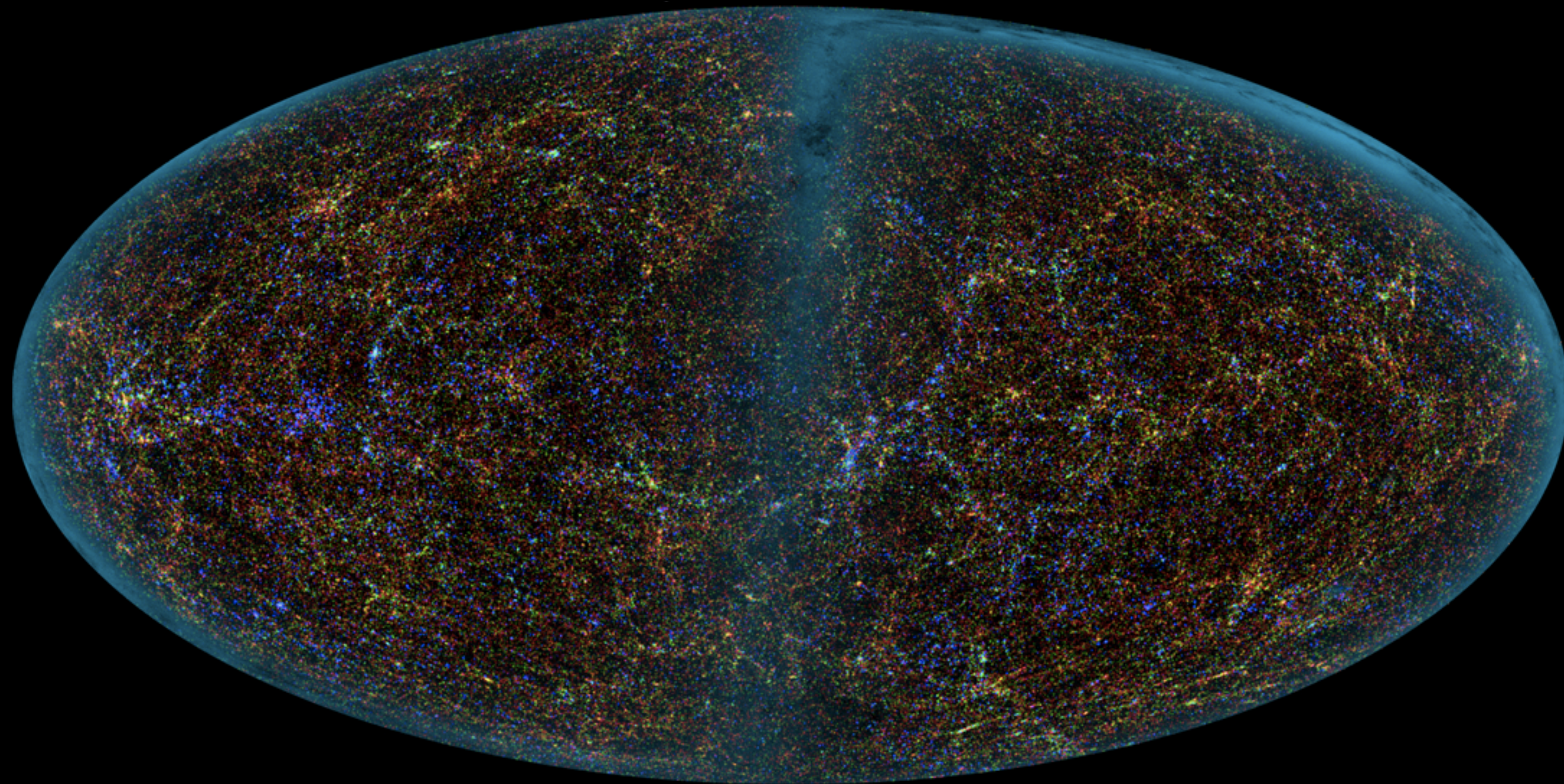


# Cosmology

## and Large Scale Structure



Today  
More CMB  
Reionization

Next time: Review, Homework 5 due  
One week hence: Exam



# CMB power spectrum

Etc. pole

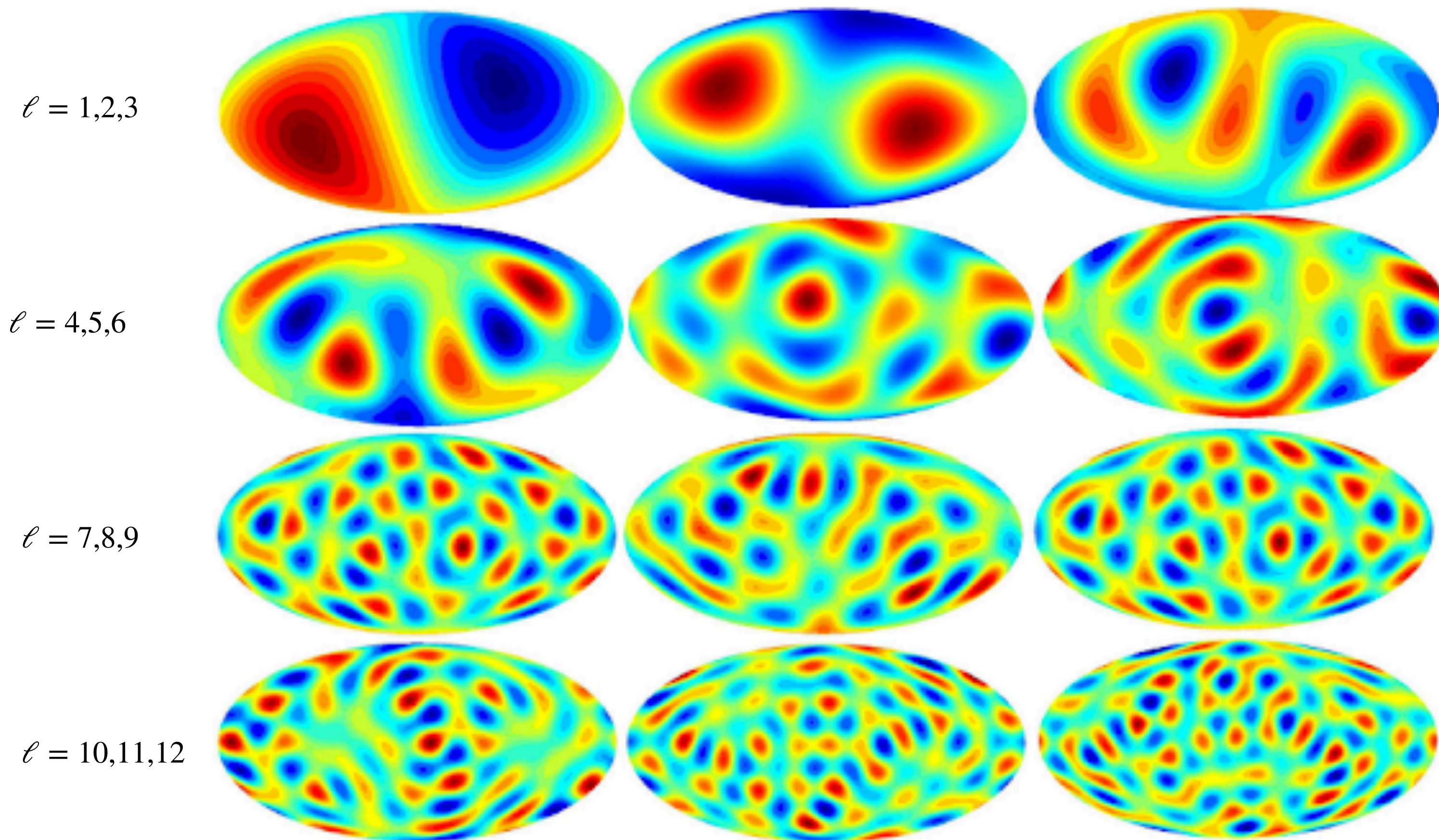
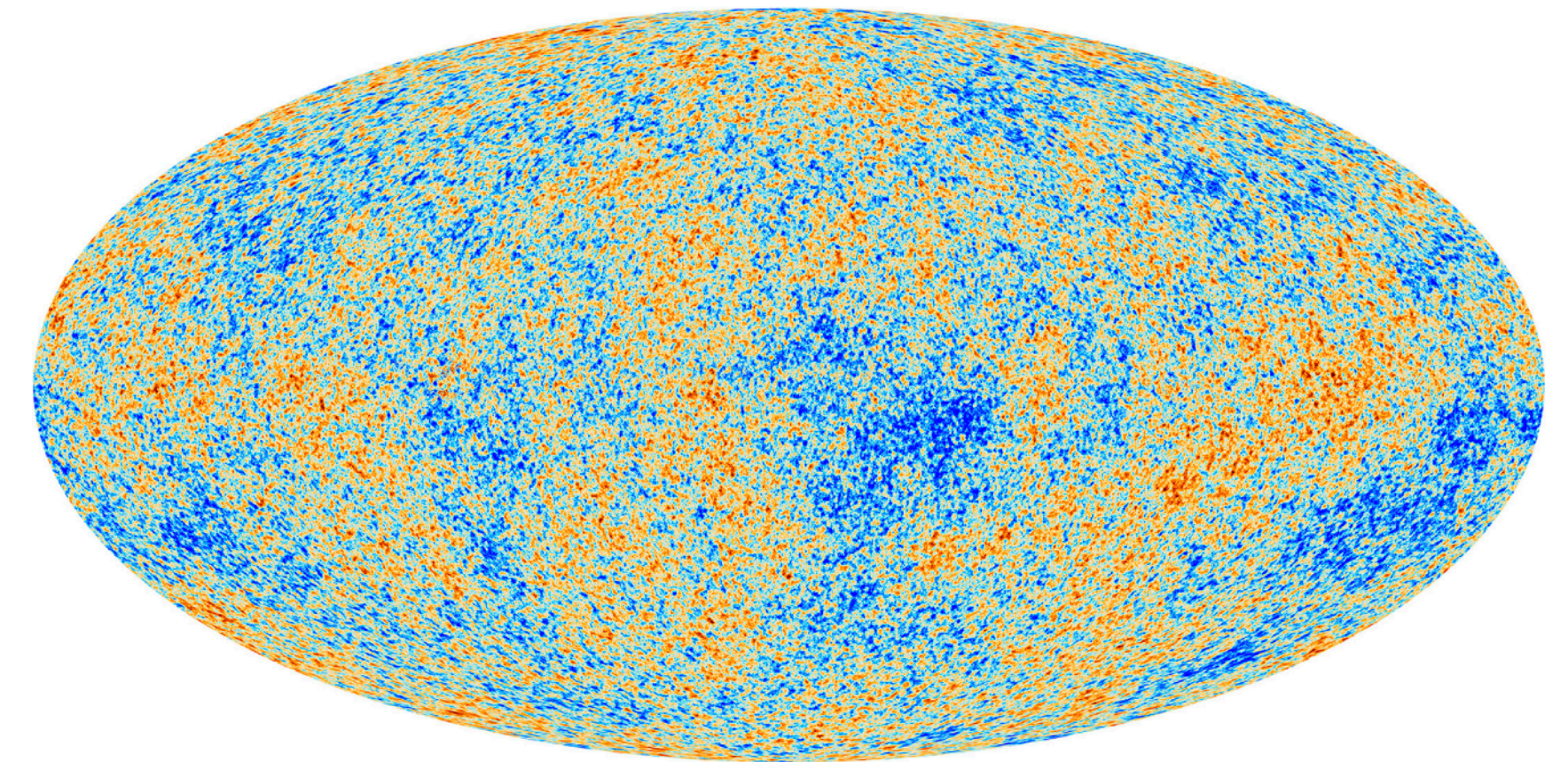


Figure 6: Randomly generated skies containing only a single multipole  $\ell$ . Starting from top left:  $\ell = 1$  (dipole only), 2 (quadrupole only), 3 (octupole only), 4, 5, 6, 7, 8, 9, 10, 11, 12. Figure by Ville Heikkilä.



Spherical harmonics provide a convenient way to decompose the fluctuations observed on the sky

$$\frac{\Delta T}{T}(\theta, \phi) = \sum_{\ell=0}^{\infty} \sum_{m=-\ell}^{\ell} A_{\ell m} Y_{\ell m}$$

with Fourier transform

$$A_{\ell m} = \int_{\text{sky}} \frac{\Delta T}{T}(\theta, \phi) Y_{\ell m}^* d\Omega$$

giving the power in fluctuations on an angular scale  $\frac{\pi}{\ell}$

$$C_{\ell} = \frac{1}{2\ell + 1} \sum_m A_{\ell m} A_{\ell m}^* = \langle |A_{\ell m}|^2 \rangle$$

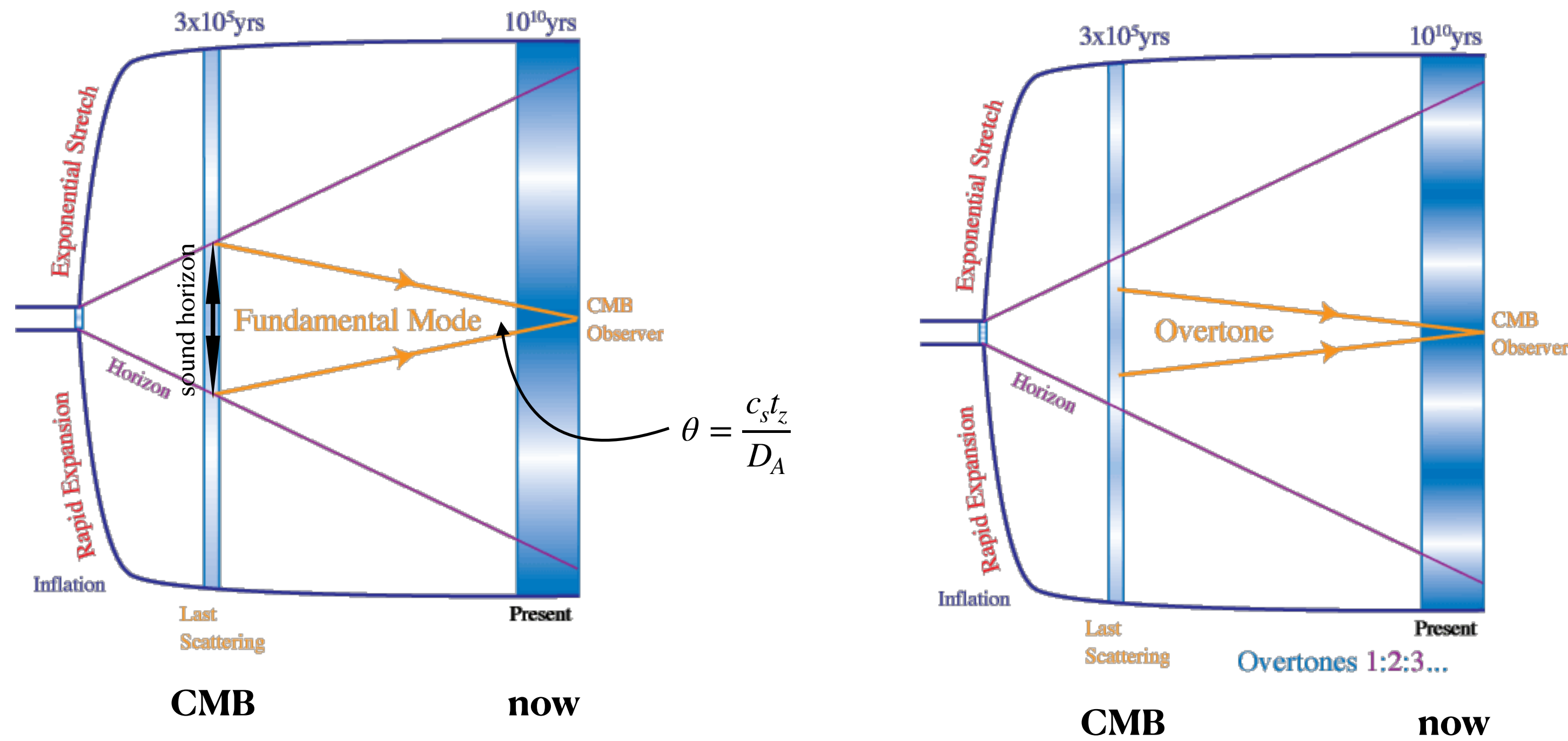
note:  $1^\circ = 0.0175$  radians so one degree corresponds to  $\frac{\pi}{\ell} = 0.0175$ , hence  $\ell = 180$ .

Multipole  $\ell$  varies inversely with angular scale.

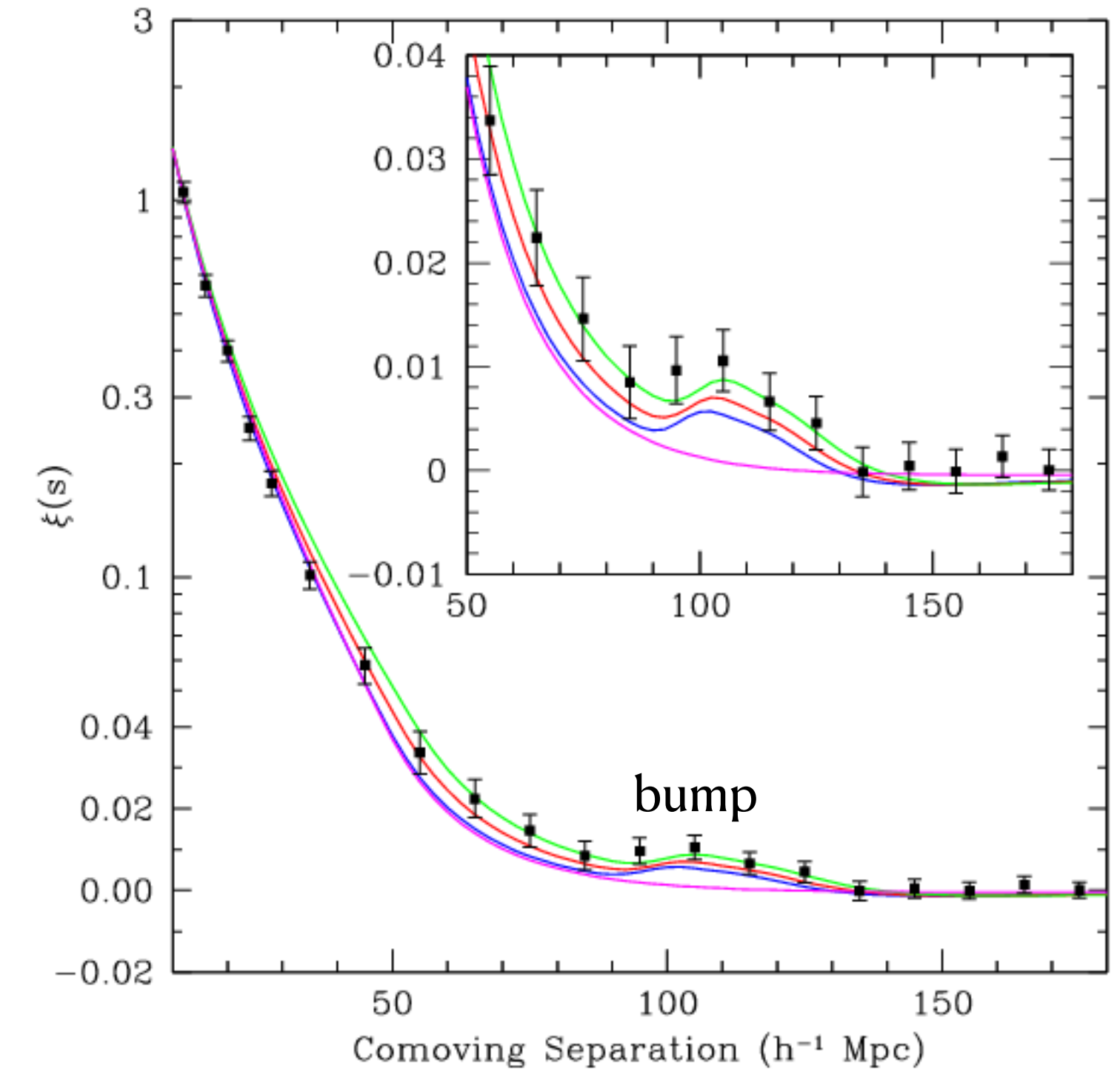


# CMB power spectrum

Detailed shape of the acoustic power spectrum depends sensitively on cosmic parameters. First and foremost, the location of the first peak measures the angular diameter distance to the surface of last scattering. This is the best evidence that the universe is very nearly flat:  $\Omega_k = -0.011 \pm 0.006$  (Planck X 2018)



Baryon acoustic oscillation in galaxy correlation function



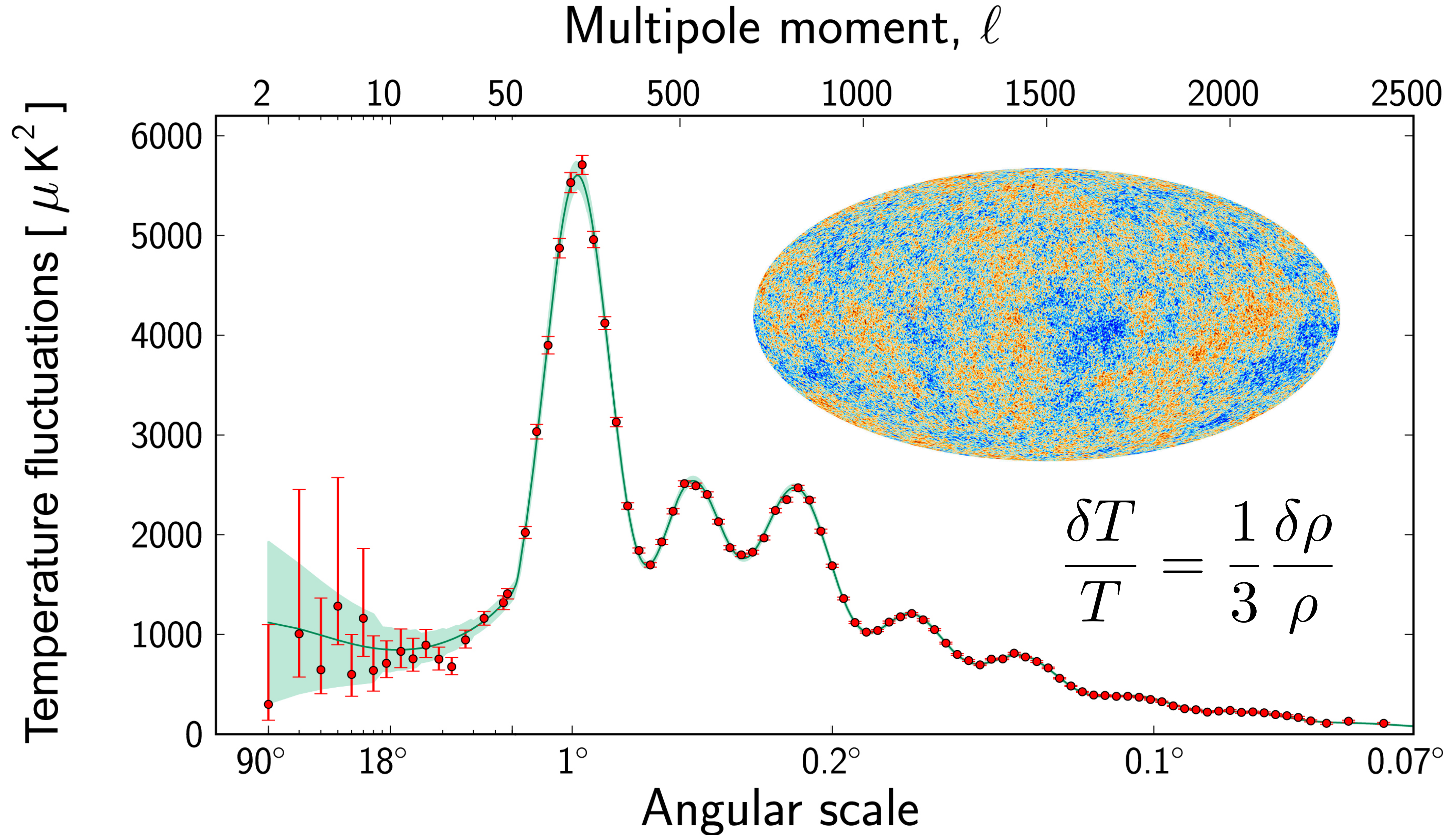
Eisenstein et al. (2005)

From Wayne Hu's CMB tutorial - <http://background.uchicago.edu/index.html>



# CMB power spectrum

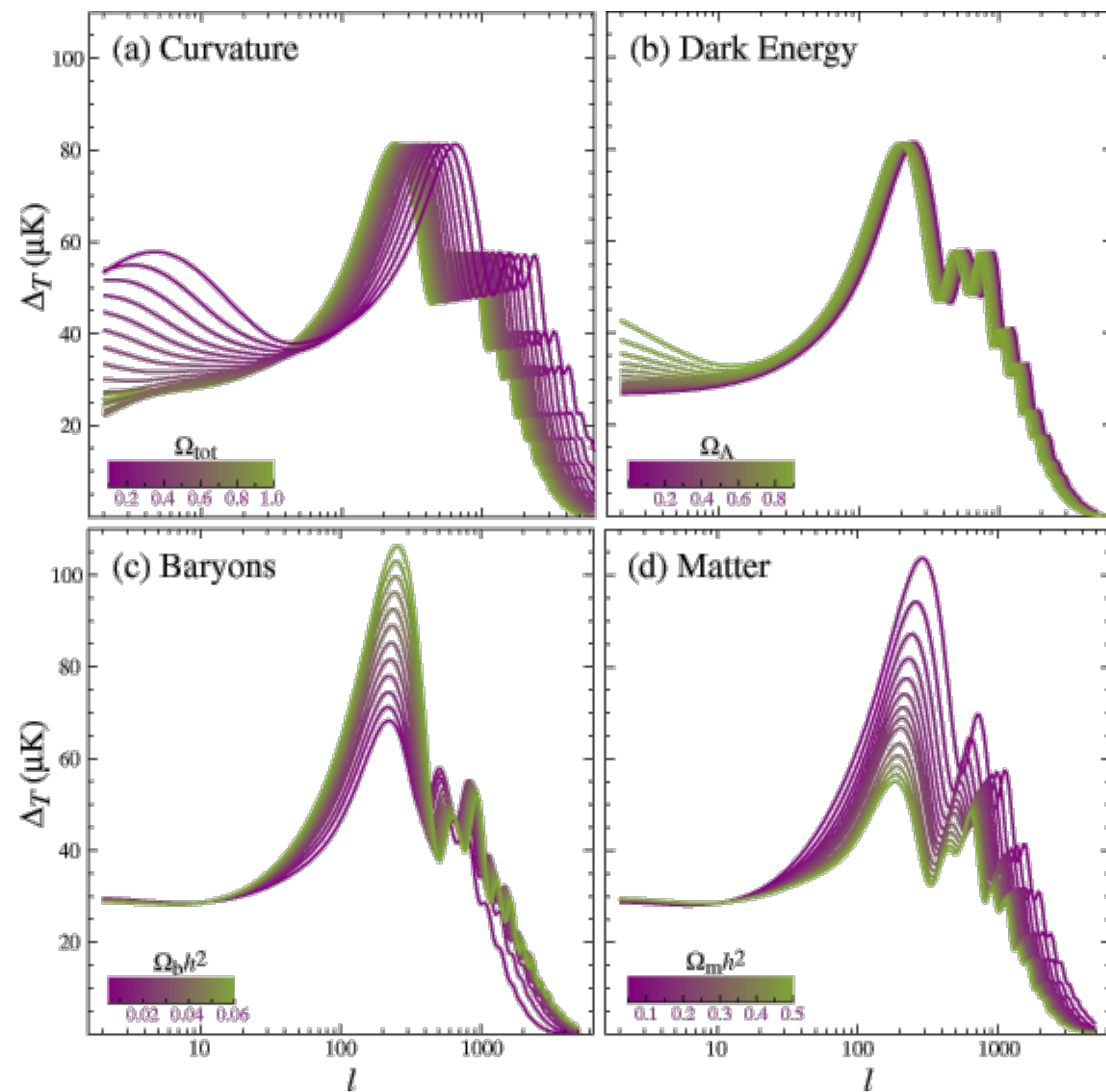
Detailed shape of the acoustic power spectrum depends sensitively on cosmic parameters. First and foremost, the location of the first peak measures the angular diameter distance to the surface of last scattering. This is the best evidence that the universe is very nearly flat:  $\Omega_k = -0.011 \pm 0.006$  (Planck X 2018)





# CMB power spectrum

Detailed shape of the acoustic power spectrum depends sensitively on cosmic parameters.



Best-fit cosmology obtained from multi-parameter fit. Well constrained, but not unique - lots of parameter degeneracy.

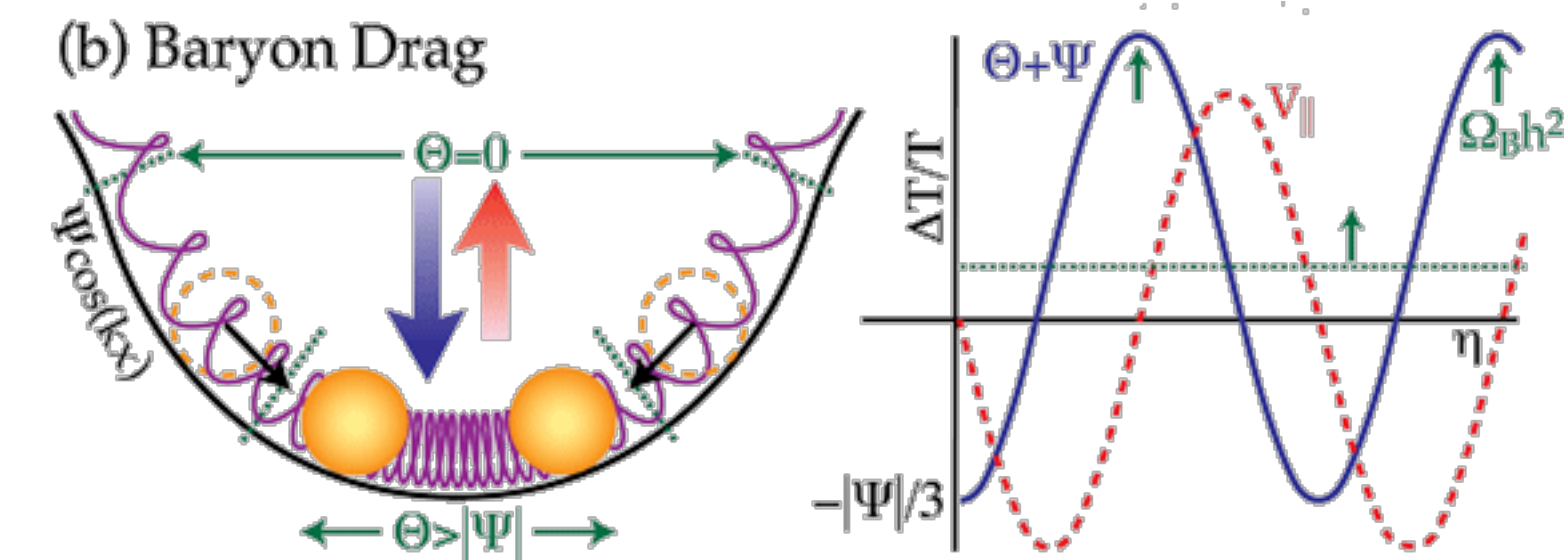
Compression and rarefaction nearly cancel out, but don't quite. Left with

$$\frac{\delta T}{T} = \frac{1}{3} \frac{\delta \rho}{\rho}$$

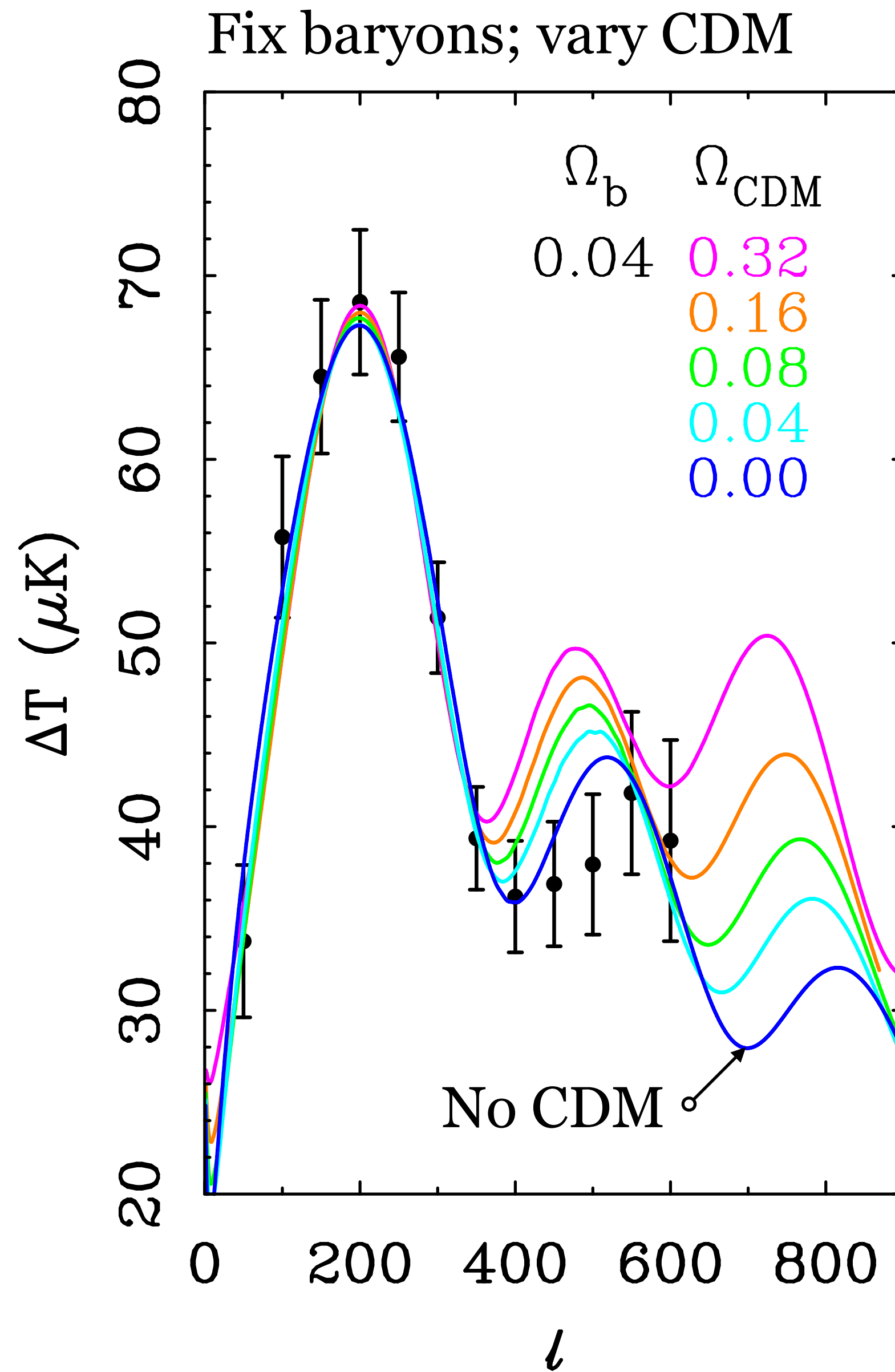
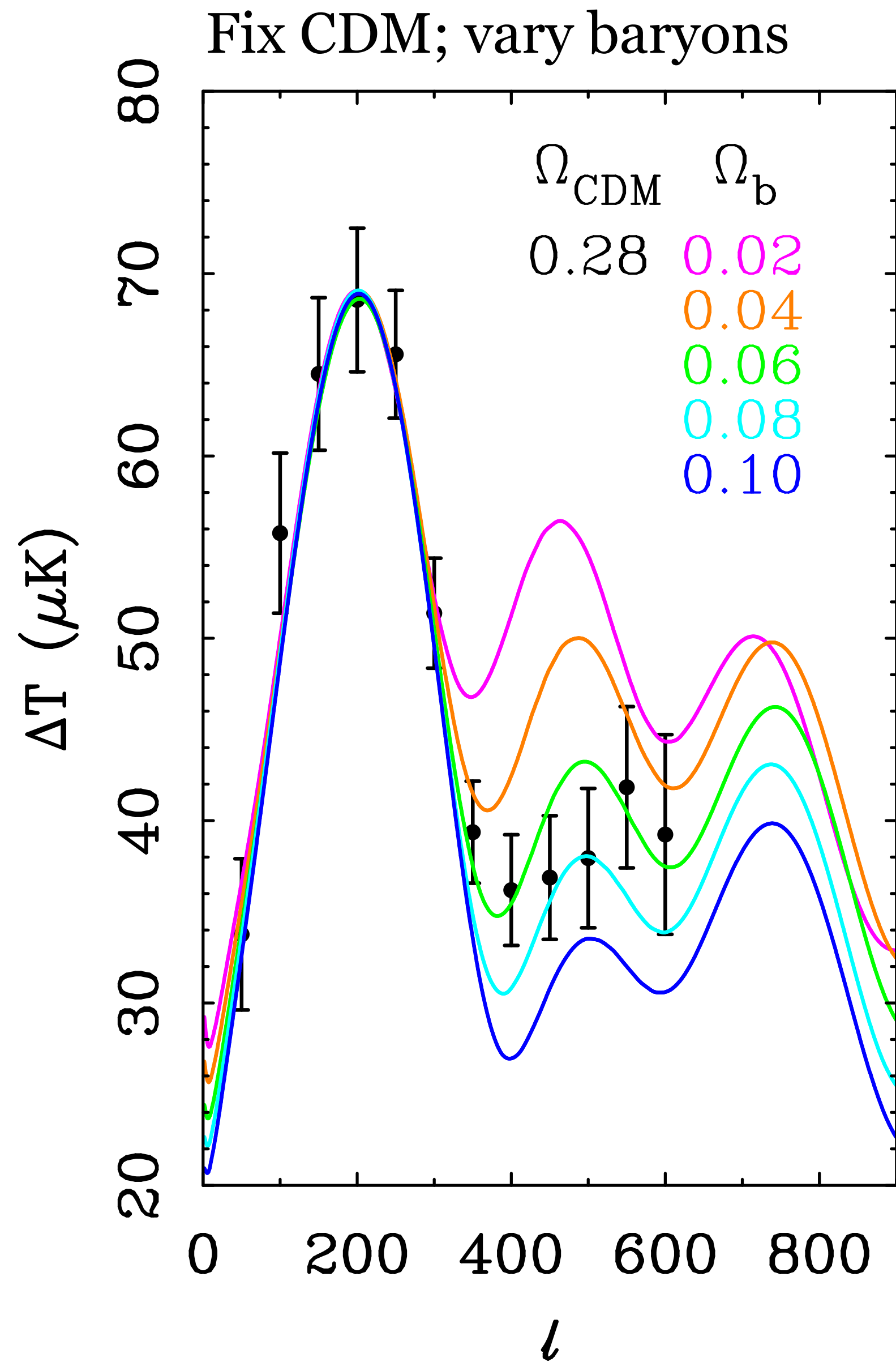
Damped and driven oscillator

Baryons damp oscillations, like a kid dragging his feet on a swing. pure damping spectrum in limit of all baryons

Dark matter helps drive oscillations, like a parent pushing the kid.



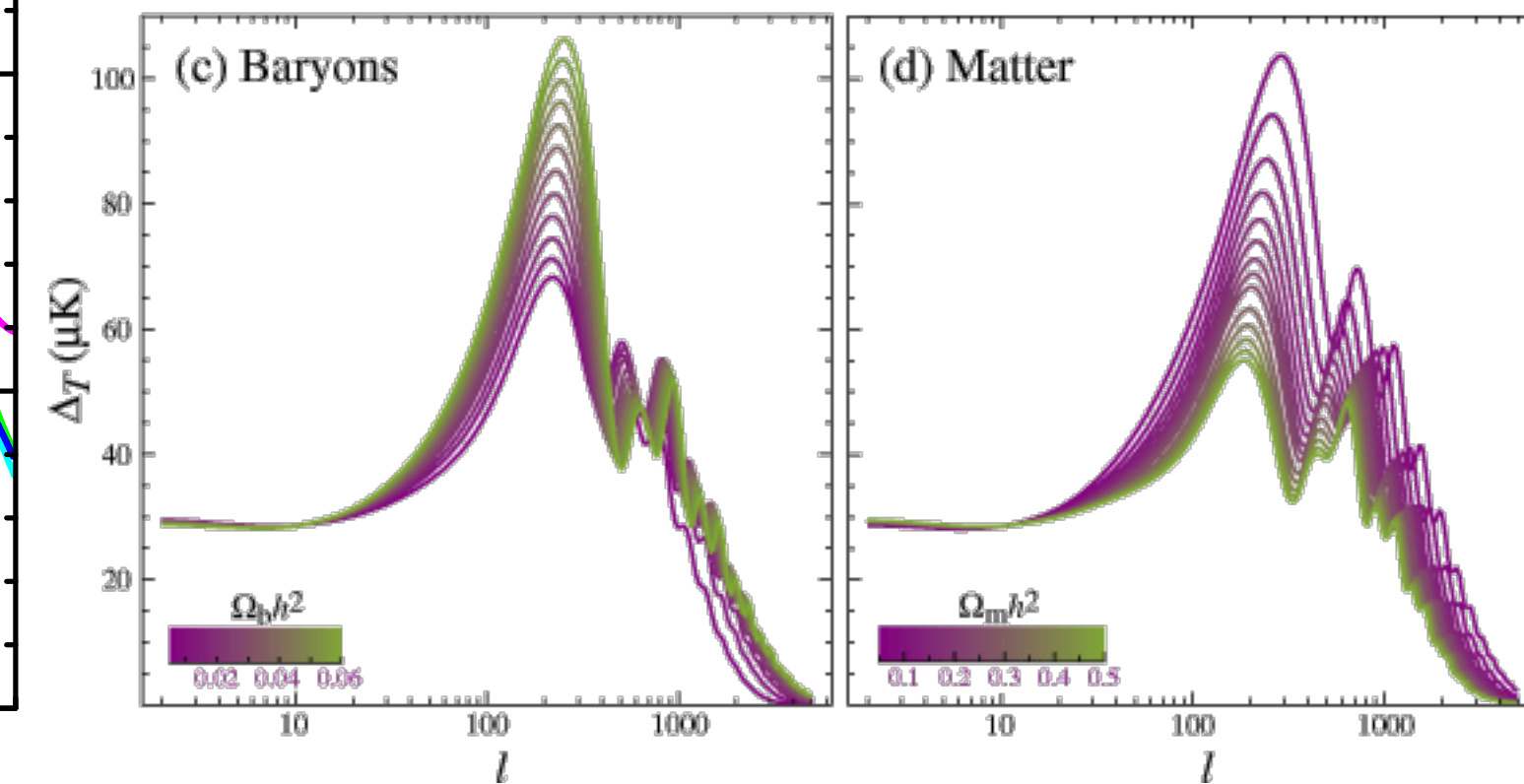
# CMB dependence on the density of baryonic and non-baryonic matter

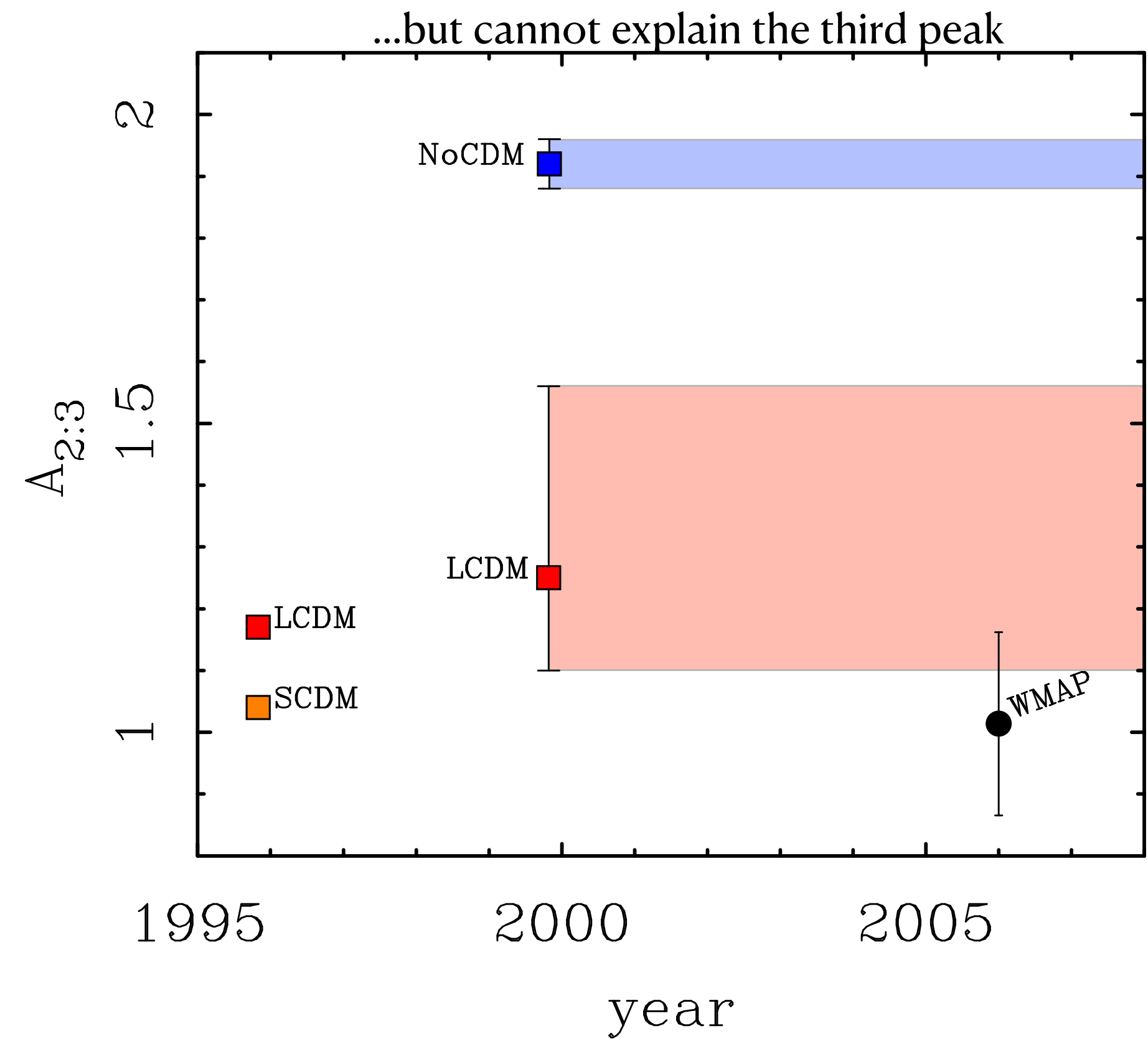
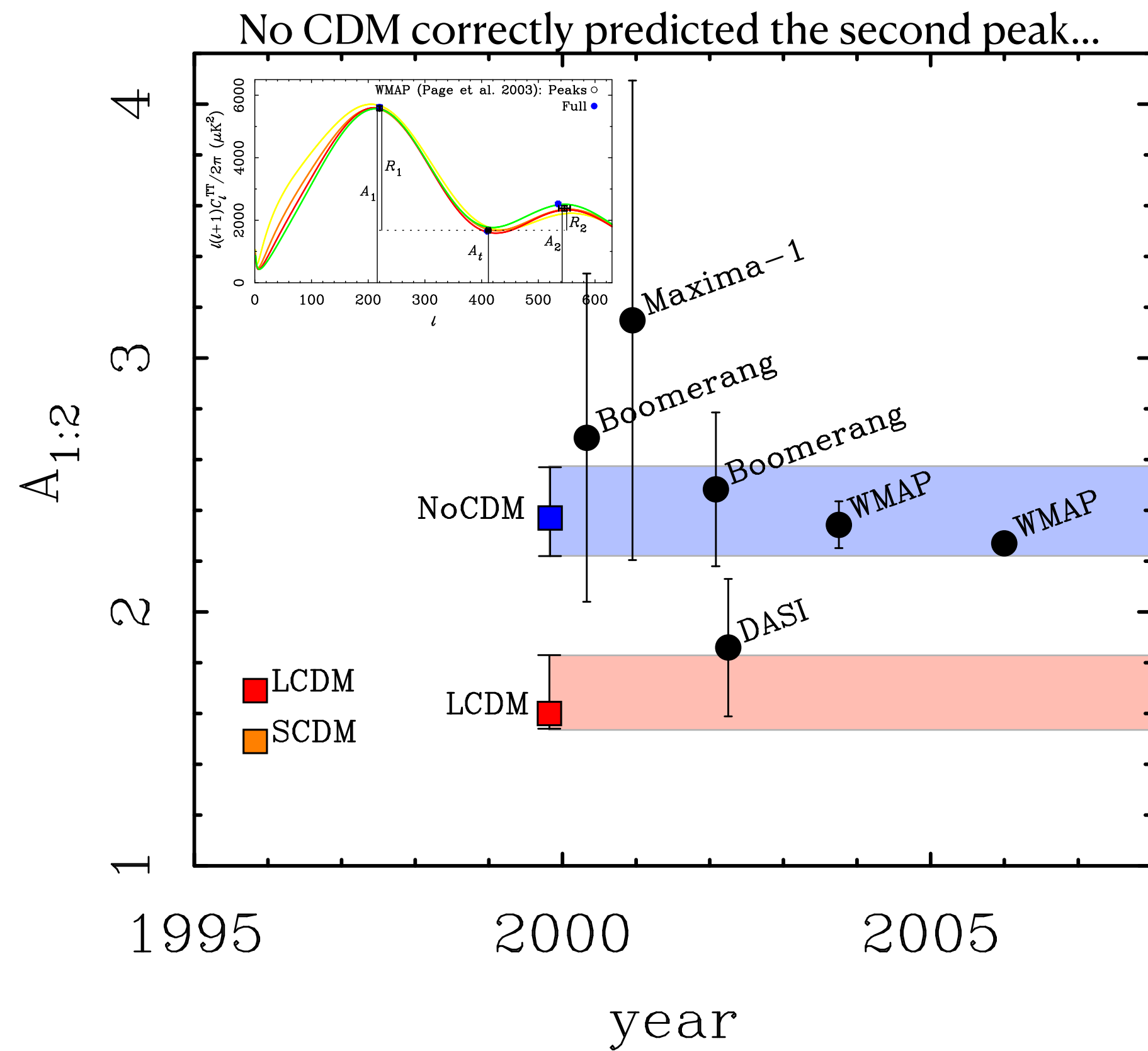
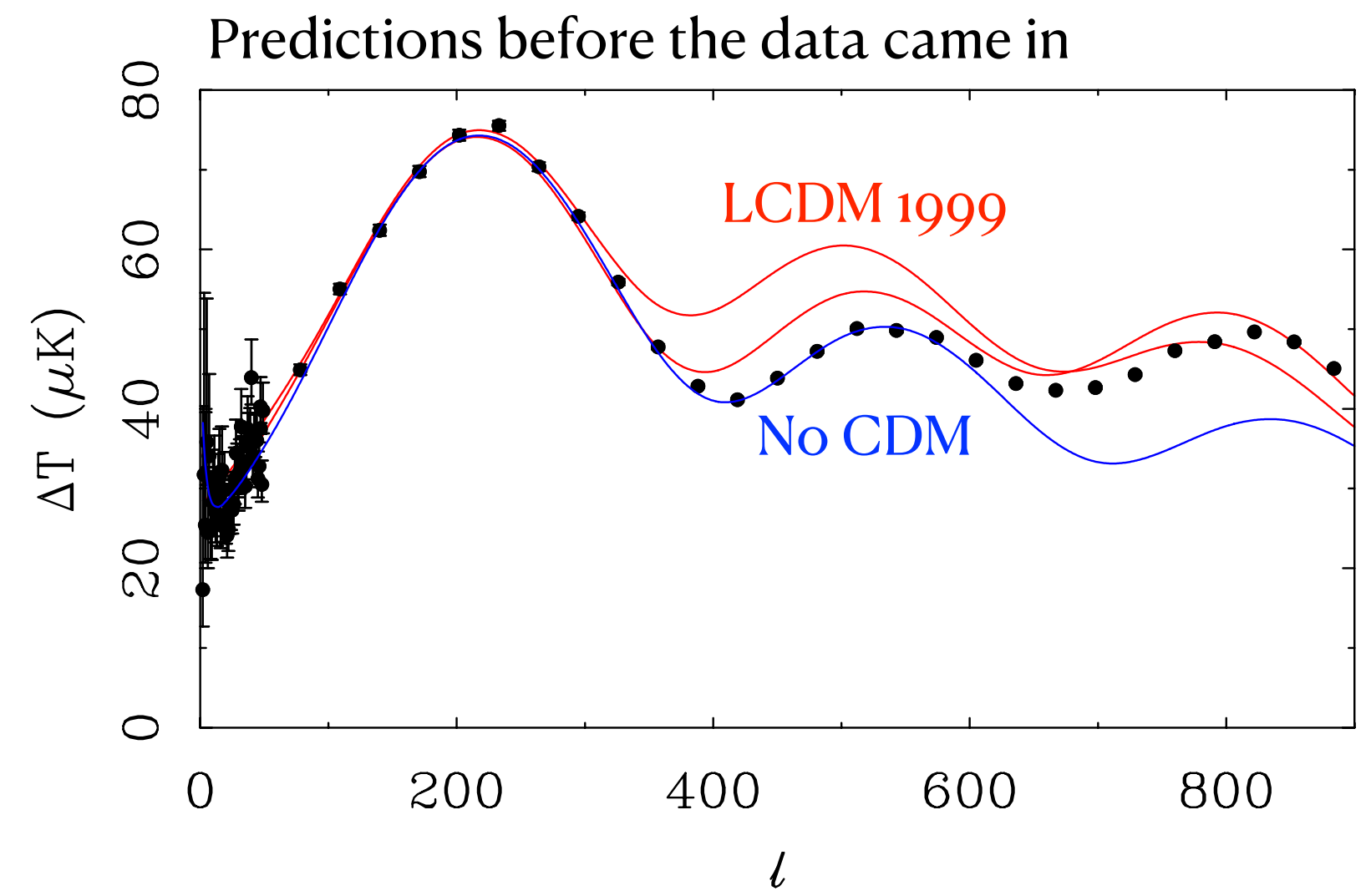
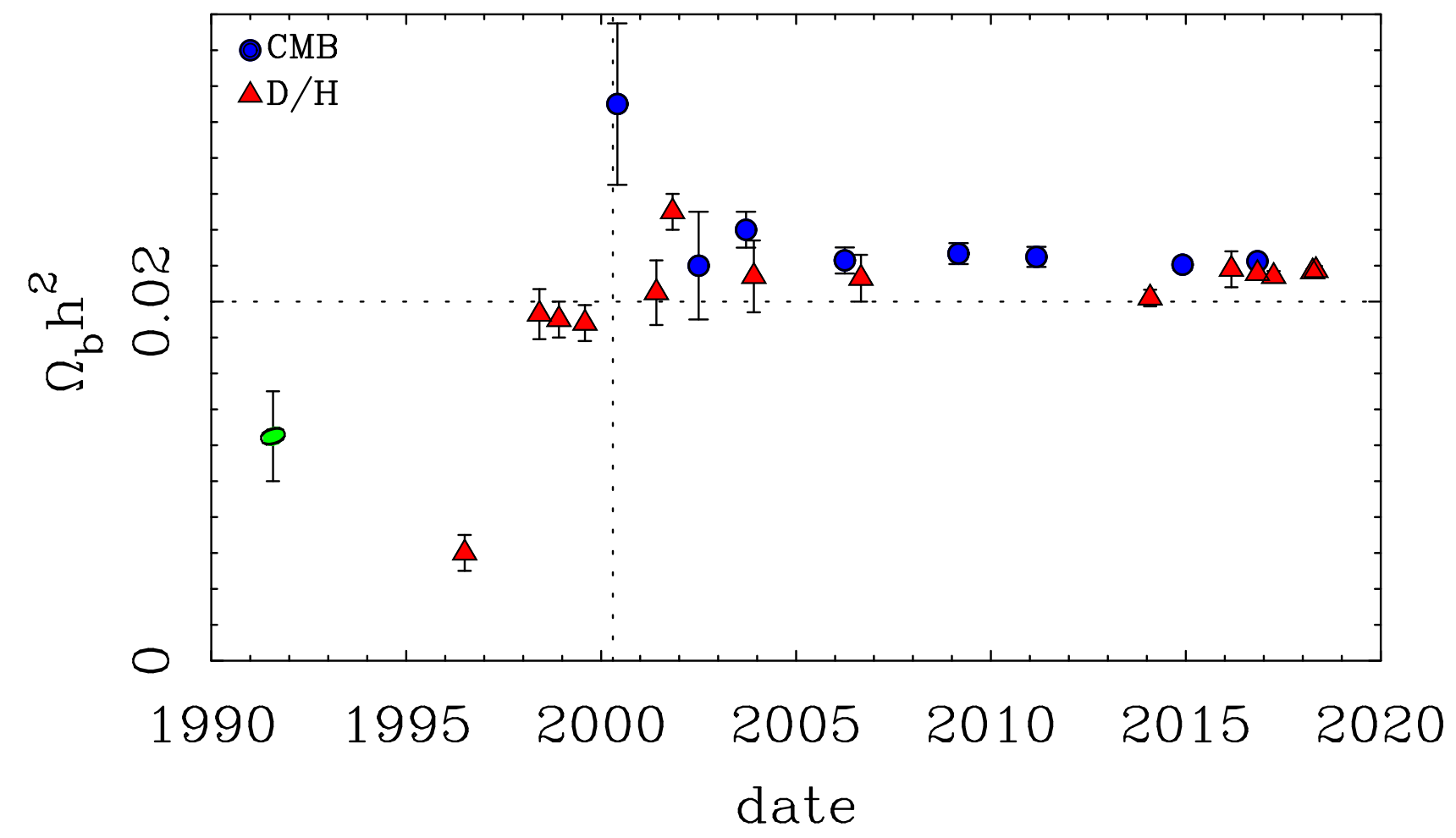


Damped and driven oscillator

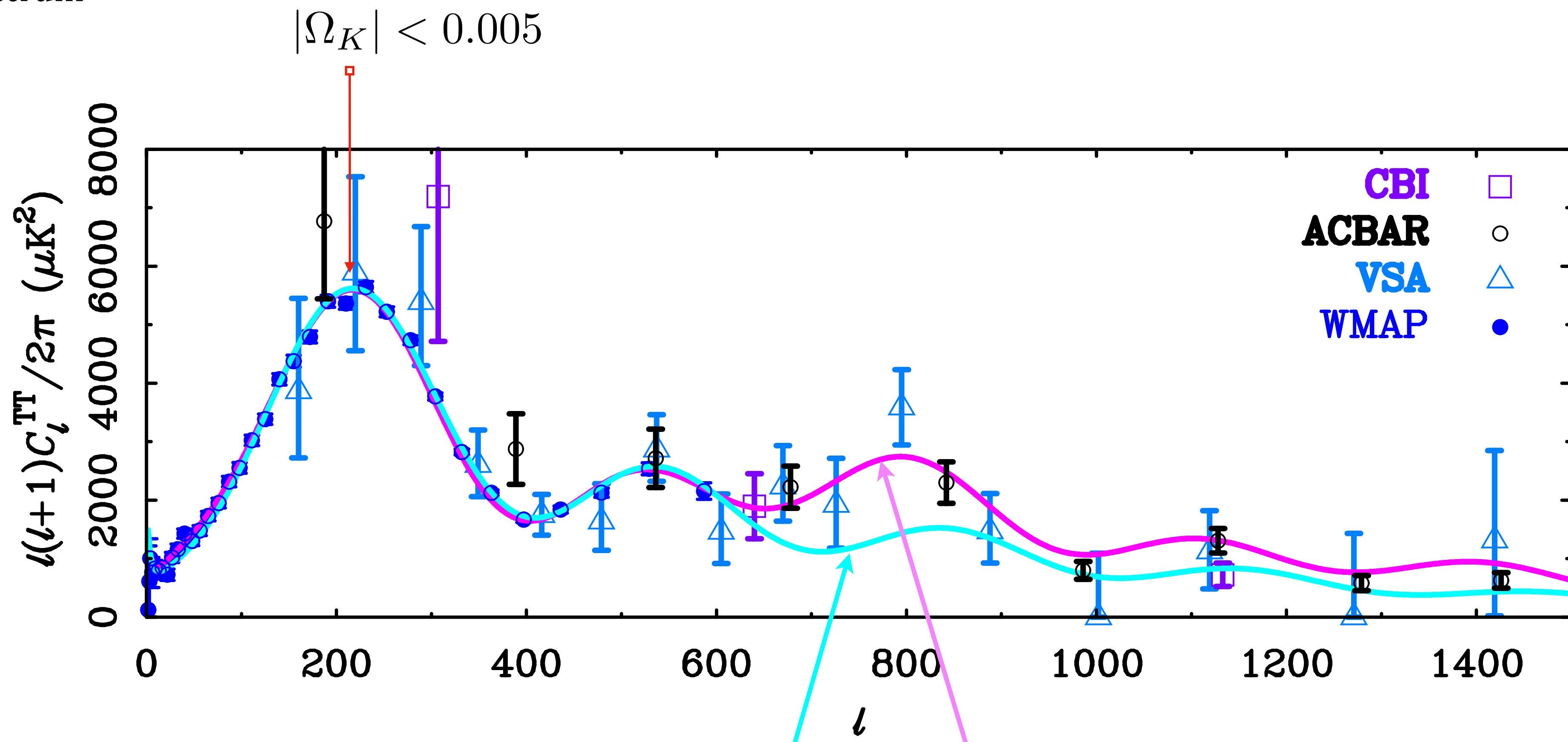
Baryons damp oscillations, like a kid dragging his feet on a swing.  
pure damping spectrum in limit of all baryons

Dark matter helps drive oscillations, like a parent pushing the kid.





# CMB power spectrum



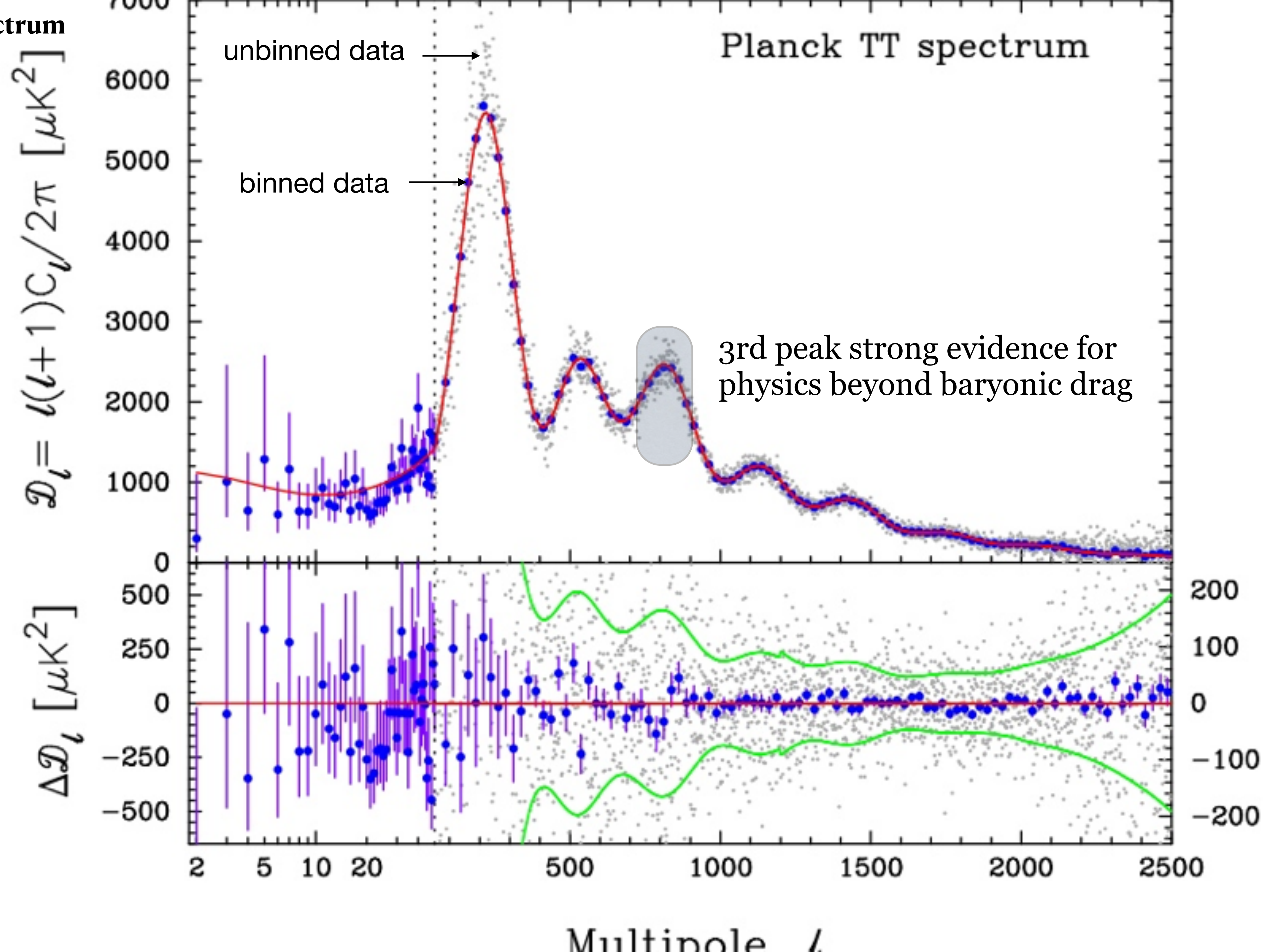
$$k^2\Phi = 4\pi G(\rho_b\delta_b + \rho_\gamma\delta_\gamma + \rho_{CDM}\delta_{CDM})$$

baryons a net drag

CDM a net forcing term



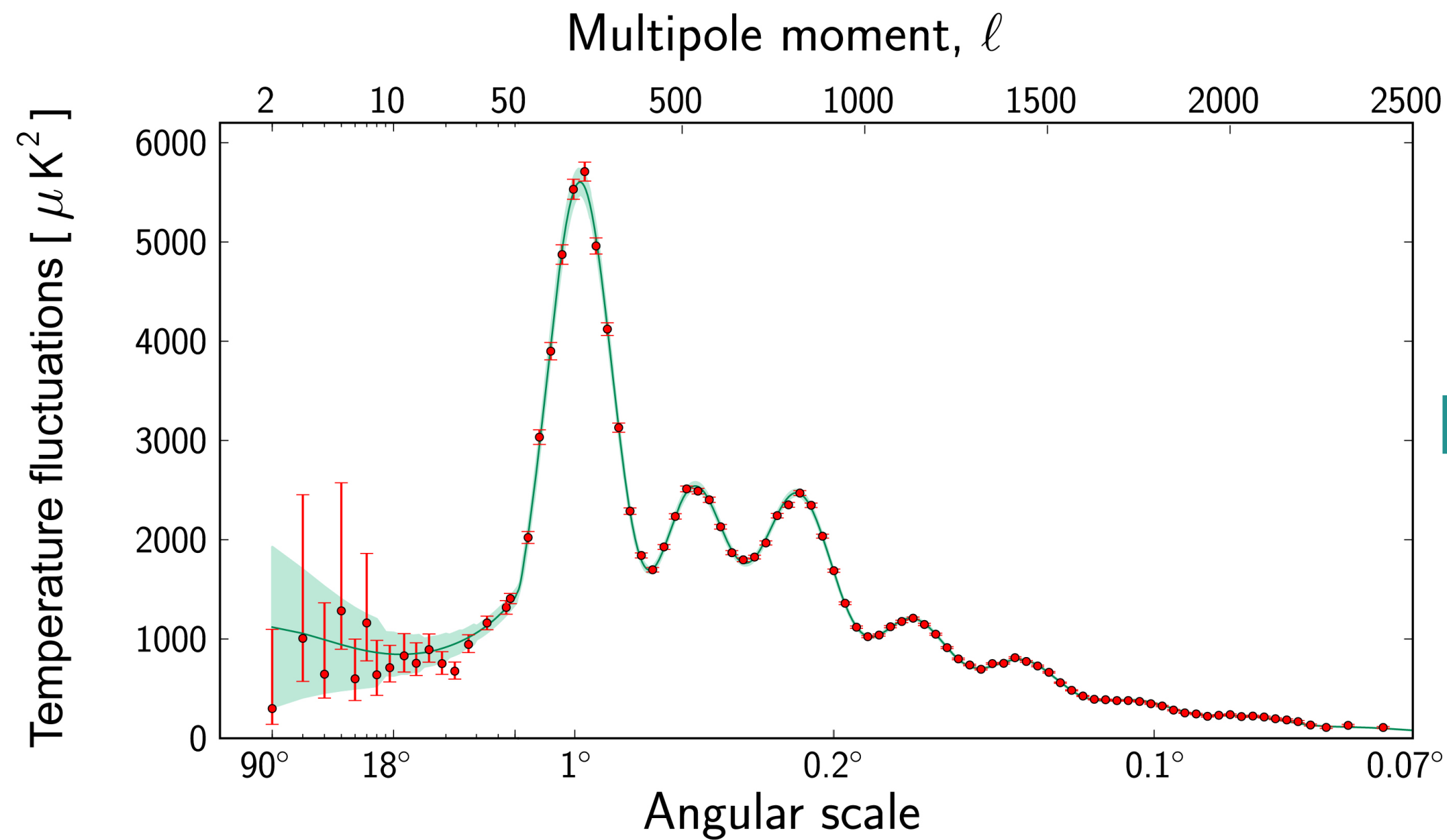
# CMB power spectrum





# CMB power spectrum

Detailed shape of the acoustic power spectrum depends sensitively on cosmic parameters.



Best-fit cosmology obtained from multi-parameter fit.  
Well constrained, but not unique - lots of parameter degeneracy.

## 2 Baseline model

### 2.1 base\_plikHM\_TT\_lowl\_lowE

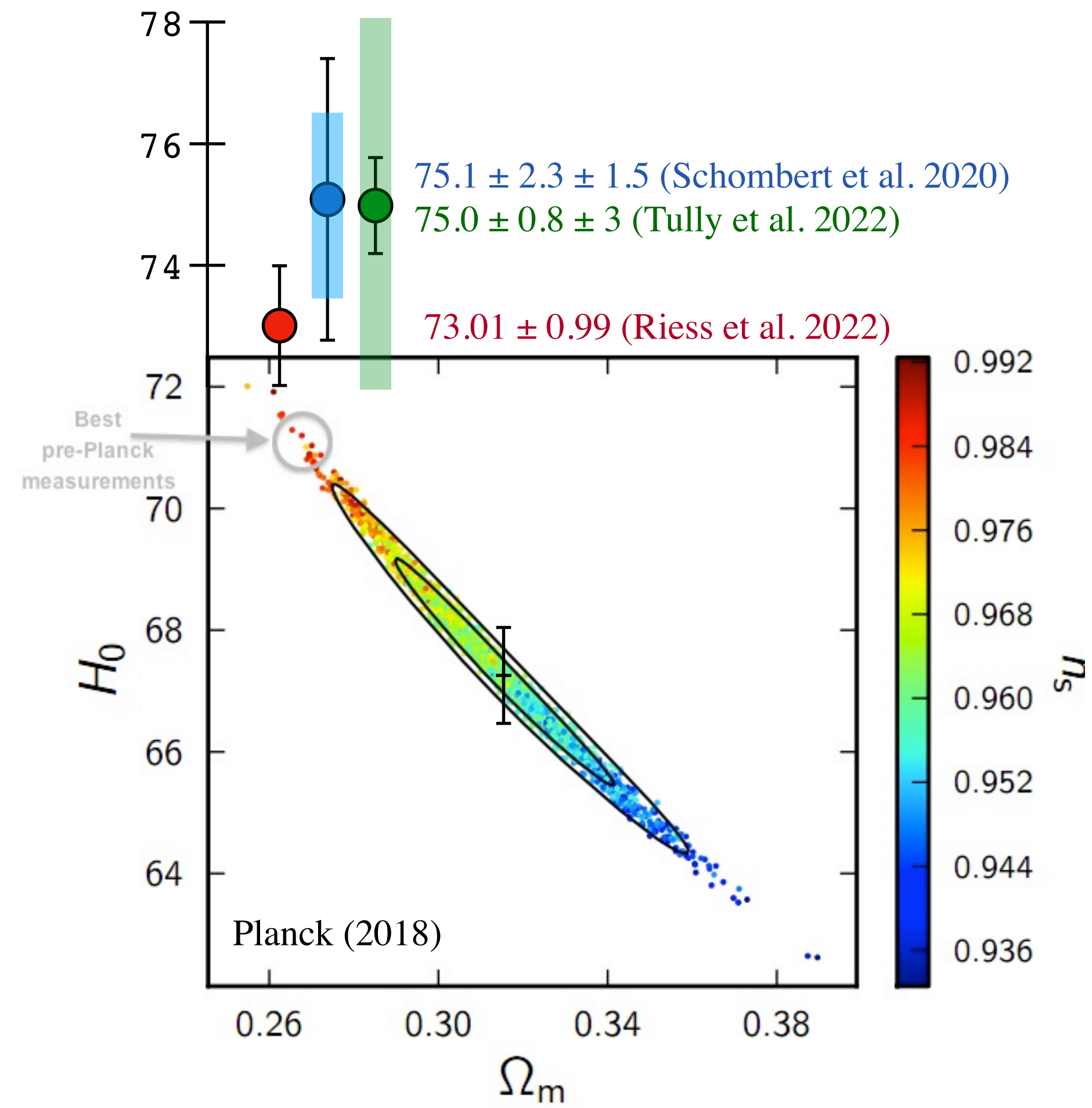
Parameter	Best fit	68% limits	Parameter	Best fit	68% limits	Parameter	Best fit	68% limits
$\Omega_b h^2$	0.022126	$0.02212 \pm 0.00022$	$\sigma_8 \Omega_m^{0.25}$	0.6116	$0.611 \pm 0.012$	$H(0.15)$	72.23	$72.25 \pm 0.78$
$\Omega_c h^2$	0.12068	$0.1206 \pm 0.0021$	$\sigma_8/h^{0.5}$	0.9938	$0.993 \pm 0.016$	$D_M(0.15)$	647.8	$647.7 \pm 7.9$
$100\theta_{MC}$	1.040748	$1.04077 \pm 0.00047$	$r_{drag} h$	98.40	$98.5 \pm 1.6$	$H(0.38)$	82.50	$82.52 \pm 0.56$
$\tau$	0.0523	$0.0522 \pm 0.0080$	$\langle d^2 \rangle^{1/2}$	2.4537	$2.454 \pm 0.038$	$D_M(0.38)$	1542.6	$1542 \pm 16$
$\ln(10^{10} A_s)$	3.0413	$3.040 \pm 0.016$	$z_{re}$	7.54	$7.50 \pm 0.82$	$H(0.51)$	89.310	$89.32 \pm 0.44$
$n_s$	0.9635	$0.9626 \pm 0.0057$	$10^9 A_s$	2.0933	$2.092 \pm 0.034$	$D_M(0.51)$	1996.8	$1997 \pm 18$
$y_{cal}$	1.00046	$1.0004 \pm 0.0025$	$10^9 A_s e^{-2\tau}$	1.8853	$1.884 \pm 0.014$	$H(0.61)$	94.998	$95.01 \pm 0.35$
$A_{217}^{CIB}$	48.5	$48 \pm 7$	$D_{40}$	1231.7	$1234 \pm 15$	$D_M(0.61)$	2322.3	$2322 \pm 20$
$\xi^{tSZ \times CIB}$	0.32	—	$D_{220}$	5710.4	$5713 \pm 42$	$H(2.33)$	236.75	$236.7 \pm 1.3$
$A_{143}^{tSZ}$	7.03	$5.1 \pm 2.0$	$D_{810}$	2538.2	$2536 \pm 14$	$D_M(2.33)$	5777.8	$5778 \pm 16$
$A_{100}^{PS}$	254.9	$263 \pm 28$	$D_{1420}$	815.5	$814.4 \pm 5.1$	$f\sigma_8(0.15)$	0.4642	$0.464 \pm 0.012$
$A_{143}^{PS}$	49.8	$49 \pm 8$	$D_{2000}$	229.94	$229.5 \pm 1.8$	$\sigma_8(0.15)$	0.7500	$0.7492 \pm 0.0075$
$A_{143 \times 217}^{PS}$	47.3	$44 \pm 9$	$n_{s,0.002}$	0.9635	$0.9626 \pm 0.0057$	$f\sigma_8(0.38)$	0.4804	$0.4798 \pm 0.0095$
$A_{217}^{PS}$	119.9	$115 \pm 10$	$Y_P$	0.245295	$0.24529^{+0.00011}_{-0.000088}$	$\sigma_8(0.38)$	0.6638	$0.6631 \pm 0.0060$
$A^{kSZ}$	0.00	$< 4.84$	$Y_P^{BBN}$	0.246621	$0.24661^{+0.00011}_{-0.000089}$	$f\sigma_8(0.51)$	0.4779	$0.4773 \pm 0.0082$
$A_{100}^{dustTT}$	8.86	$8.9 \pm 1.8$	$10^5 D/H$	2.6321	$2.634 \pm 0.042$	$\sigma_8(0.51)$	0.6208	$0.6202 \pm 0.0055$
$A_{143}^{dustTT}$	10.80	$10.7 \pm 1.8$	Age/Gyr	13.8300	$13.830 \pm 0.037$	$f\sigma_8(0.61)$	0.4722	$0.4716 \pm 0.0072$
$A_{143 \times 217}^{dustTT}$	19.43	$18.3 \pm 3.3$	$z_*$	1090.292	$1090.30 \pm 0.41$	$\sigma_8(0.61)$	0.5904	$0.5899 \pm 0.0051$
$A_{217}^{dustTT}$	94.8	$93.3 \pm 7.4$	$r_*$	144.442	$144.46 \pm 0.48$	$f\sigma_8(2.33)$	0.29733	$0.2971 \pm 0.0025$
$c_{100}$	0.99965	$0.99961 \pm 0.00061$	$100\theta_*$	1.040956	$1.04097 \pm 0.00046$	$\sigma_8(2.33)$	0.30613	$0.3059 \pm 0.0027$
$c_{217}$	0.99825	$0.99826 \pm 0.00063$	$D_M(z_*)/\text{Gpc}$	13.8759	$13.878 \pm 0.044$	$f_{2000}^{143}$	30.49	$31.2 \pm 3.0$
$H_0$	66.86	$66.88 \pm 0.92$	$z_{drag}$	1059.437	$1059.39 \pm 0.46$	$f_{2000}^{143 \times 217}$	33.34	$33.6 \pm 2.0$
$\Omega_\Lambda$	0.6791	$0.679 \pm 0.013$	$r_{drag}$	147.182	$147.21 \pm 0.48$	$f_{2000}^{217}$	107.77	$108.2 \pm 1.9$
$\Omega_m$	0.3209	$0.321 \pm 0.013$	$k_D$	0.14058	$0.14054 \pm 0.00052$	$\chi_{small}^2$	395.88	$397.0 \pm 1.7$
$\Omega_m h^2$	0.14345	$0.1434 \pm 0.0020$	$100\theta_D$	0.161051	$0.16107 \pm 0.00027$	$\chi_{lowl}^2$	23.60	$23.9 \pm 1.3$
$\Omega_m h^3$	0.095909	$0.09589 \pm 0.00046$	$z_{eq}$	3412.7	$3411 \pm 48$	$\chi_{plik}^2$	758.7	$771.4 \pm 5.5$
$\sigma_8$	0.8126	$0.8118 \pm 0.0089$	$k_{eq}$	0.010416	$0.01041 \pm 0.00014$	$\chi_{prior}^2$	1.35	$7.3 \pm 3.7$
$S_8$	0.8405	$0.840 \pm 0.024$	$100\theta_{eq}$	0.8106	$0.8109 \pm 0.0089$	$\chi_{CMB}^2$	1178.2	$1192.3 \pm 5.5$
$\sigma_8 \Omega_m^{0.5}$	0.4604	$0.460 \pm 0.013$	$100\theta_{s,eq}$	0.44817	$0.4483 \pm 0.0046$			

Best-fit  $\chi_{eff}^2 = 1179.58$ ;  $\tilde{\chi}_{eff}^2 = 1199.58$ ;  $R - 1 = 0.00927$

$\chi_{eff}^2$ : CMB - small\_100x143\_offlike5\_EE\_Aplanck\_B: 395.88 commander\_dx12\_v3.2.29: 23.60 plik\_rd12\_HM\_v22\_TT: 758.75

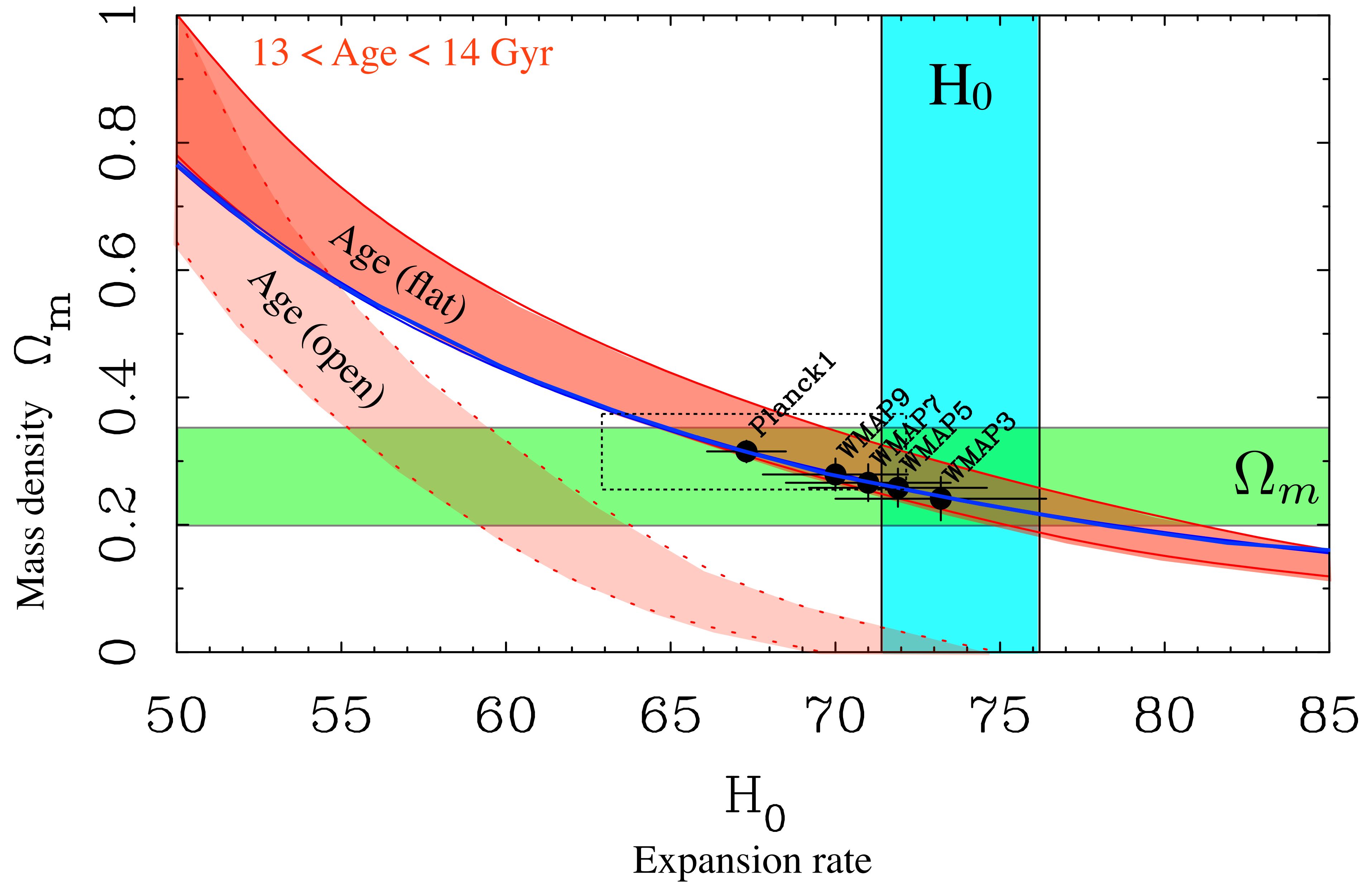


### Hubble constant tension



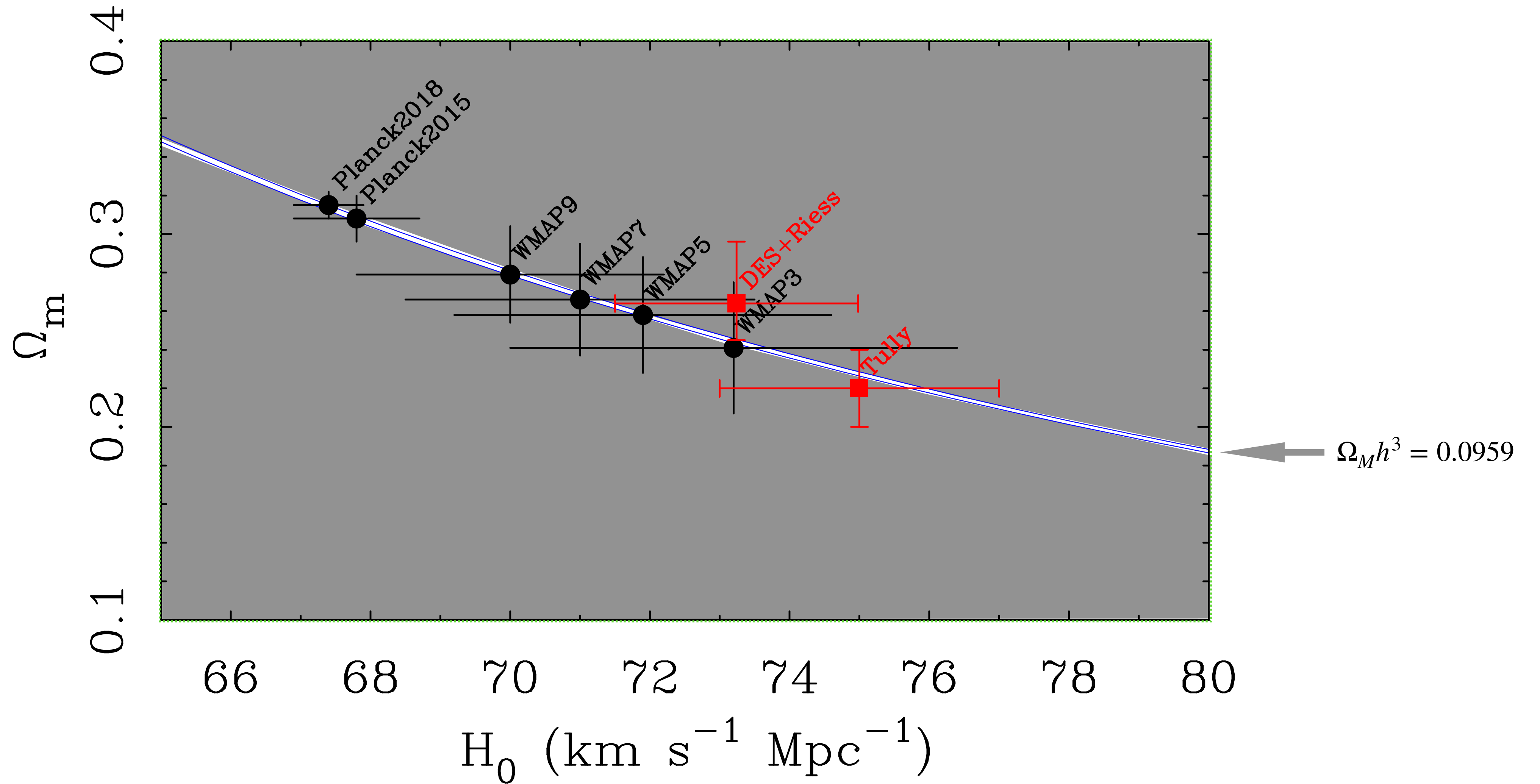


Planck constraint:  $\Omega_m h^3 = 0.0959 \pm 0.0006$



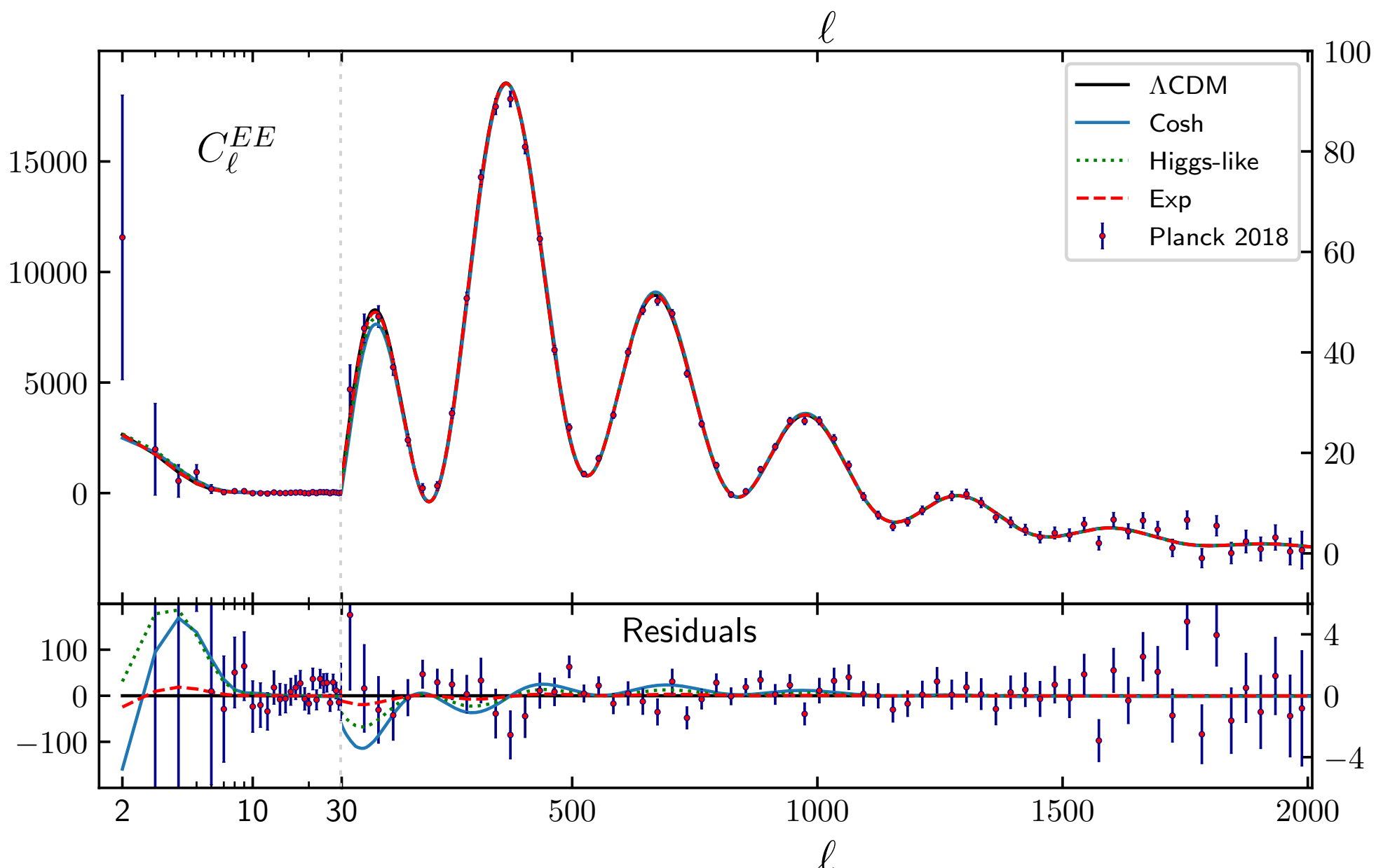
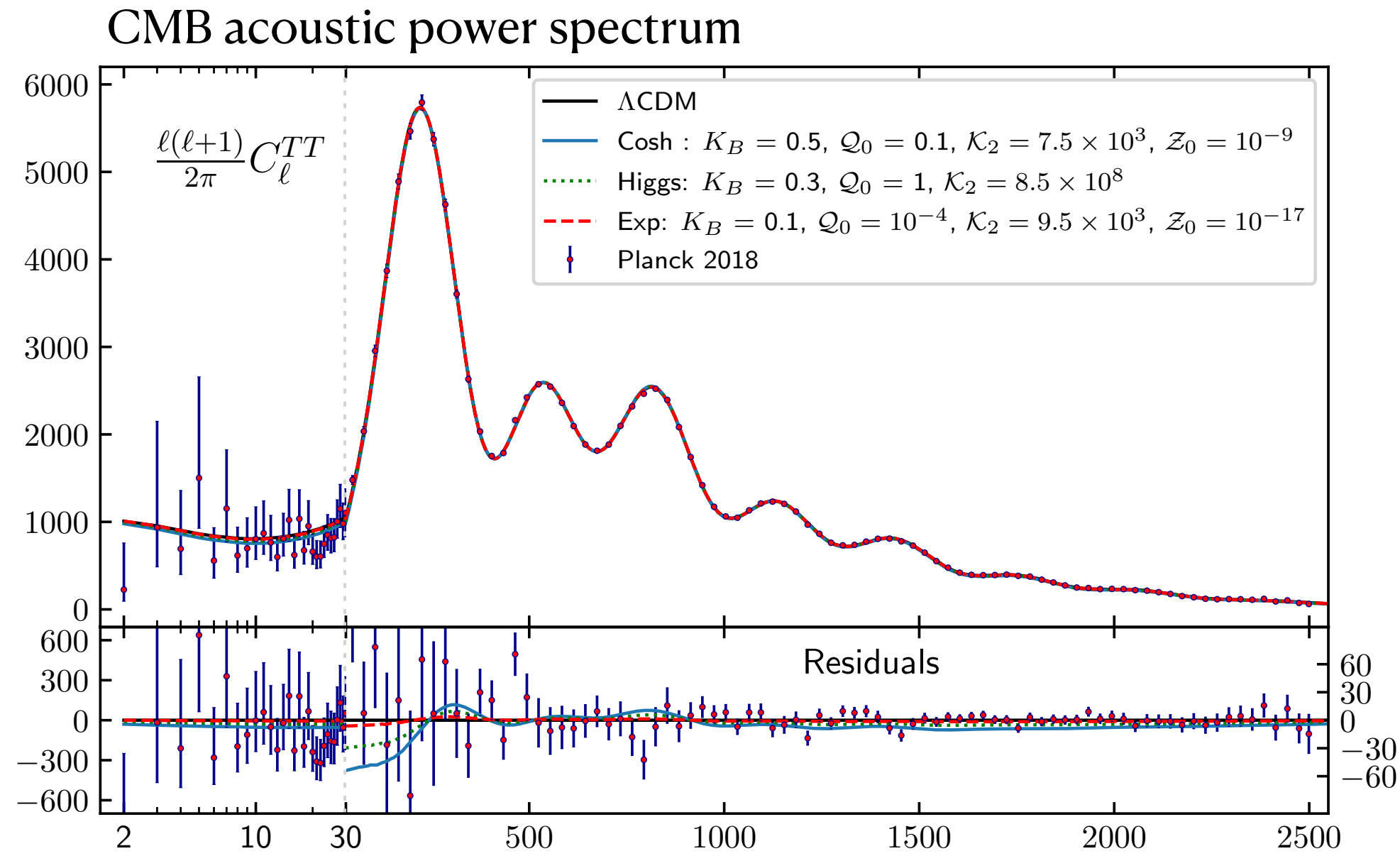


# Cosmology today: tension in $H_0$ ...and $\Omega_m$



The CMB best fits have marched away from the original concordance region



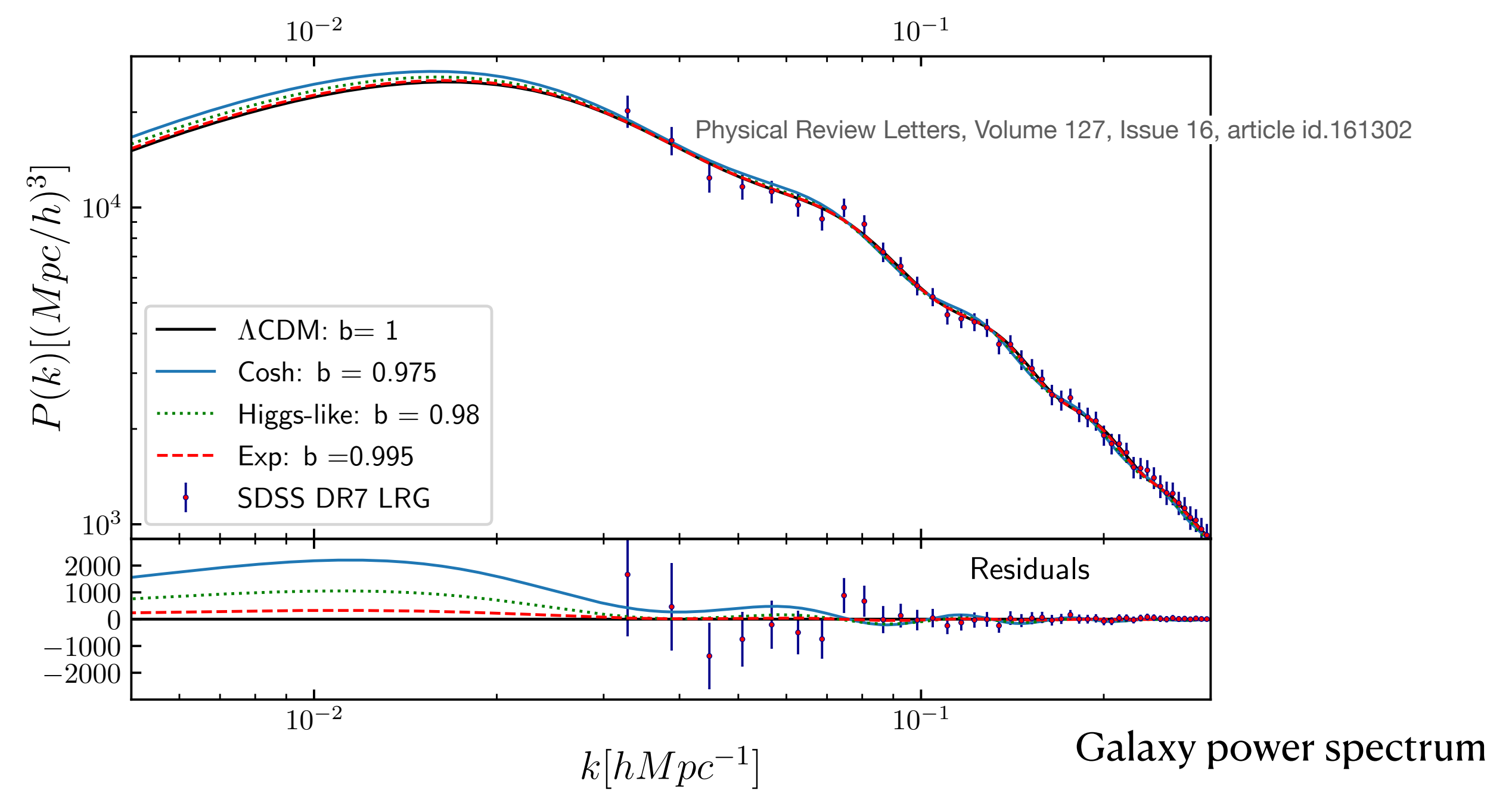


3rd peak strong evidence for physics beyond baryonic drag.

This is usually interpreted to require the existence of non-baryonic cold dark matter, which Planck requires at over  $50 \sigma$ :

$$\Omega_{\text{CDM}} h^2 = 0.1206 \pm 0.0021$$

However, the interpretation remains ambiguous - could also be a modification of gravity (e.g., RMOND gives an identical power spectrum.) (Skordis & Zlosnik 2021, PRL, 127, 161302)





*“Cosmologists are often wrong, but never in doubt”*

- Lev Landau

**Cosmological parameters by decade**

Quantity	“Standard CDM” SCDM 1988	“Concordance model” LCDM 1995	WMAP5 2008	Planck 2018
$\Omega_m$	1	0.35	0.258±0.027	0.315 ± 0.007
$\Omega_\Lambda$	0	0.65	0.742	0.696 ± 0.009
$\Omega_b h^2$	0.0125 ±0.0025	0.015 0.009 - 0.020 “reasonable range”	0.02273 ±0.00062	0.0224 ±0.0001
$H_o$	50	65	71.9±2.7	67.4 ± 0.5
dark matter	CDM	CDM	CDM	CDM