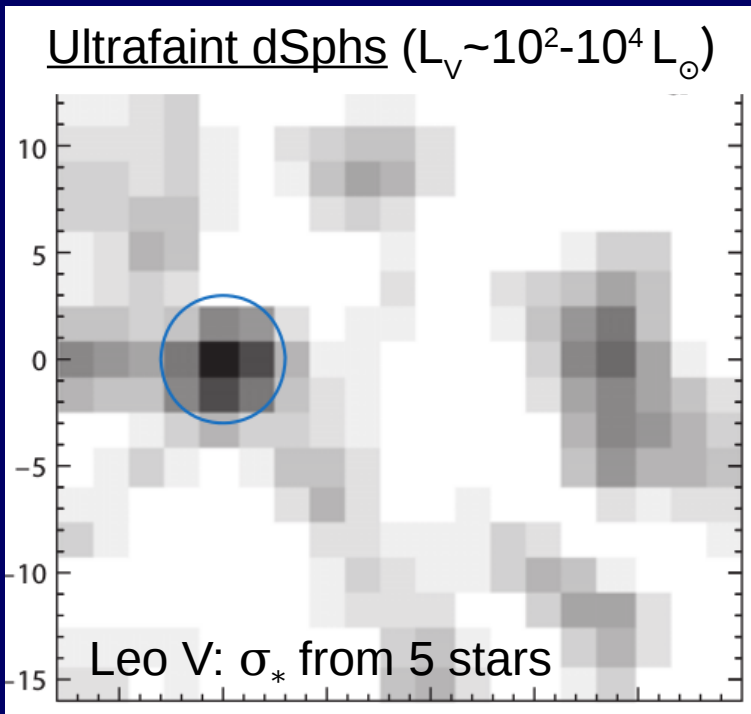
9 Non-Rotating ETGs with X-ray Halos



Humphrey+2006, 2008, 2009, 2011, 2012

Lelli+2017, ApJ

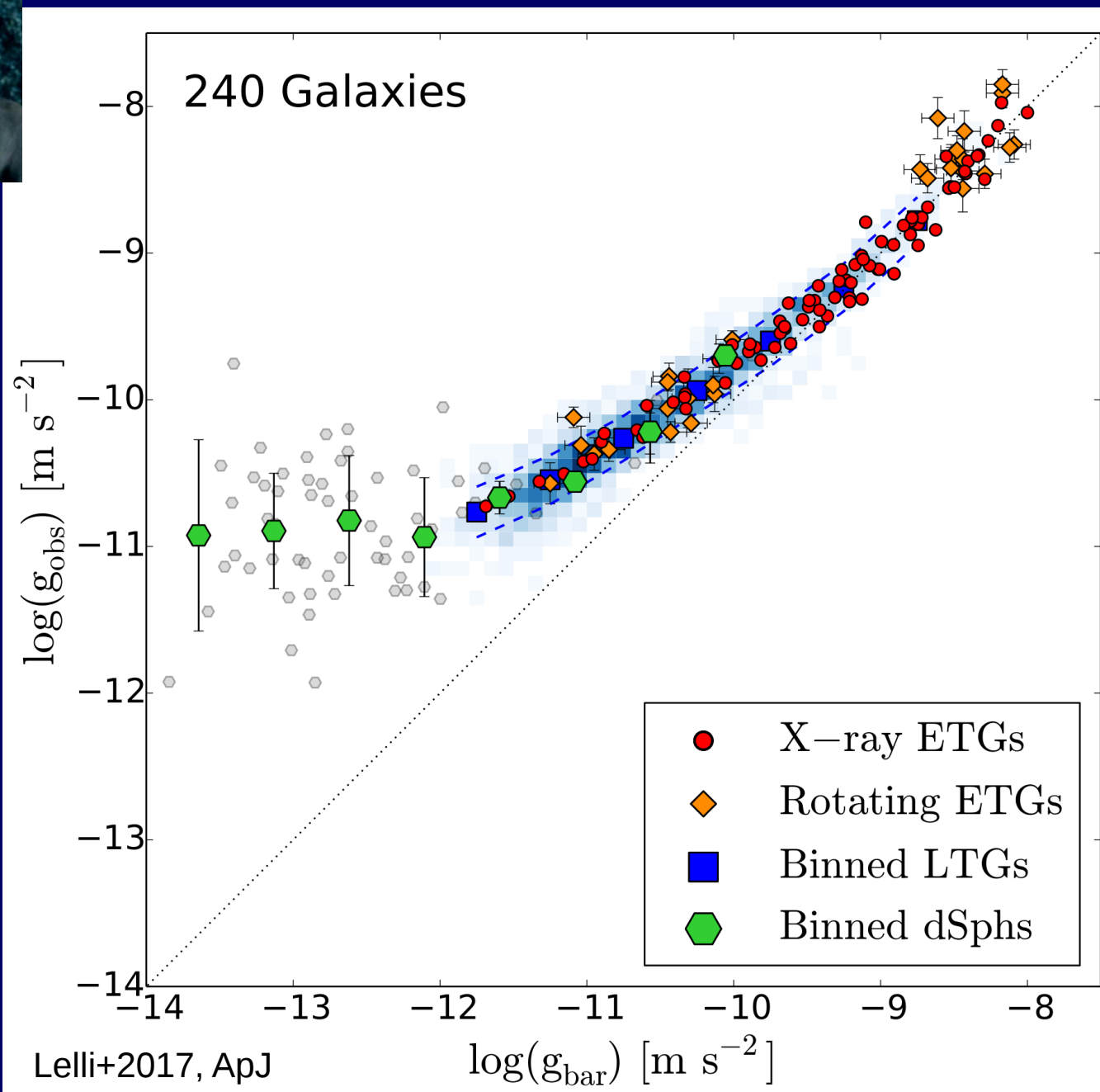
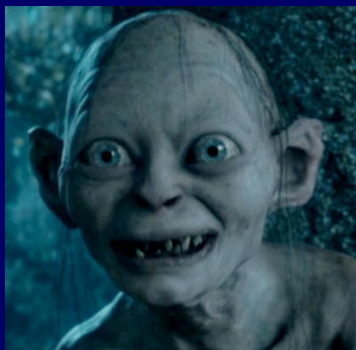
Dwarf Spheroidals in the Local Group



$$g_{\text{obs}} = 3\sigma_*^2 / r_h$$

$$g_{\text{bar}} = GM_{\text{bar}} / r_h^2$$

One Law to Rule Them All!



Possible Interpretations:

1. End product of galaxy formation in Λ CDM
2. New Dynamical Laws (Milgromian Dynamics)
3. New Physics in the Dark Sector / Dark Forces

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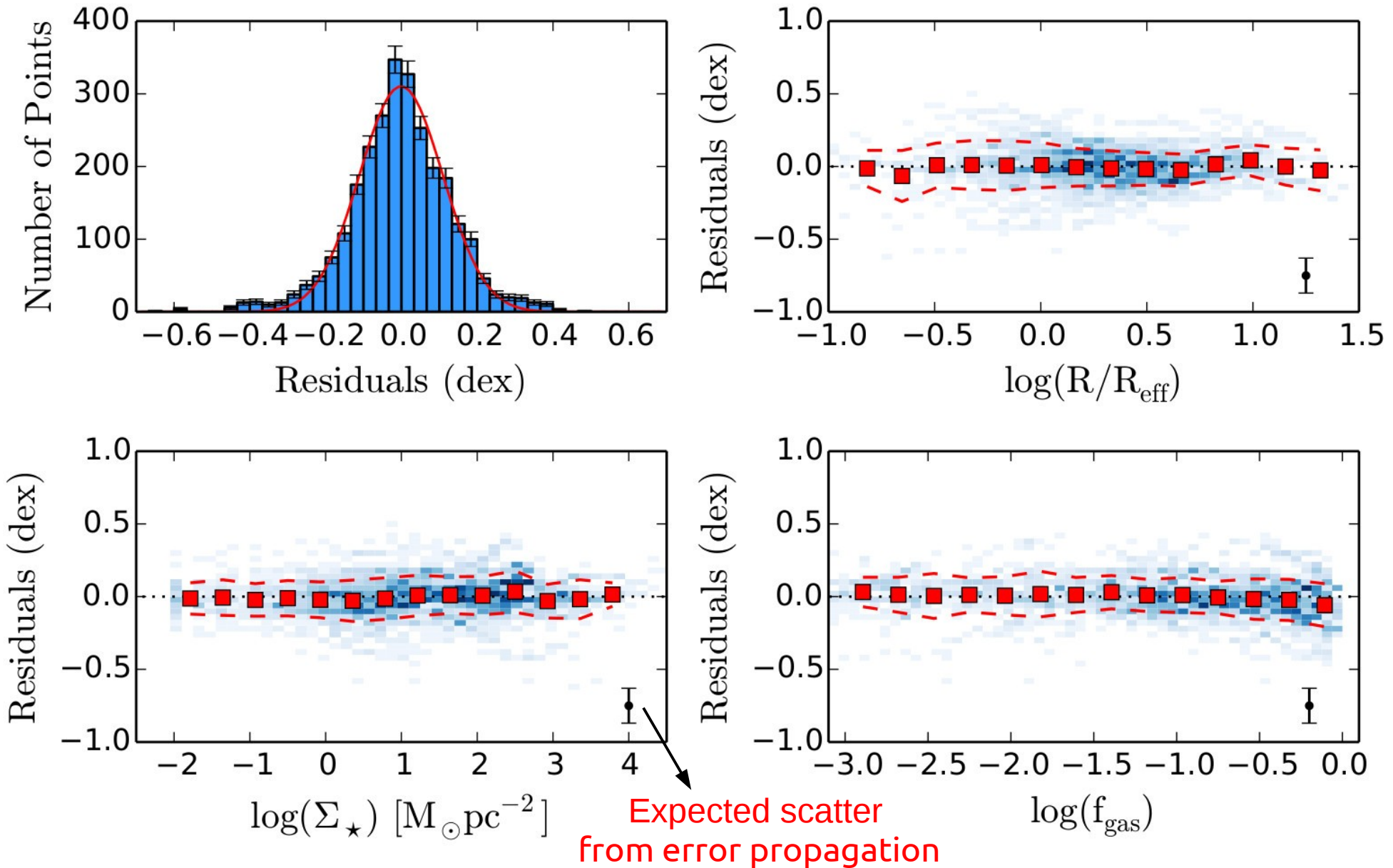
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Good: Hybrids Λ CDM + MOND (Dark Fluids: Zhao & Li 2010; Khoury 2015)

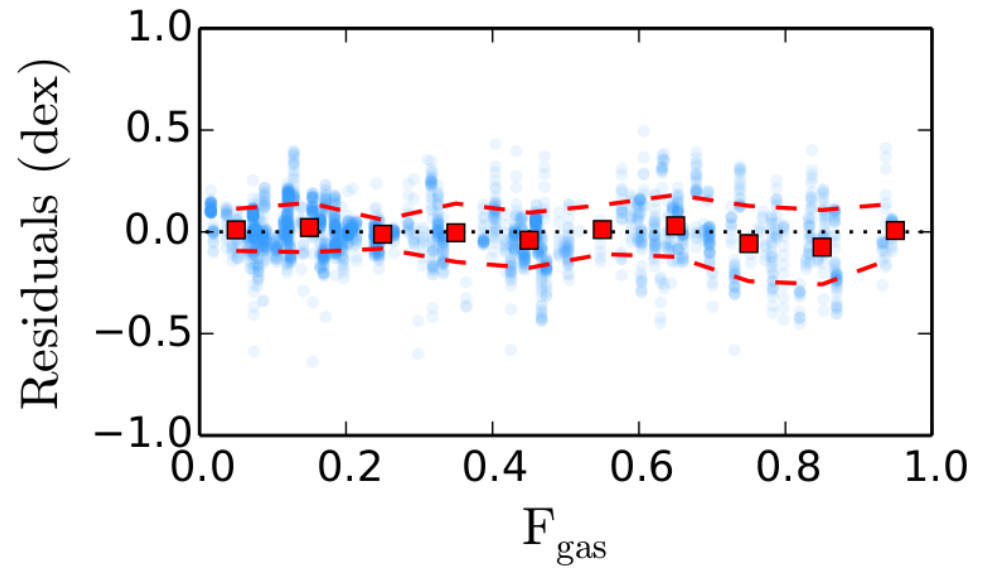
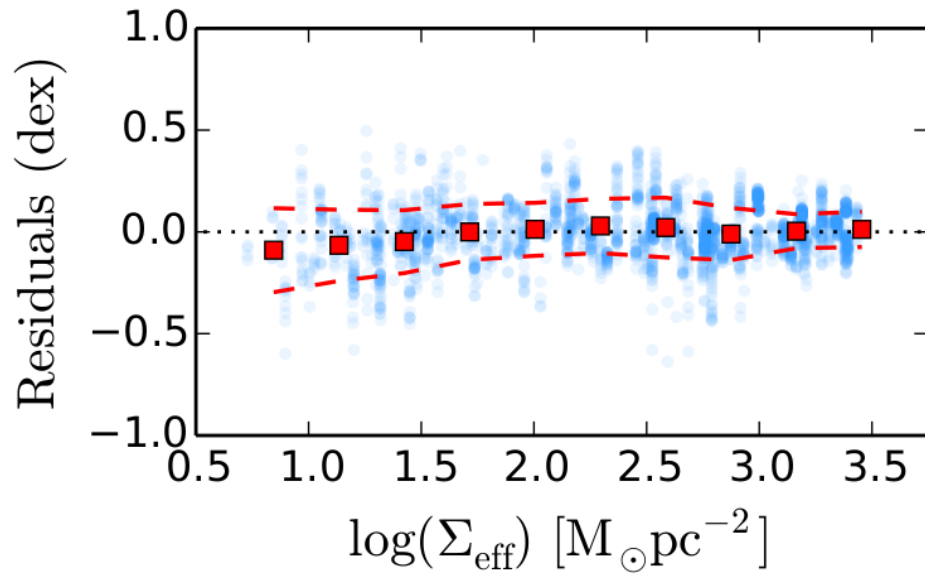
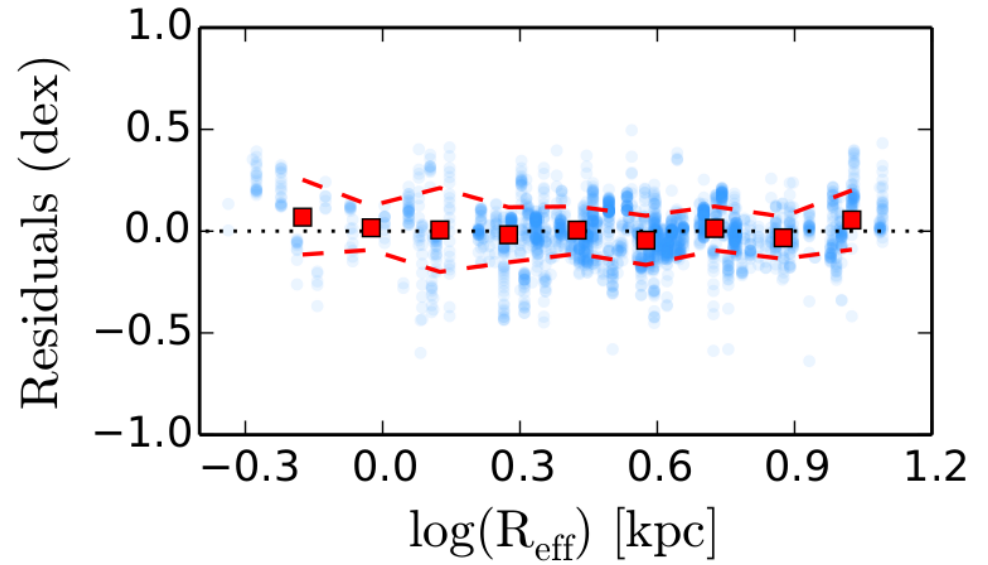
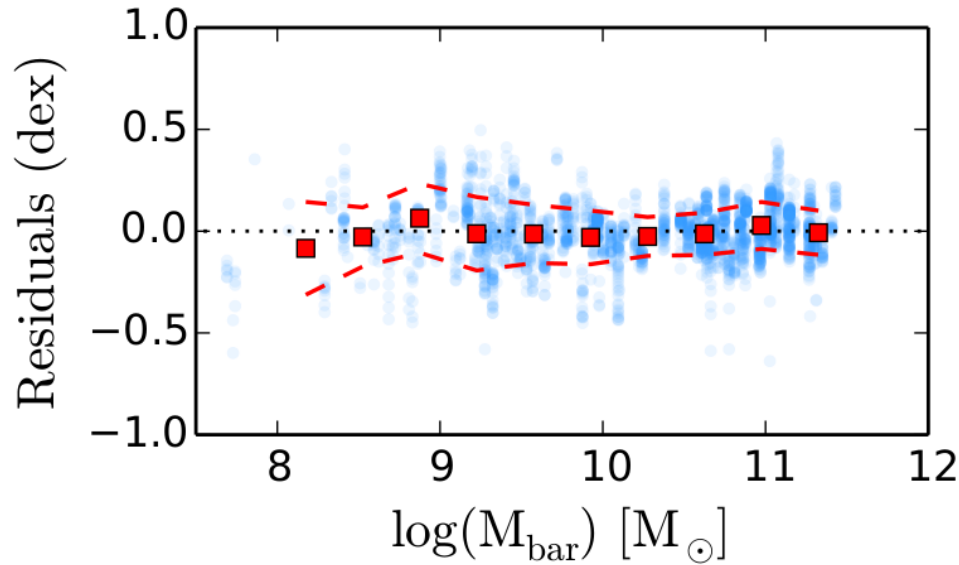
Bad: 'Good' is good by construction. New predictions?

Additional Slides

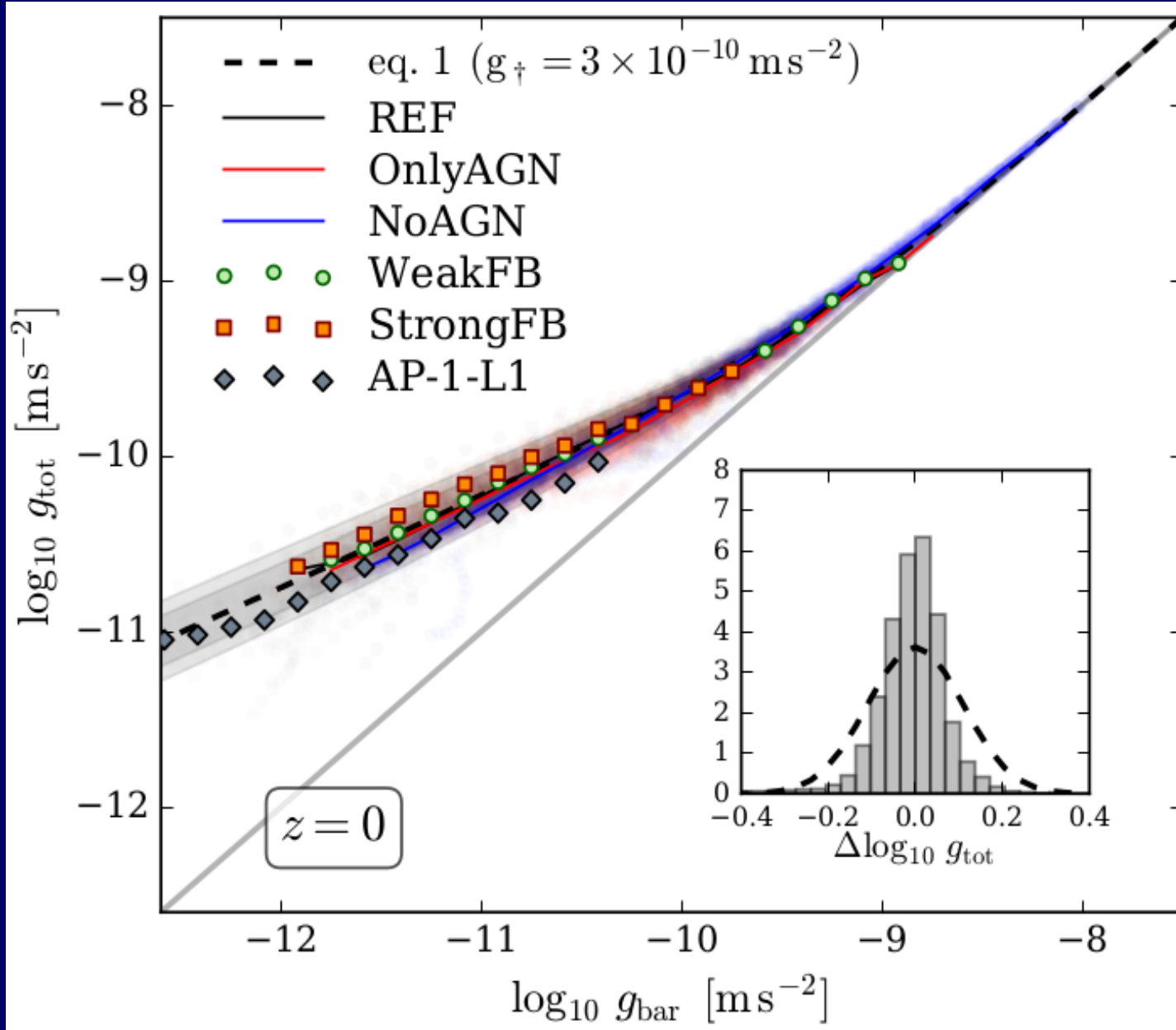
Residuals vs Local Galaxy Properties



Residuals vs Global Galaxy Properties



RAR from Hydrodynamical Simulations



A similar relation is found but the **real problem** is the **TIGHTNESS!**

$$\sigma_{\text{obs}}^2 = \sigma_{\text{int}}^2 + \sigma_{\text{err}}^2$$

Can't forget errors!

Analytic Models:

[Di Cintio & Lelli 2016](#)

[Navarro+2016](#)

[Desmond 2017](#)

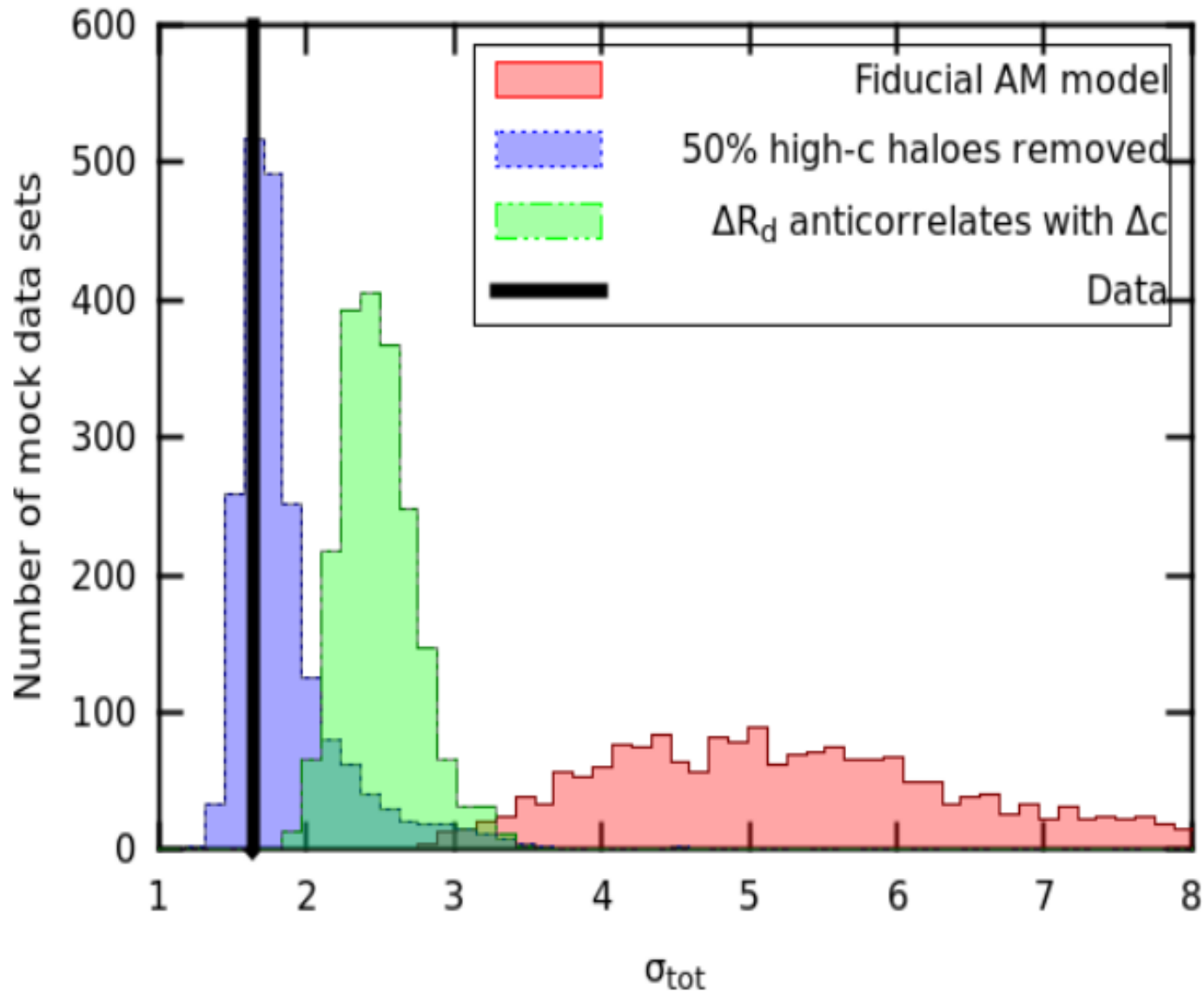
Numerical Sims:

[Keller & Wadsley 2016](#)

[Ludlow+2017](#)

[Tenneti+2017](#)

RAR Scatter from Semi-Empirical Models

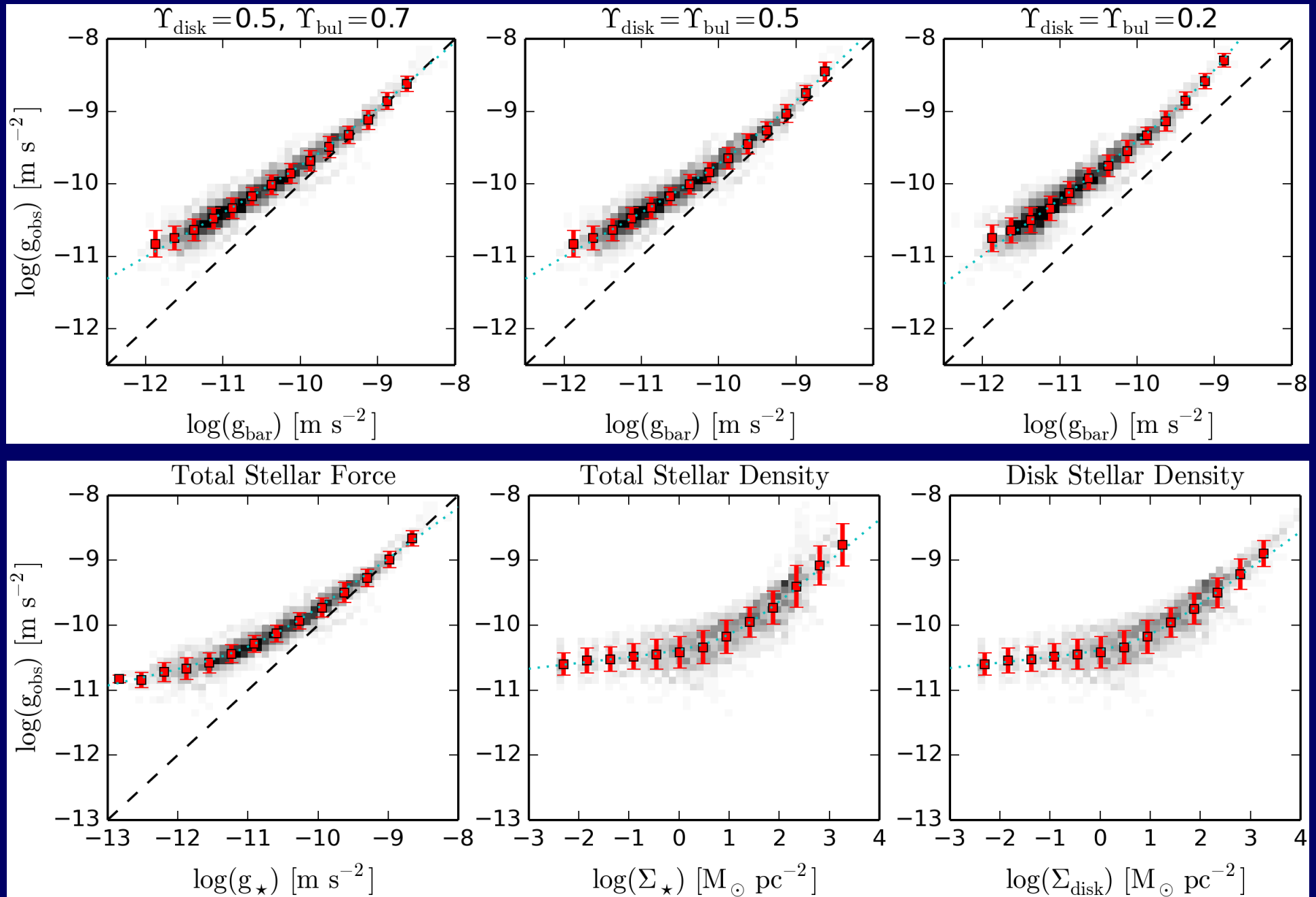


Each SPARC galaxy is associated to a DM halo by matching relative abundances (see also DiCintio & Lelli).

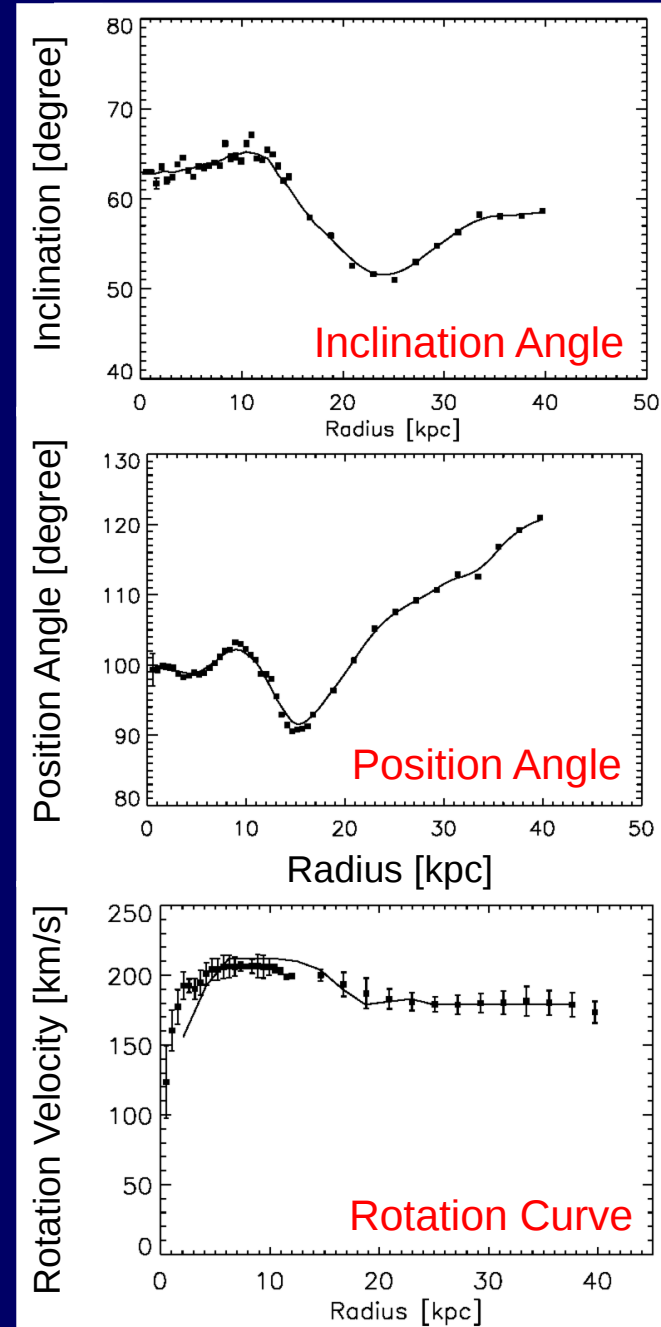
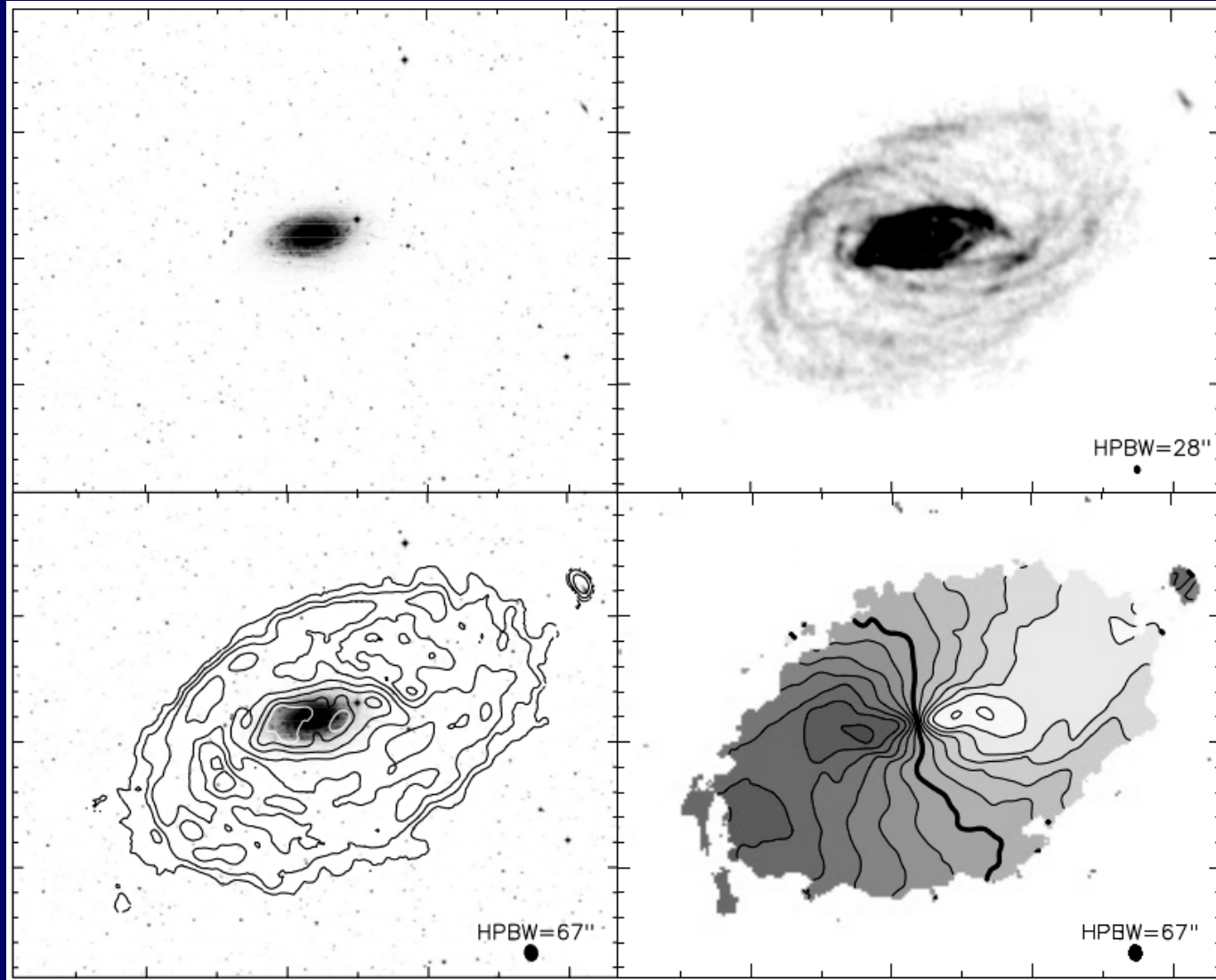
Multiple realizations taking into account **sample variance** and **observational errors**.

Fiducial model **over-predicts** the observed scatter!

Alternative versions of the RAR

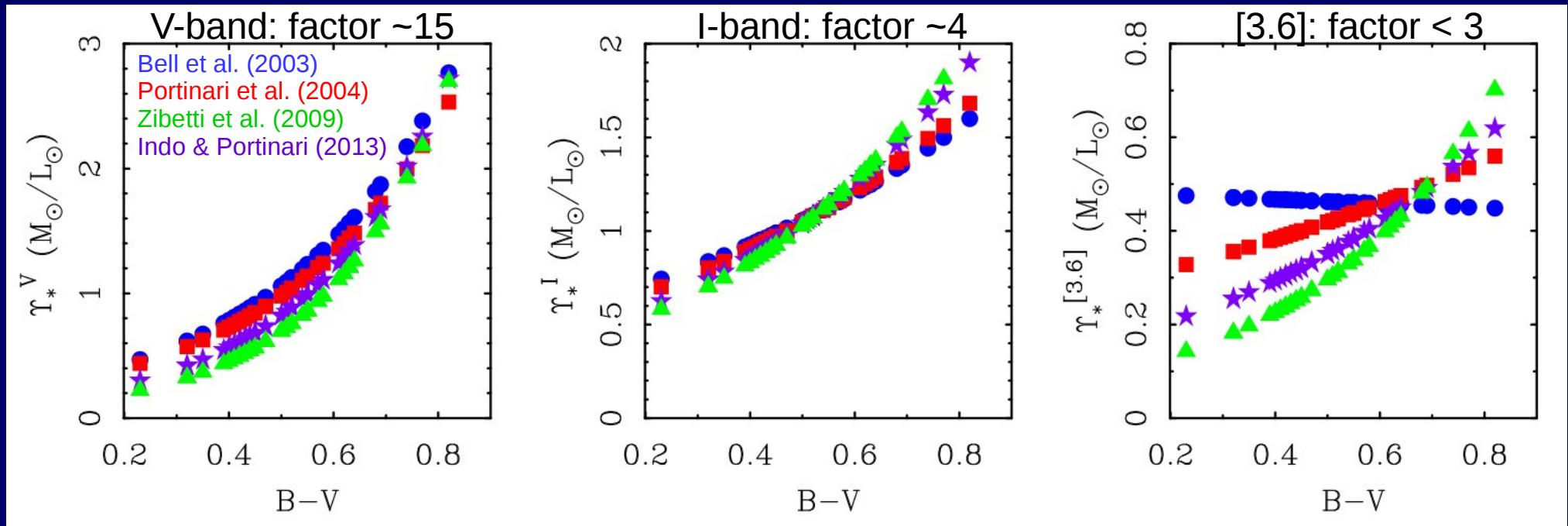


HI observations: Rotation Curves



$$V_{\text{l.o.s.}} = V_{\text{sys}} + V_{\text{rot}} \sin(i) \cos(\theta)$$
$$\cos(\theta) = \text{func}(x_0, y_0, \text{PA})$$

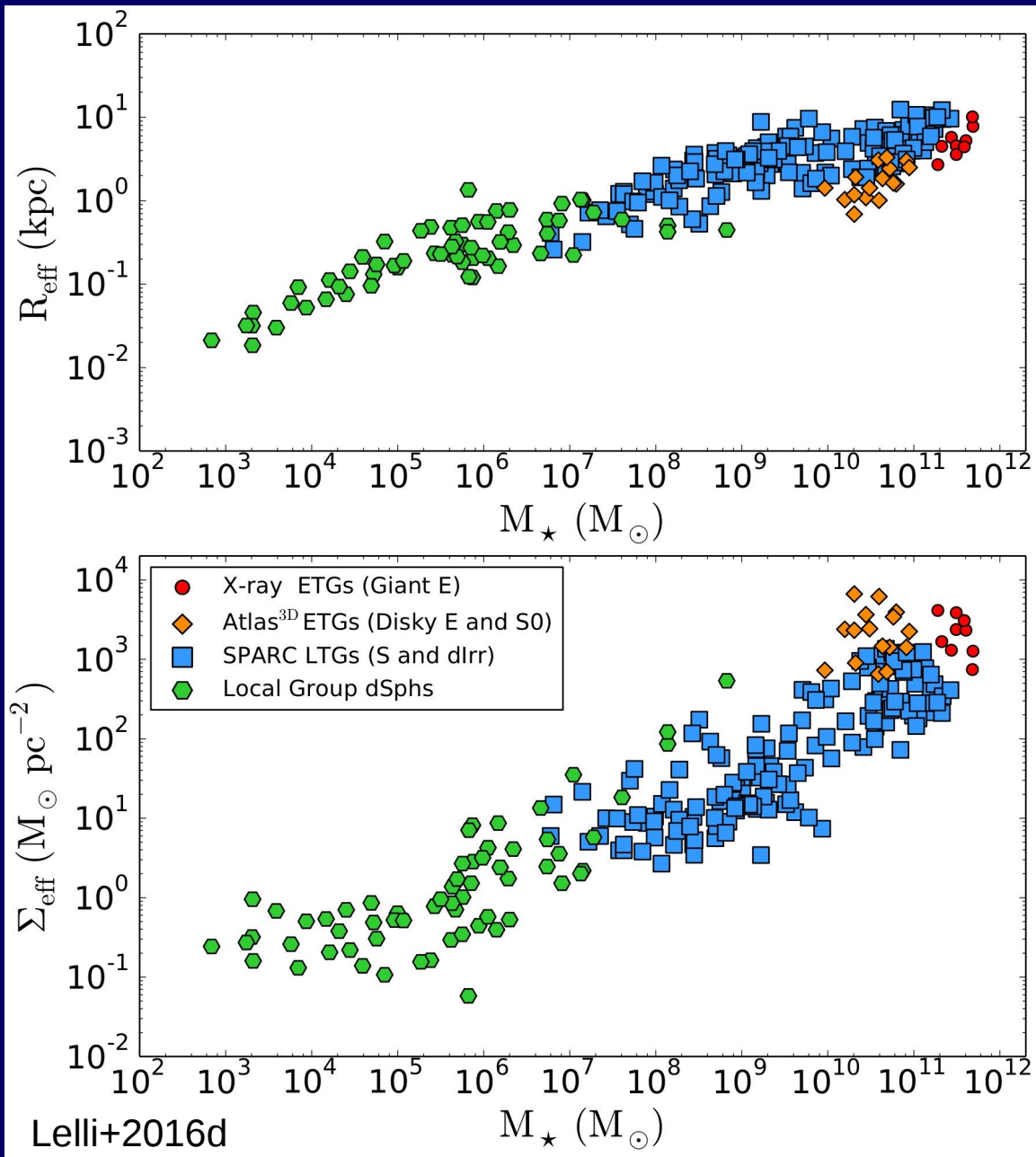
Spitzer [3.6] Photometry: Stellar Mass



Υ_* -color relations from SPS models (McGaugh & Schombert 2014)

- Υ_* shows smaller variations at [3.6] than optical bands
- Details depend on SPS model and assumed IMF
- Most recent models: $\Upsilon_{[3.6]}$ is nearly constant for LTGs (Meidt+2014; Schombert & McGaugh 2014; Norris+2016)

Dwarf Spheroidals (dSphs) in the Local Group



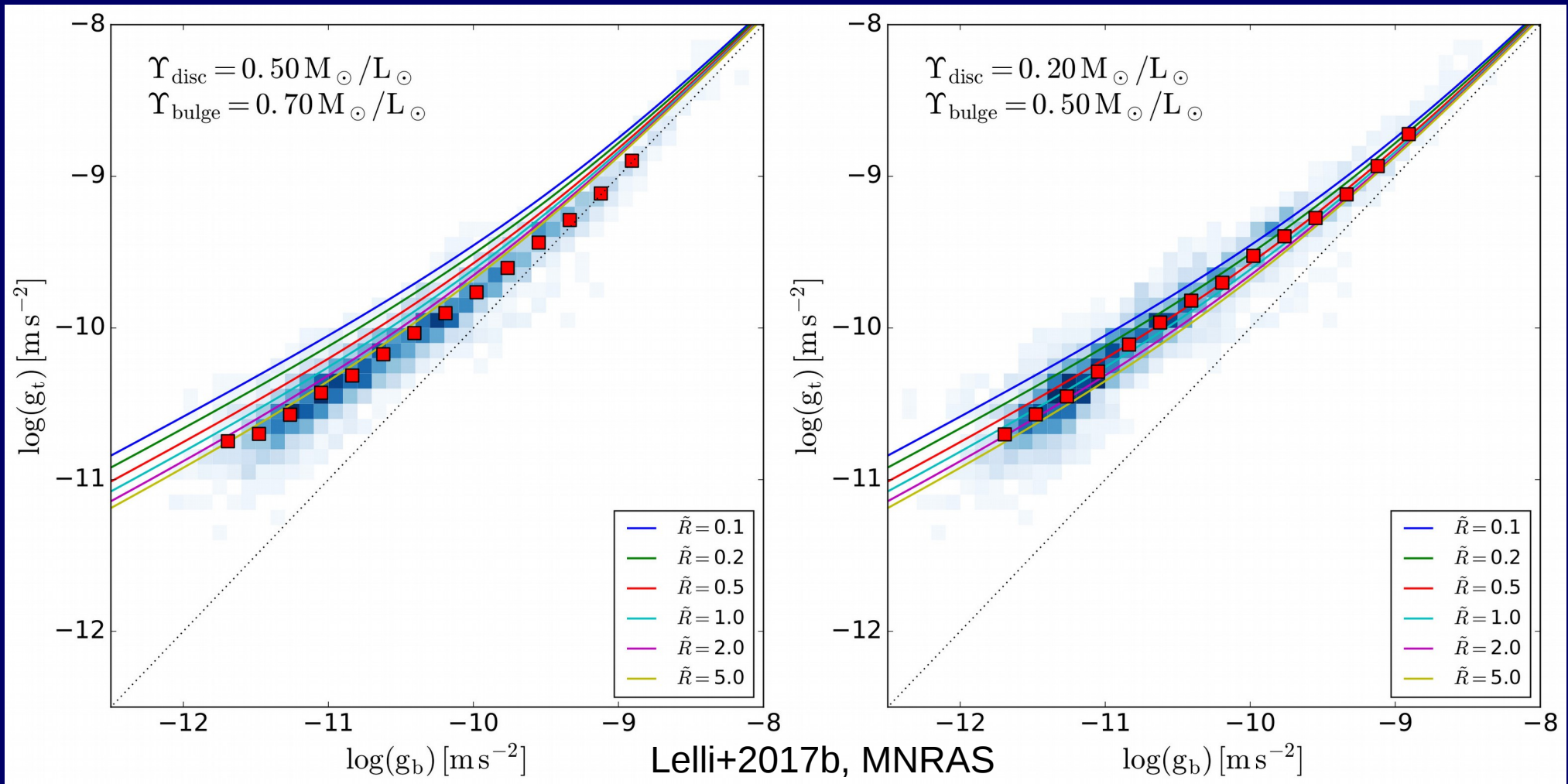
Satellites of MW and M31:
extremely low masses, sizes,
densities, and accelerations!

"Classical" dSphs discovered
between the '40 and the '80.

→ well-studied properties

"Ultrafaint" dSphs discovered
during the past ~10 years with
SDSS, DES and other surveys
→ properties remain uncertain

RAR vs Verlinde's Emergent Gravity



- EG implies:
- (1) low M/L on average
 - (2) some intrinsic scatter
 - (3) residual correlations with radius