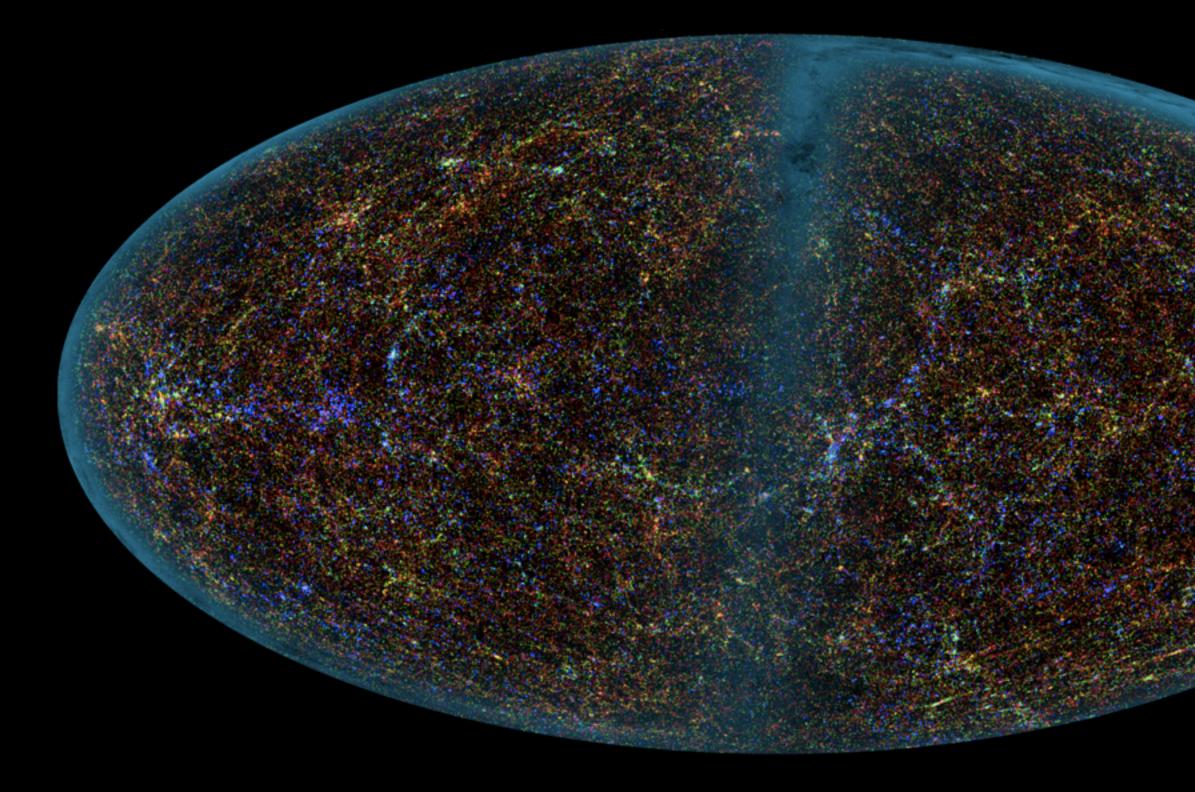
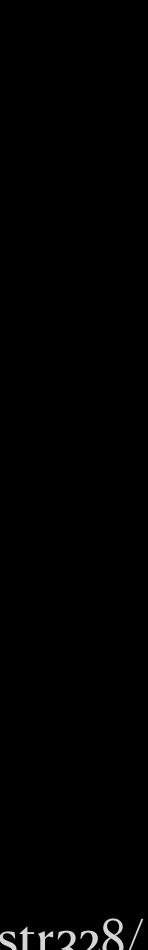
## **Cosmology** and Large Scale Structure



26 August 2020

### <u>Today</u> Hubble Expansion





The Stability Problem - gravity wants to collapse everything into a black hole

### Bentley-Newton correspondence

Bentley: would not a finite assemblage of stars collapse from their mutual gravity? Newton: if the matter was evenly diffused through an infinite space, it would never convene into one mass.

**Bentley:** can such a system remain stable?

Newton: such an assemblage, even if infinite, is like an array of needles standing upright on their points, ready to fall one way or another.

Newton: this frame of things could not always subsist without divine power to conserve it.

Exchange of letters in 1693, long after the apple dropped (1664).

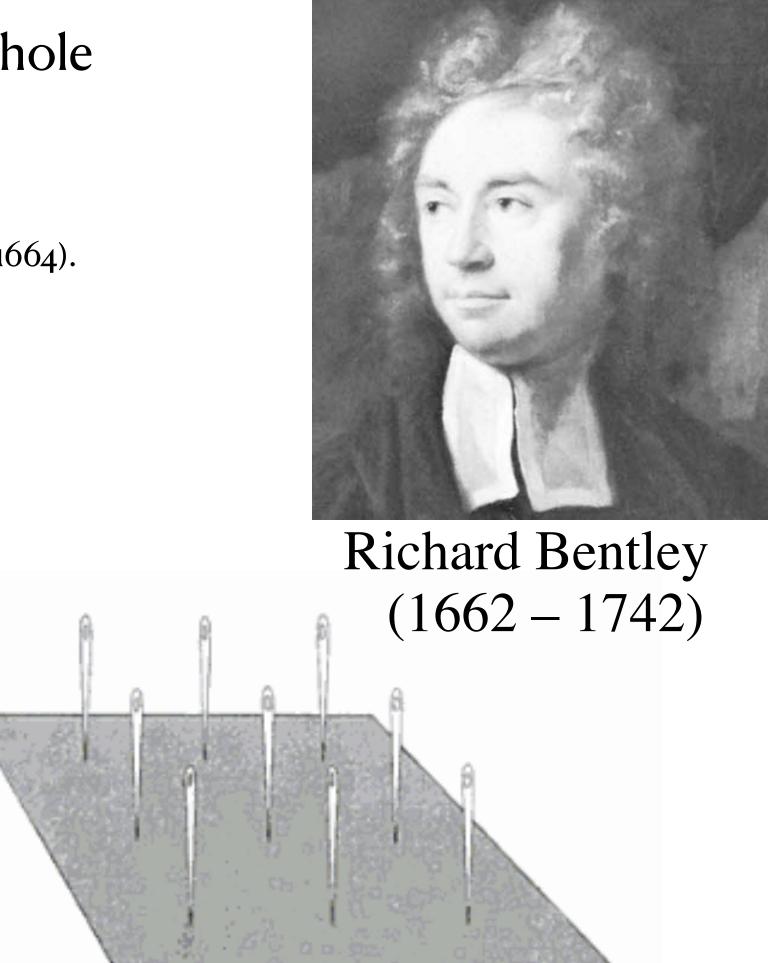
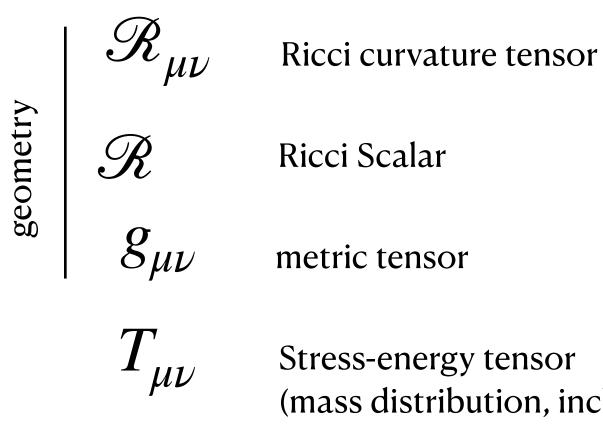


Figure 3.12. Newton agreed with Bentley that stars cannot form a finite and bounded system (as in the Stoic cosmos), for they would fall into the middle of such a system by reason of their gravitational attraction. They agreed that matter was uniformly distributed throughout infinite space, and realized that this was an unstable distribution. The particles of matter, wrote Newton, are like an array of needles standing upright on their points ready to fall one way or another, and "thus might the Sun and fixed stars be formed."



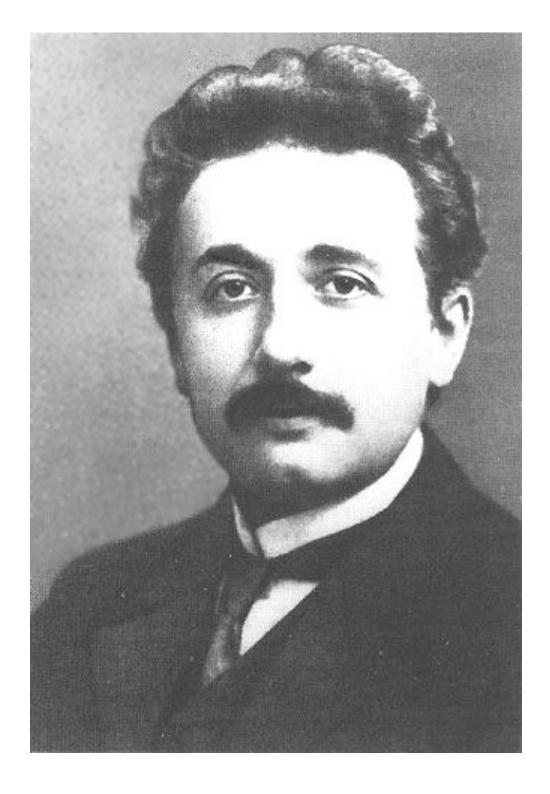
## Einstein's Equation

 $\mathcal{R}_{\mu\nu} - \frac{1}{2}\mathcal{R}g_{\mu\nu} = \frac{8\pi G}{c^4}T_{\mu\nu}$ 



 $\mu\nu$  are indices of space-time (t, x, y, z)

(mass distribution, including energy, via  $E = mc^2$ )



"Mass tells space-time how to curve, and space-time tells mass how to move." - John Wheeler

## The Expanding Universe

 $\mathcal{R}_{\mu\nu} - \frac{1}{2}\mathcal{R}g_{\mu\nu} = \frac{8\pi G}{c^4}T_{\mu\nu}$ 

Space-time is dynamic. A universe evolving according to Einstein's field equation must either expand or contract. It can not be static.

So, he fudged it.

 $\mathcal{R}_{\mu\nu} - \frac{1}{2}\mathcal{R}g_{\mu\nu} = \frac{8\pi G}{c^4}T_{\mu\nu} + \Lambda g_{\mu\nu}$ 



 $\Lambda$  is the "cosmological constant" intended to keep the universe static.



### The Cosmological Principle • The Universe is – Homogeneous (uniform in composition) – Isotropic (looks the same in every direction)

We need these *assumptions* in order to apply Einstein's equations to the universe as a whole.

### The Perfect Cosmological Principle • The universe looks the same from

everywhere at all times.

This philosophical principle led Einstein to introduce the cosmological constant. It was a fudge to force it to be so.

$$\mathcal{R}_{\mu\nu} - \frac{1}{2}\mathcal{R}g_{\mu\nu} = \frac{8\pi G}{c^4}T_{\mu\nu} + \Lambda g_{\mu\nu}$$

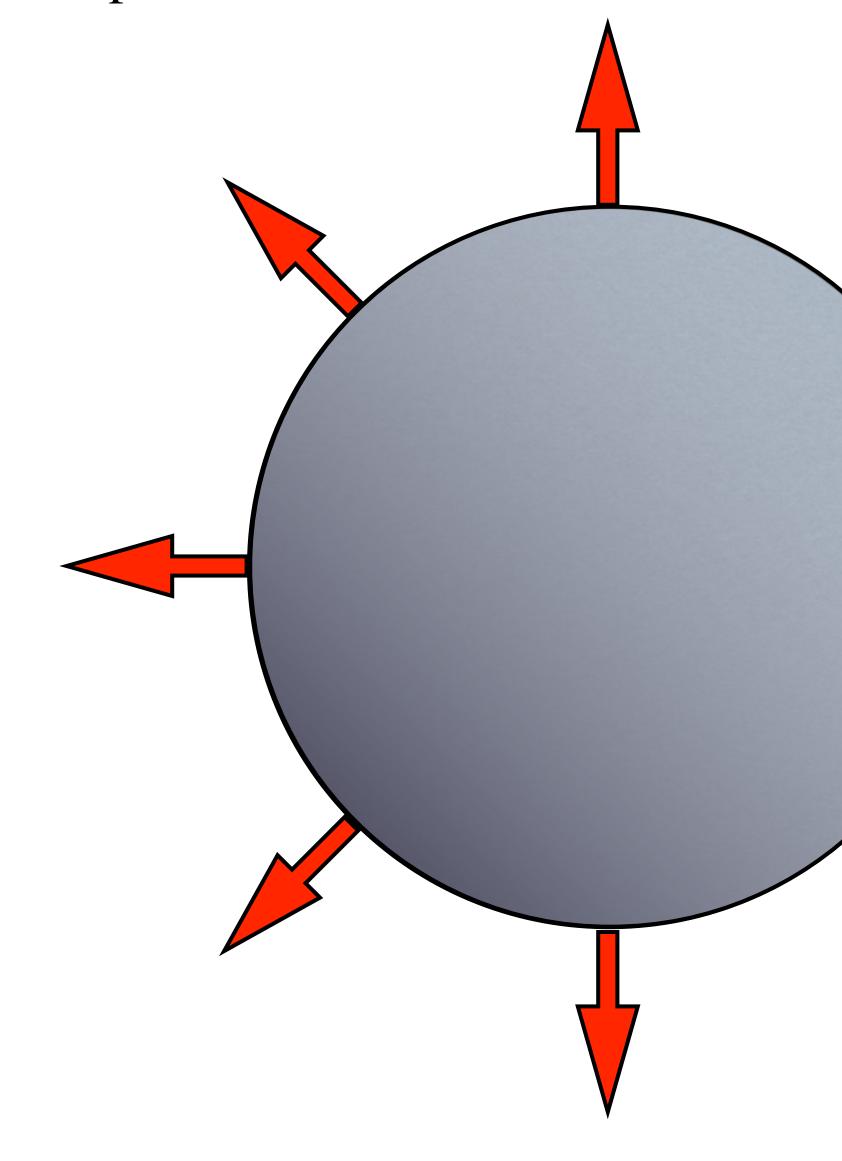
Only works if

 $\Lambda = 4\pi G\rho$ 

and even then it is unstable, like needles on their points.

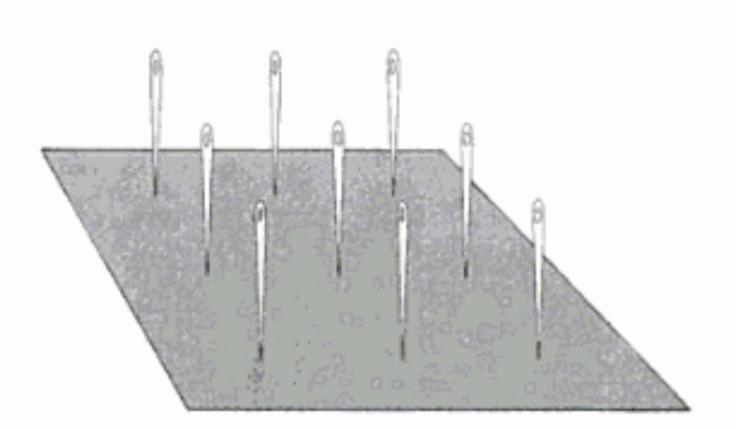


An expanding universe solves the stability problem that Newton & Bentley corresponded about.



Fundamentally, this was the same problem Bentley & Newton had encountered. A static universe will collapse to a point under the mutual gravitational attraction of all its constituent parts.

Einstein's cosmological constant suffers the same instability problem: it only holds the universe constant for one very specific, fine-tuned value. Any perturbation, and it drives accelerated expansion. General Relativity cannot satisfy the "Perfect" Cosmological Principle.





### Does this look homogeneous and isotropic?

Every dot pictured here is a galaxy

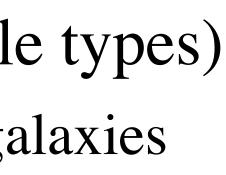
The color-coding corresponds to redshift: redder galaxies are more distant. The distribution of galaxies is structured into enormous filaments and walls surrounding giant voids.

All sky galaxy distribution 2MASS galaxy survey

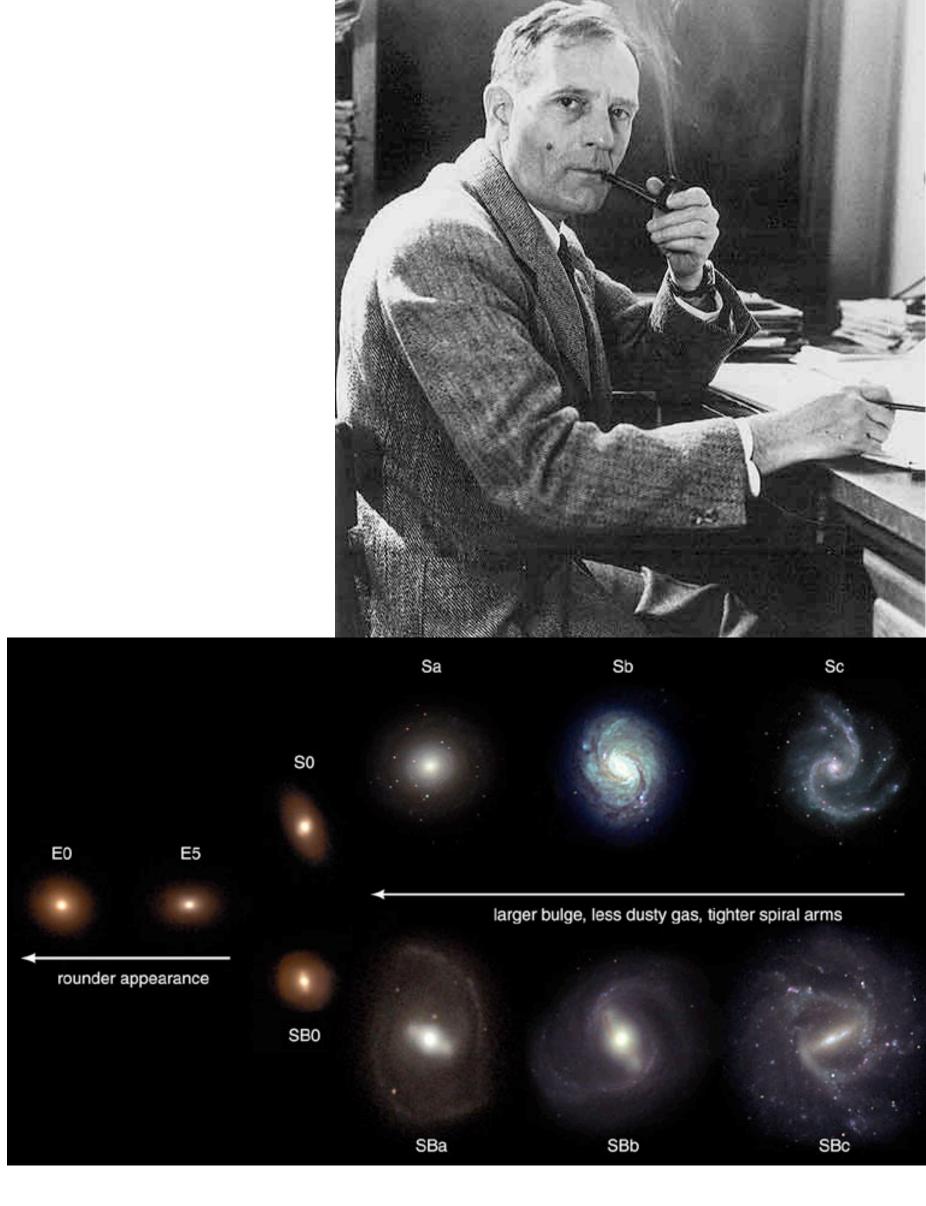


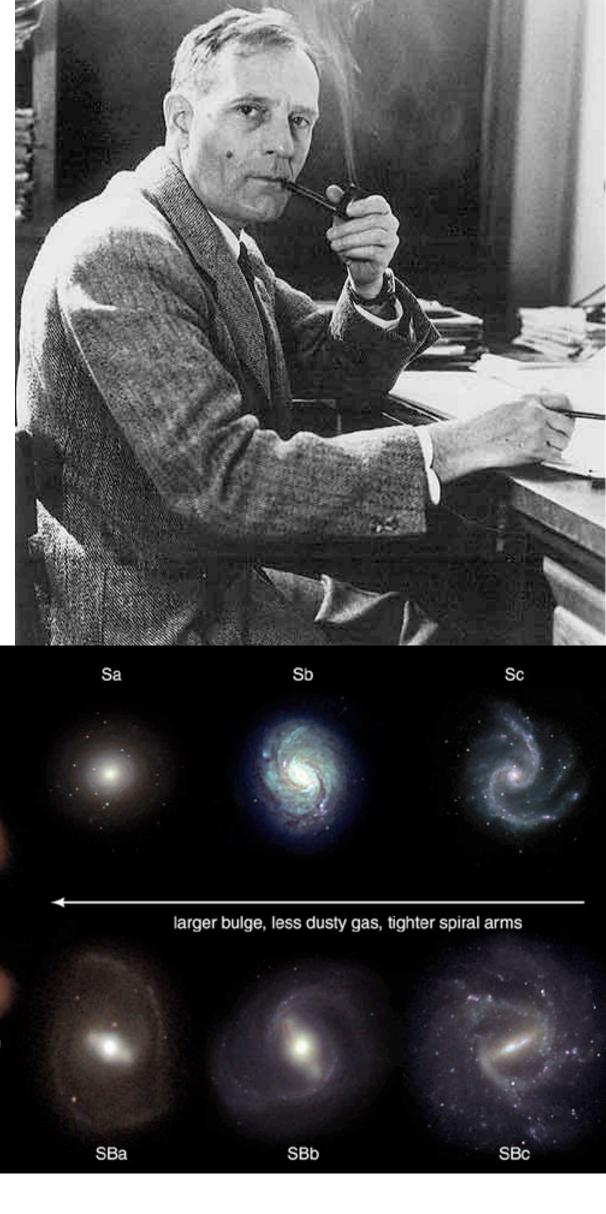
- Showed that galaxies were distant systems, comparable in size to the Milky Way
  - settled the Great Debate after ten years.
- Classified galaxy morphology (Hubble types)
  - tuning fork diagram; spiral & elliptical galaxies
- Demonstrated the expansion of the Universe.

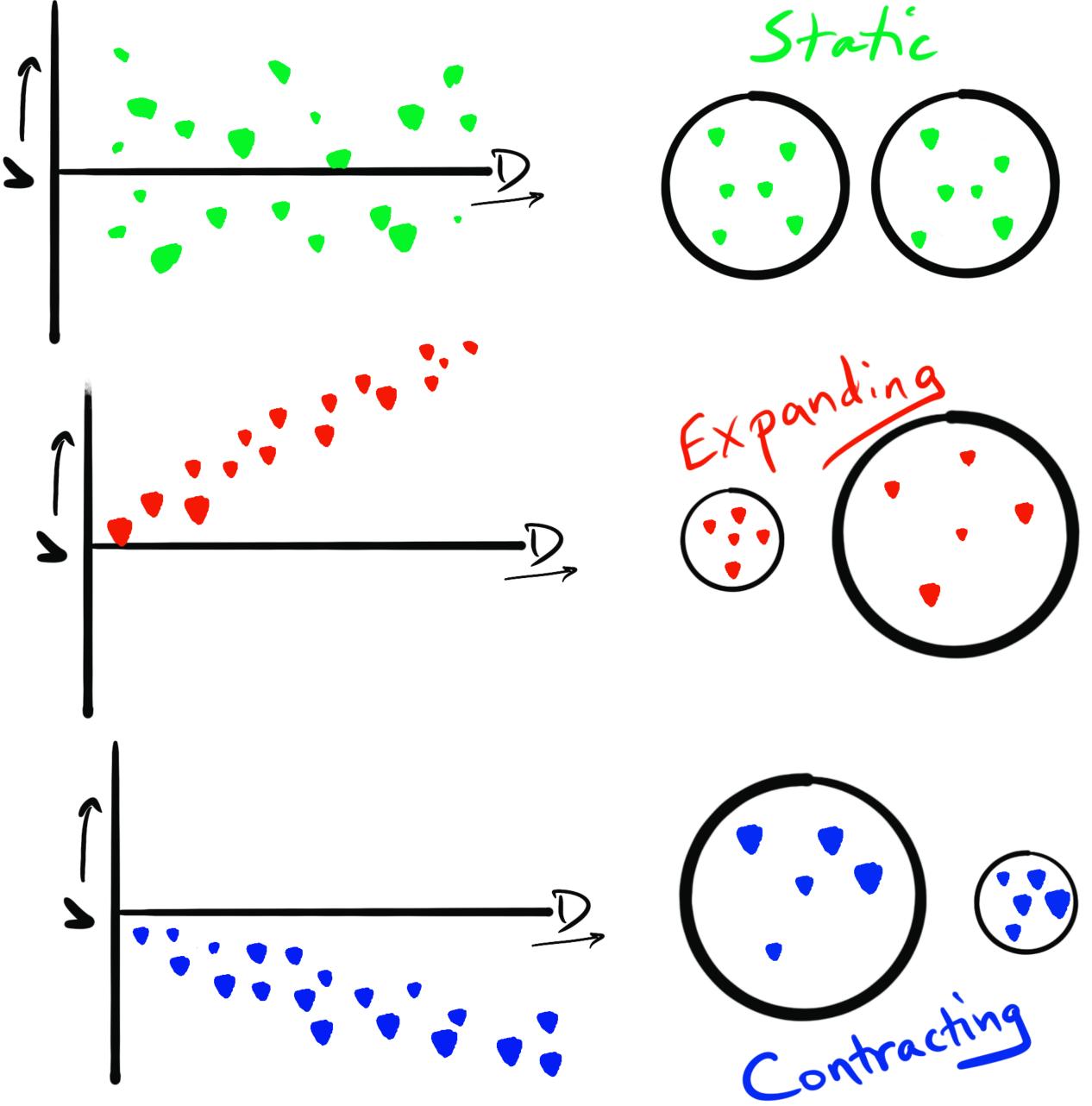
## Hubble



1920S & 30S

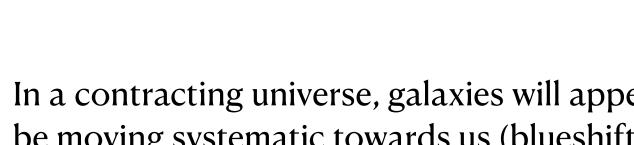






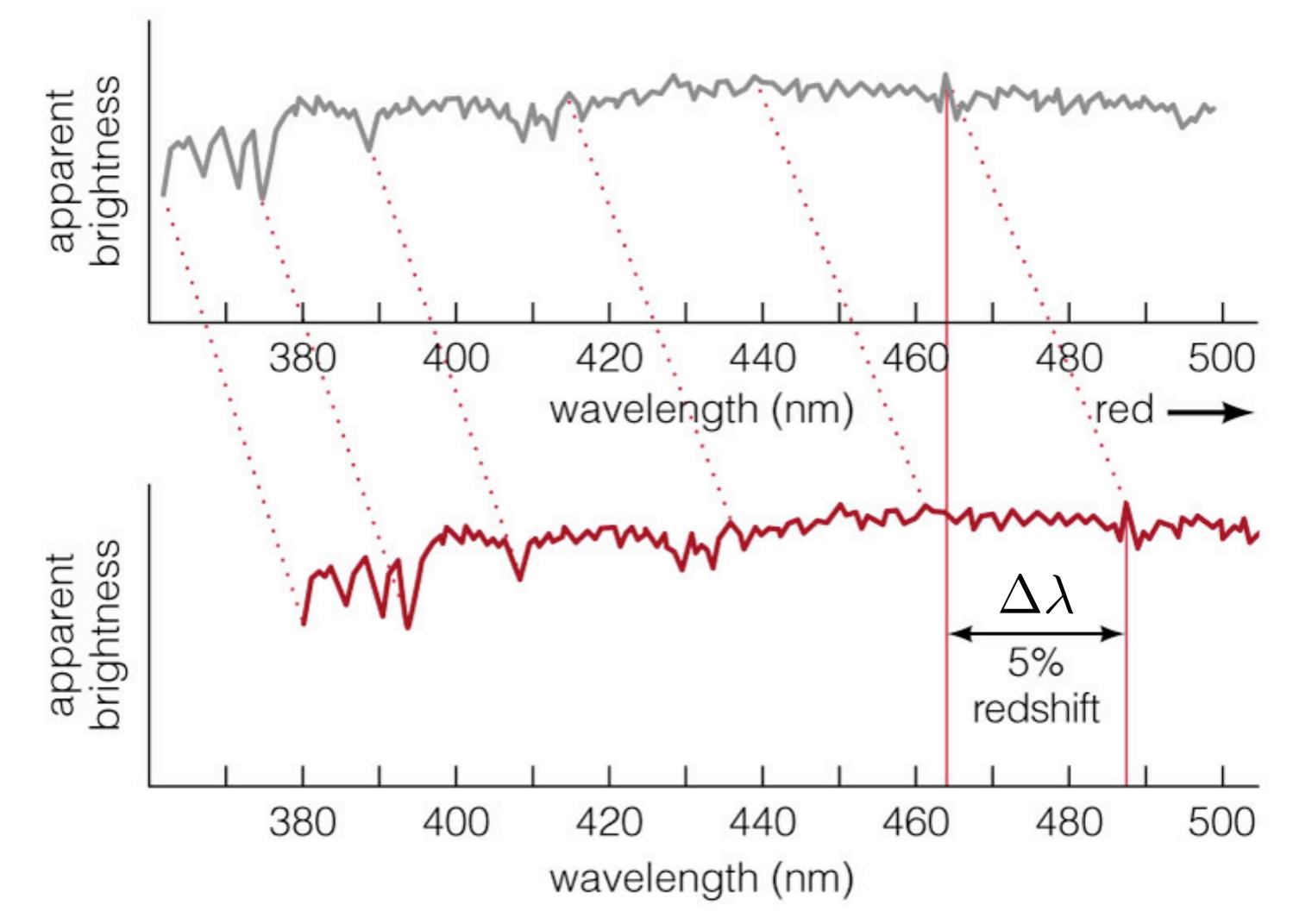
In a static universe, galaxies might move around, with some moving towards us and some away, but there should be no systematic trend one way or the other.

In an expanding universe, galaxies will appear to be moving systematic away from us in proportion to their distance. The more remote a galaxy, the more stretching of the space in between. This is the origin of Hubble's expansion law  $V = H_o D$ .



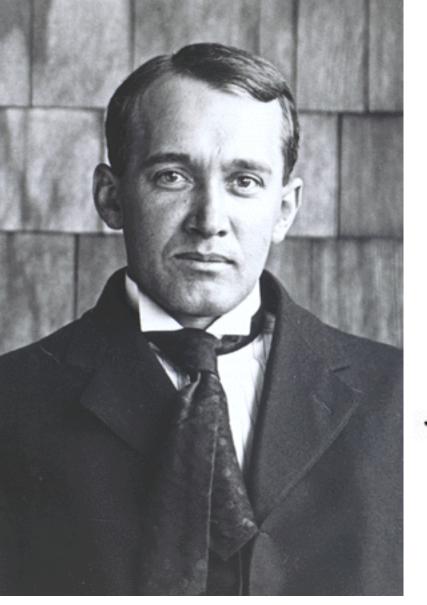
In a contracting universe, galaxies will appear to be moving systematic towards us (blueshifted instead of redshifted).





they're all moving away from us.

Hubble knew from Slipher's work that the spectral features of virtually all galaxies are *redshifted*  $\Rightarrow$ 

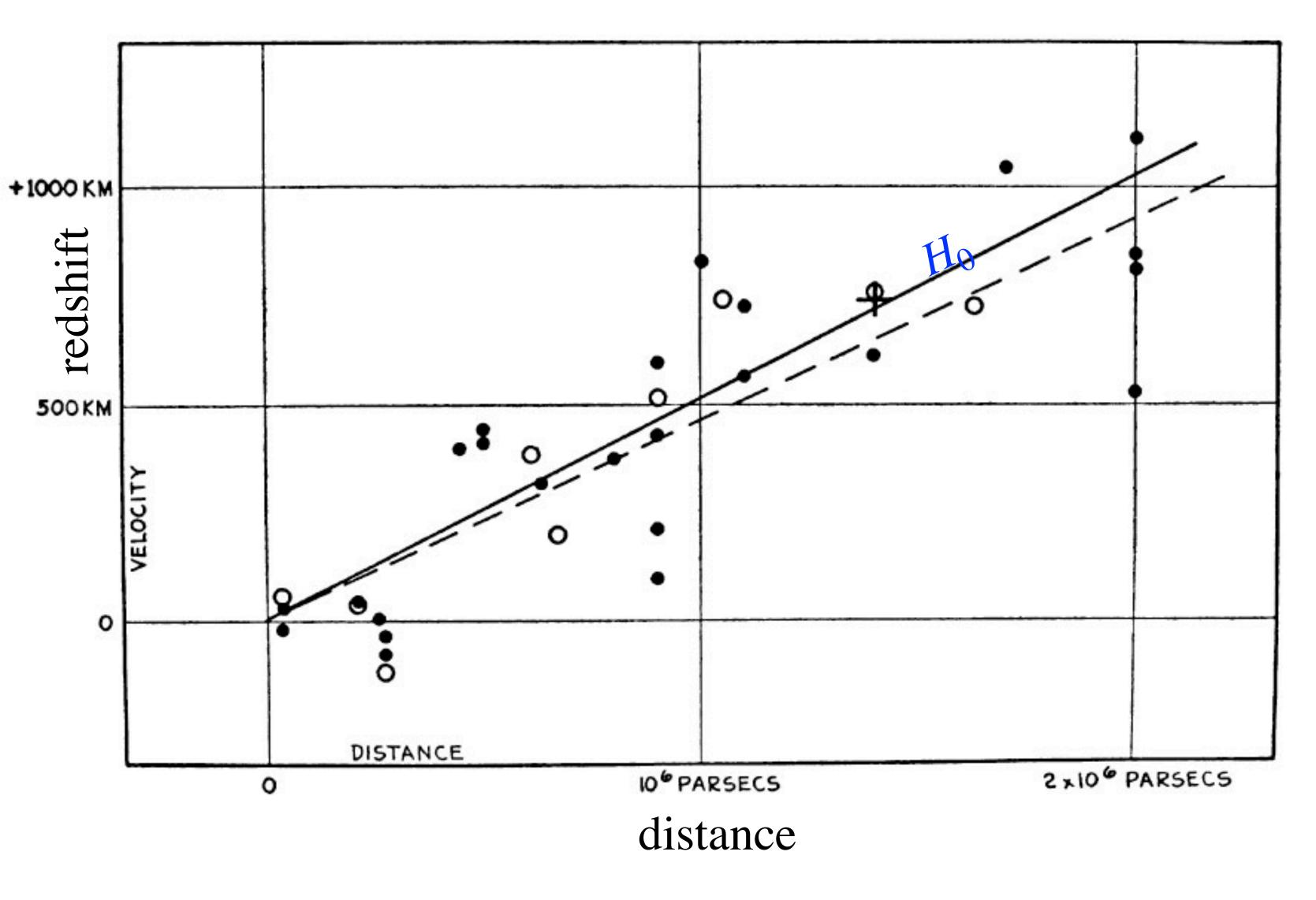


Slipher measured redshifts

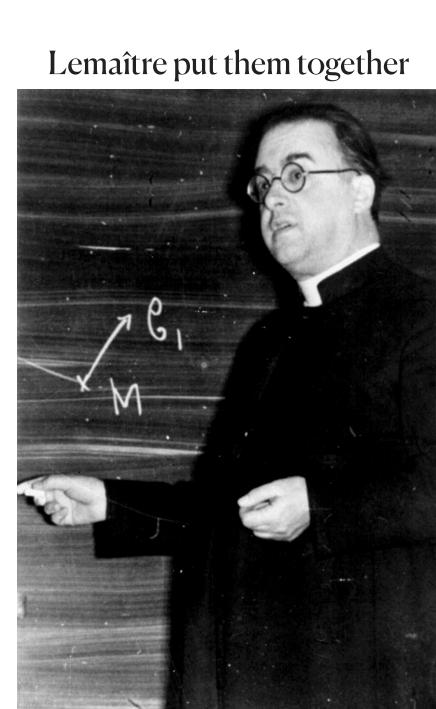
Hubble measured distances

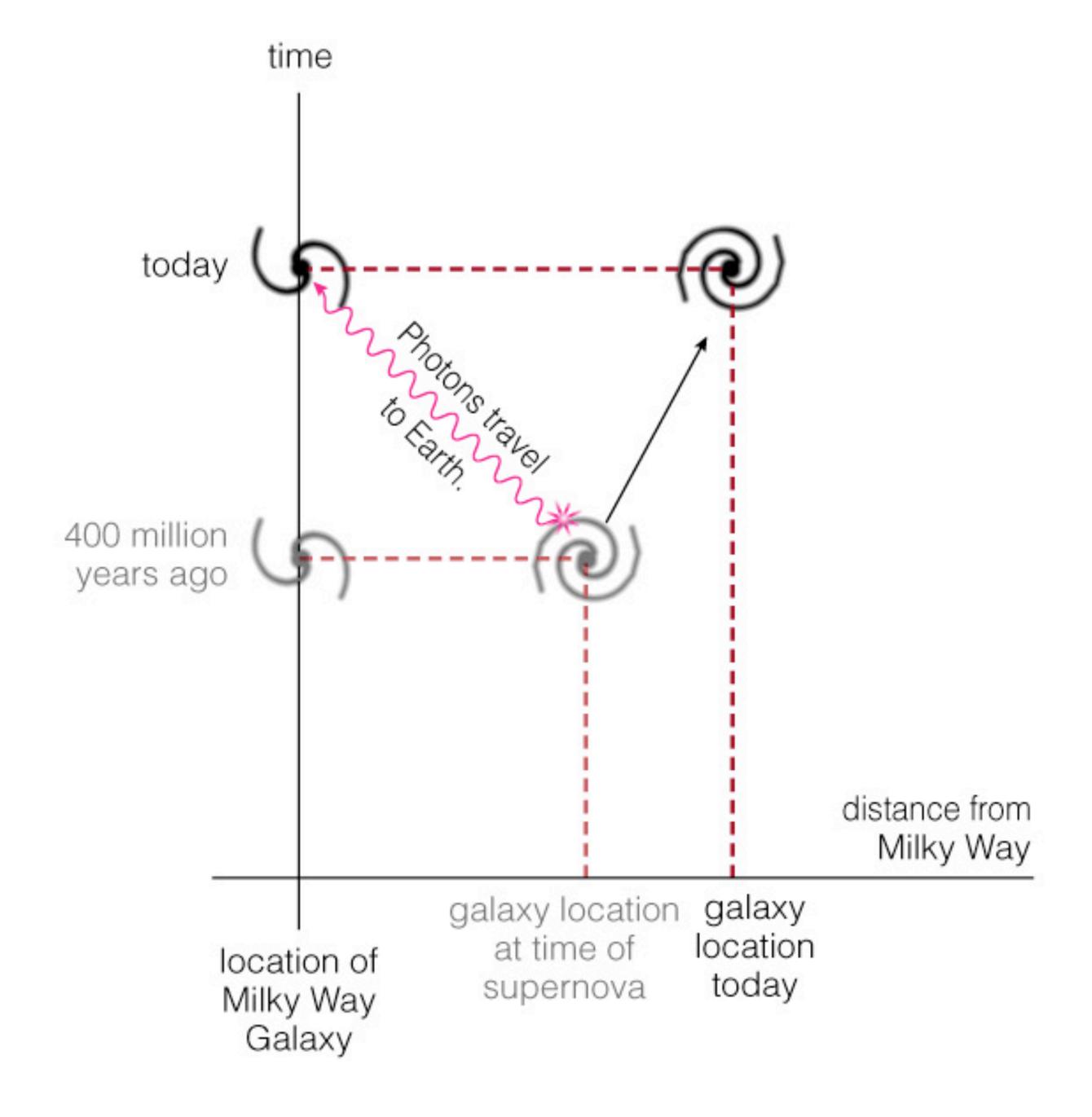


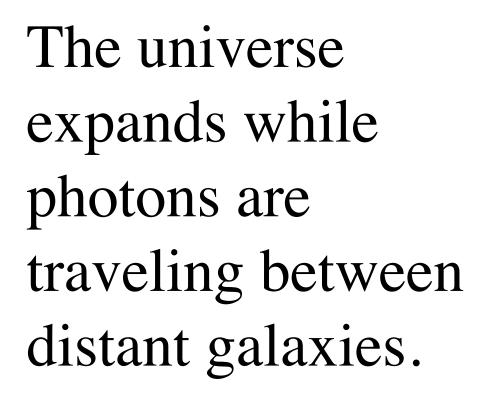
The slope of this relation is the expansion rate of the universe. Hubble's constant quantifies the size and age of the universe.



Hubble's law  $V = H_0 D$ 



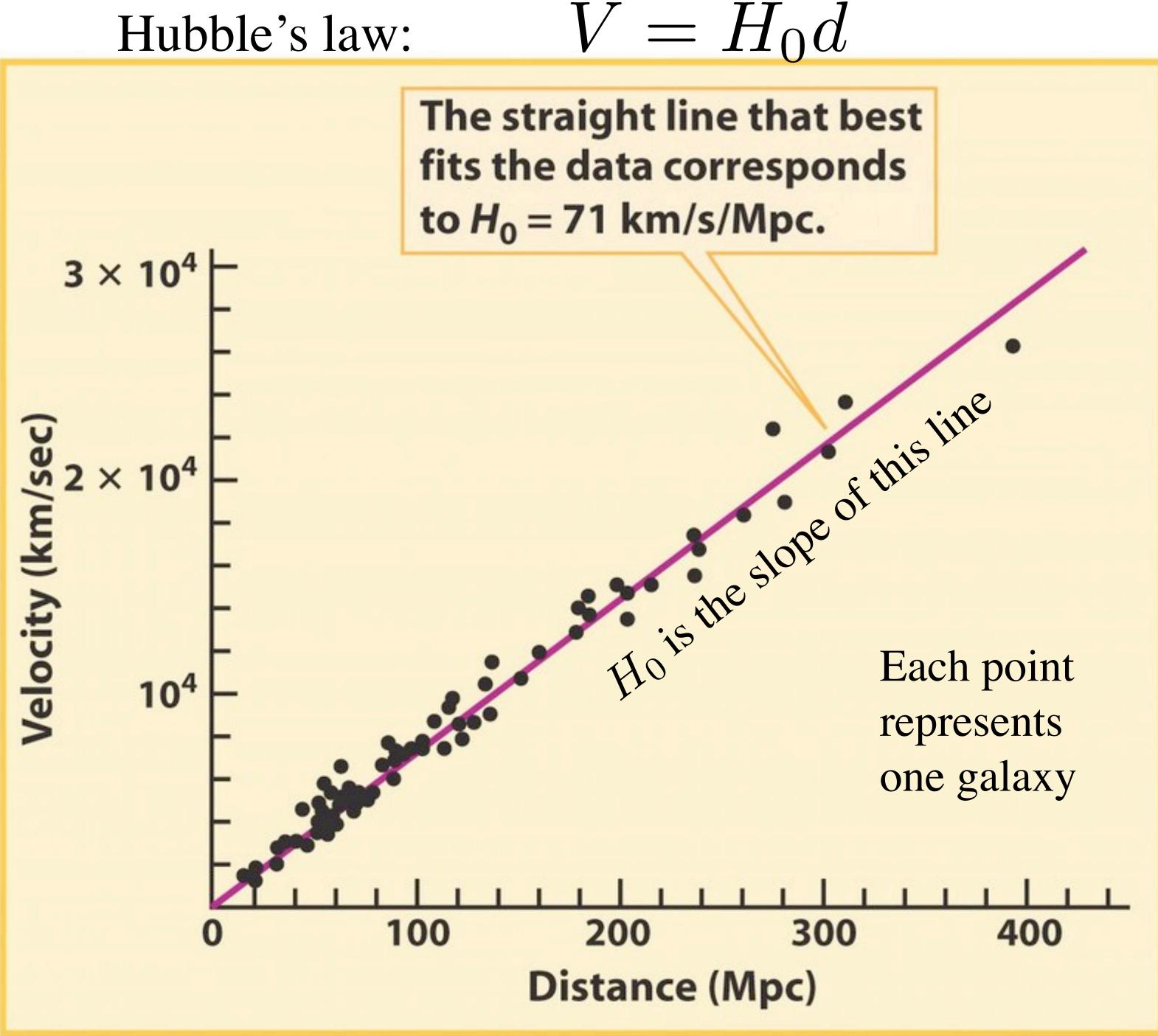




Looking further away is equivalent to looking back in time.

### Hubble's law:

# to $H_0 = 71$ km/s/Mpc.



Hubble's earliest estimate was about 500 km/s/Mpc

Historically, there was a long-running debate between 50 (Sandage) and 100 (de Vaucouleurs) km/s/Mpc

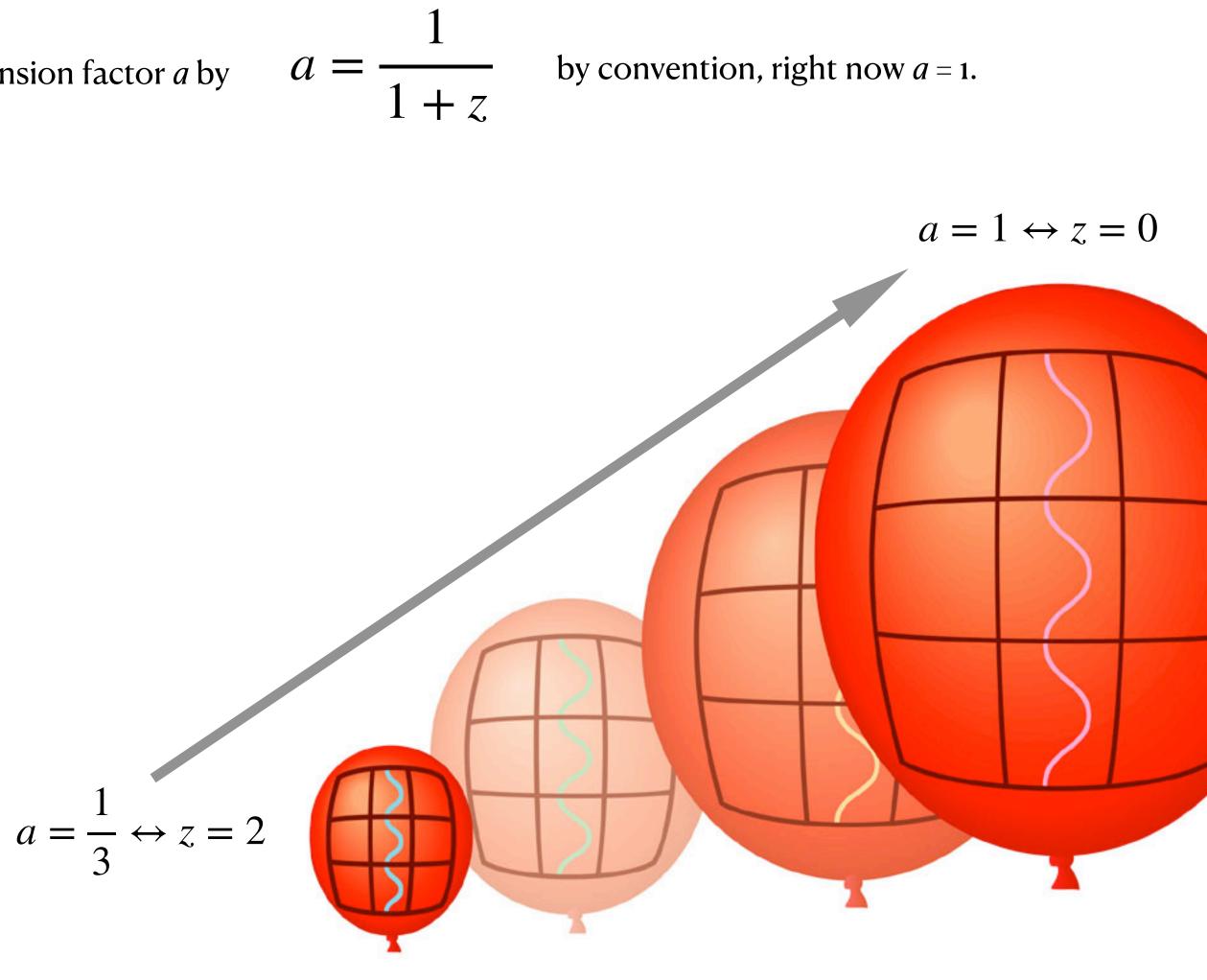
Modern estimates range from 67 - 75 km/s/Mpc



Expansion stretches photon wavelengths causing the *cosmological redshift*: stretching of space, *not* an explosion.

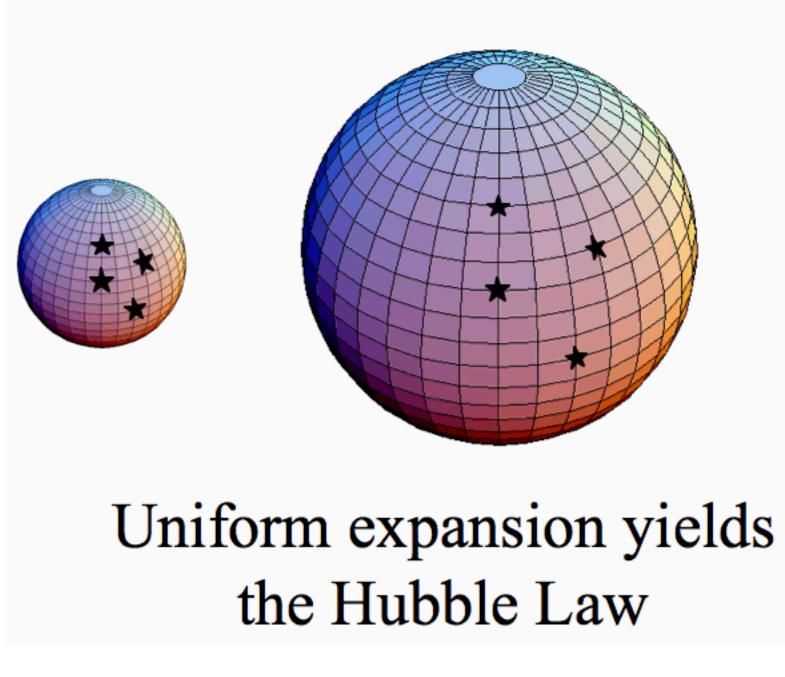
 $V = H_0 d$  is linear in the Proper Distance redshift  $z = \frac{\Delta \lambda}{\lambda} = \frac{\lambda_{obs} - \lambda_{em}}{\lambda_{em}}$  related to expansion factor *a* by  $a = \frac{1}{1+z}$  by convention, right now a = 1.  $z = \frac{\Delta \lambda}{\lambda} \approx \frac{V}{c}$  in the non-relativistic limit

but more generally  $1 + z = \sqrt{\frac{1 + V/c}{1 - V/c}}$ 





The proper distance between galaxies increases with time. Their comoving separations, as depicted by the grid, do not.



The universe expands as time increases

Expansion stretches photon wavelengths causing the *cosmological redshift*: stretching of space, *not* an explosion.

