

# DARK MATTER

ASTR 333/433

FALL 2013

MoTu 4:00-5:15PM

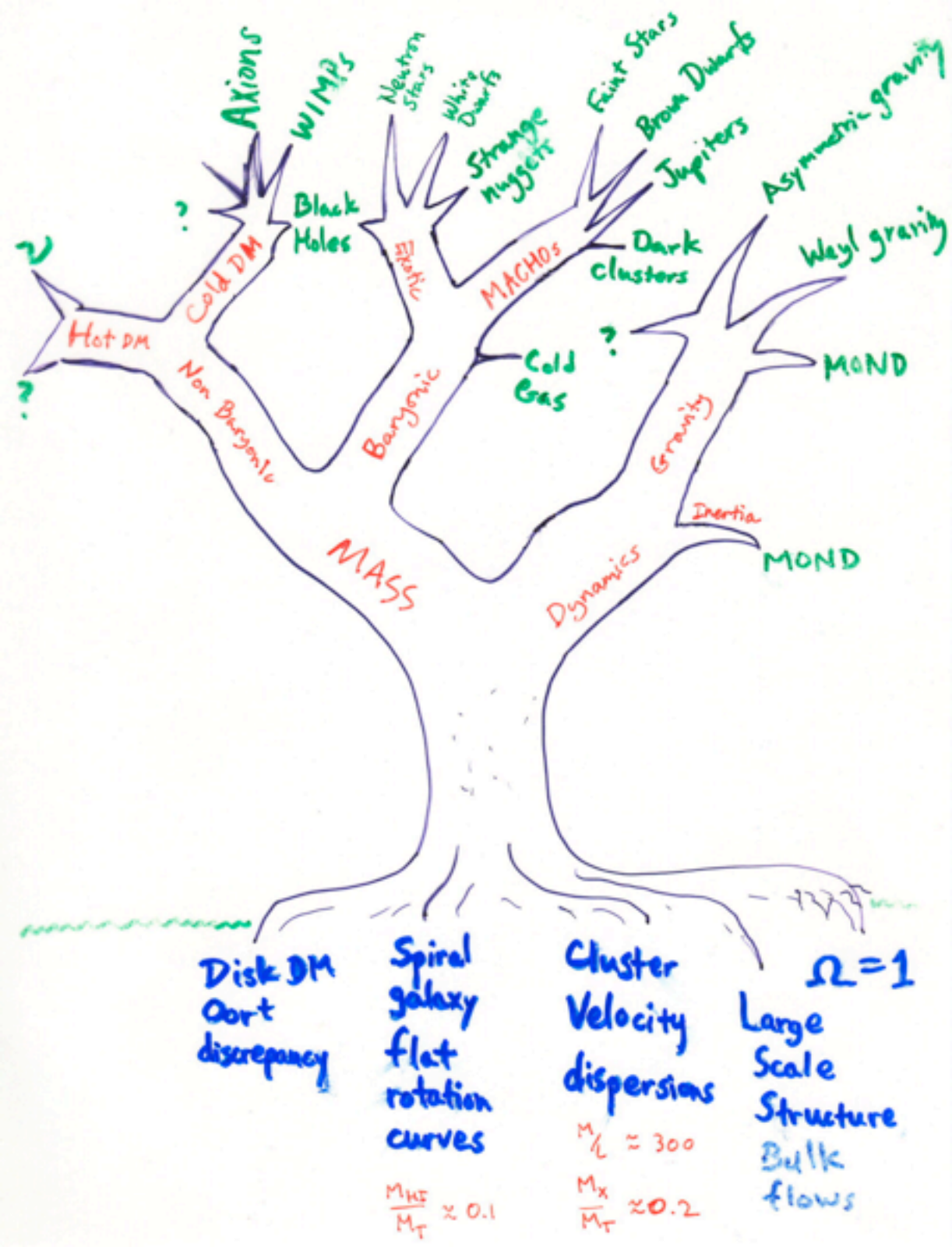
SEARS 552

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368-1808

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CASE WESTERN RESERVE  
UNIVERSITY EST. 1826

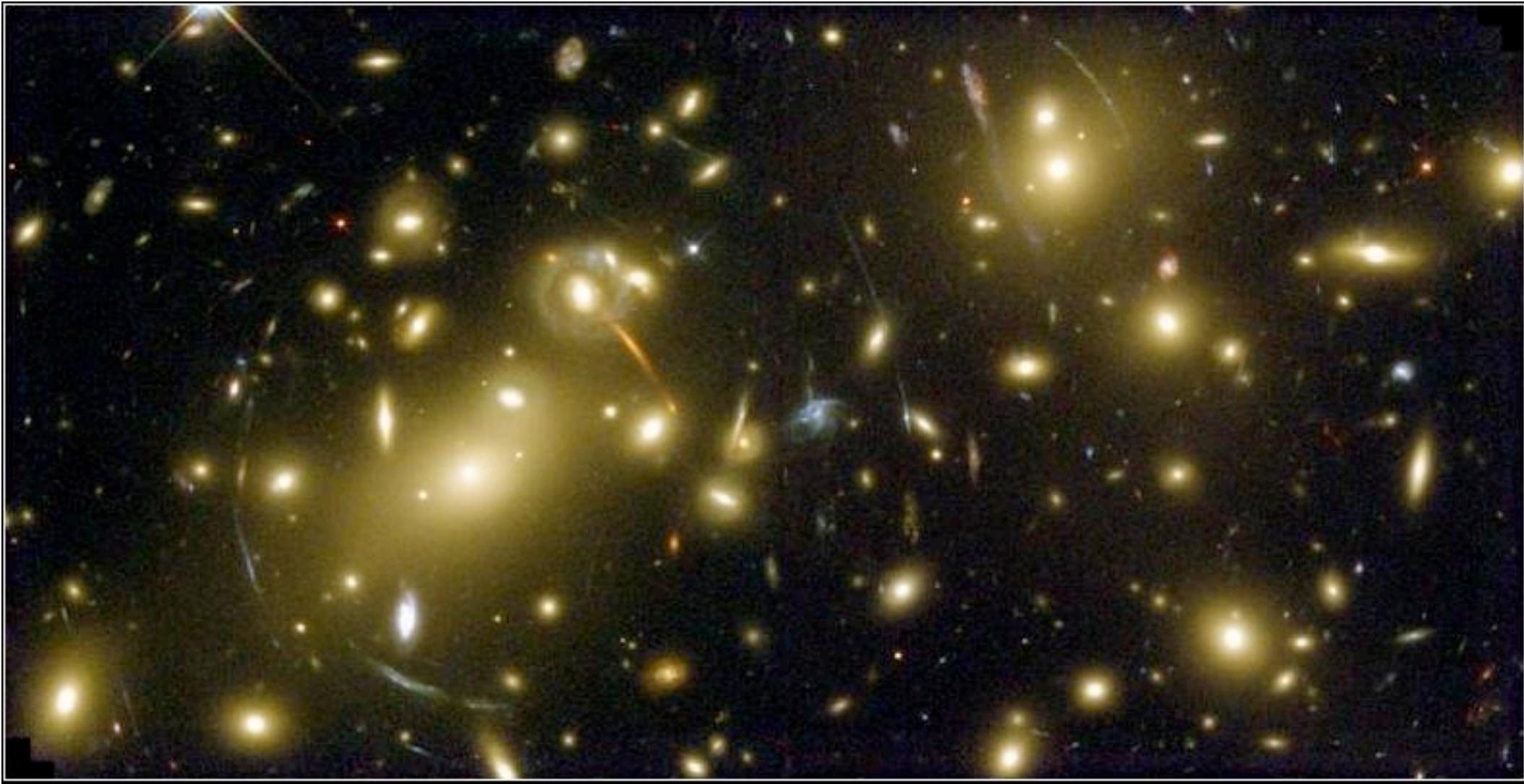
# Logistics:

- Homework 3 due tomorrow
- Abstracts for 433 talks due 11/26
- 433 talks 12/2 & 12/3
- Homework 4 due 12/3
- Review 12/9
- Final 12/11 (9 AM)

Today: cluster masses from

- X-ray gas
- S-Z effect

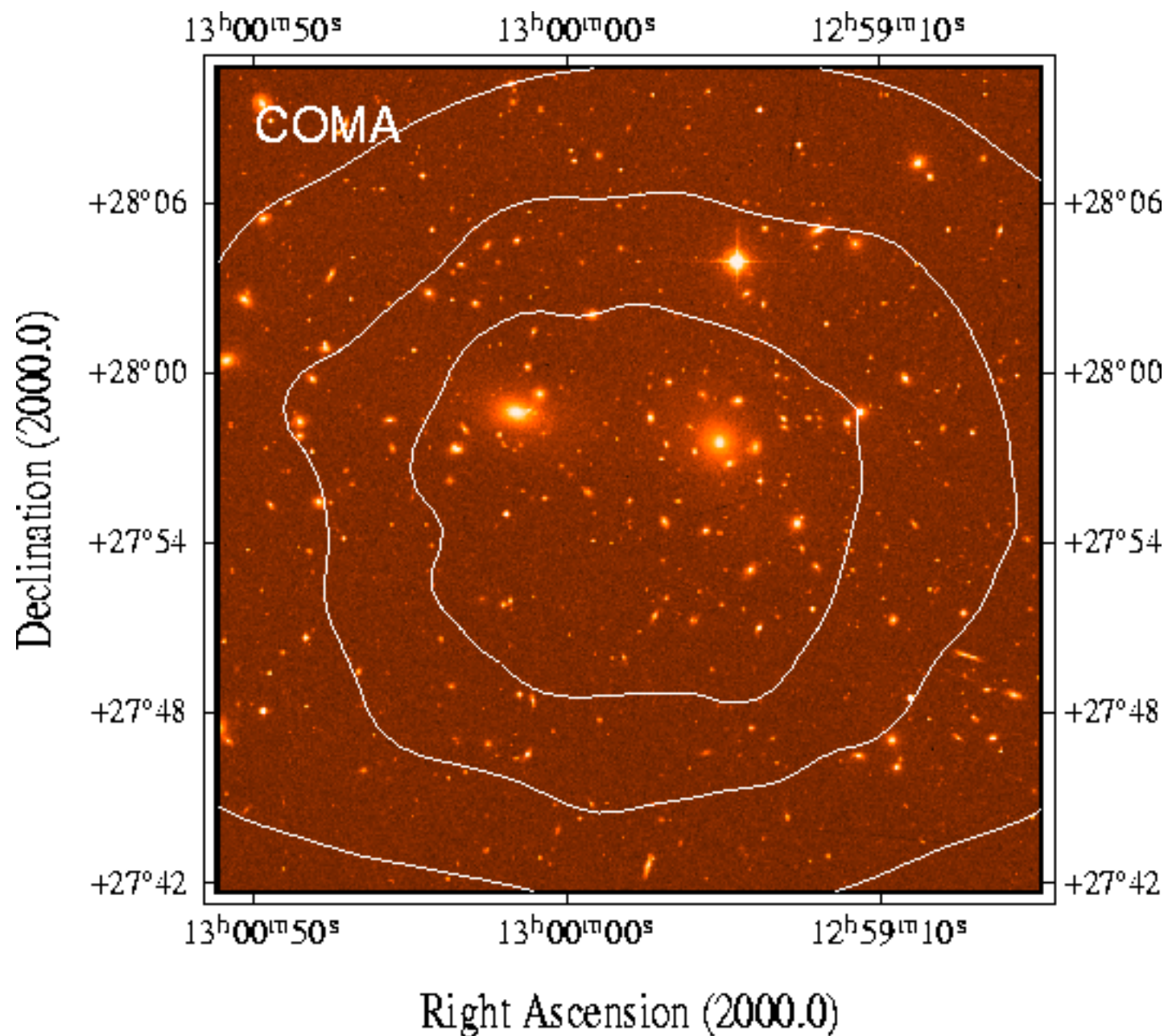
# Galaxy Clusters



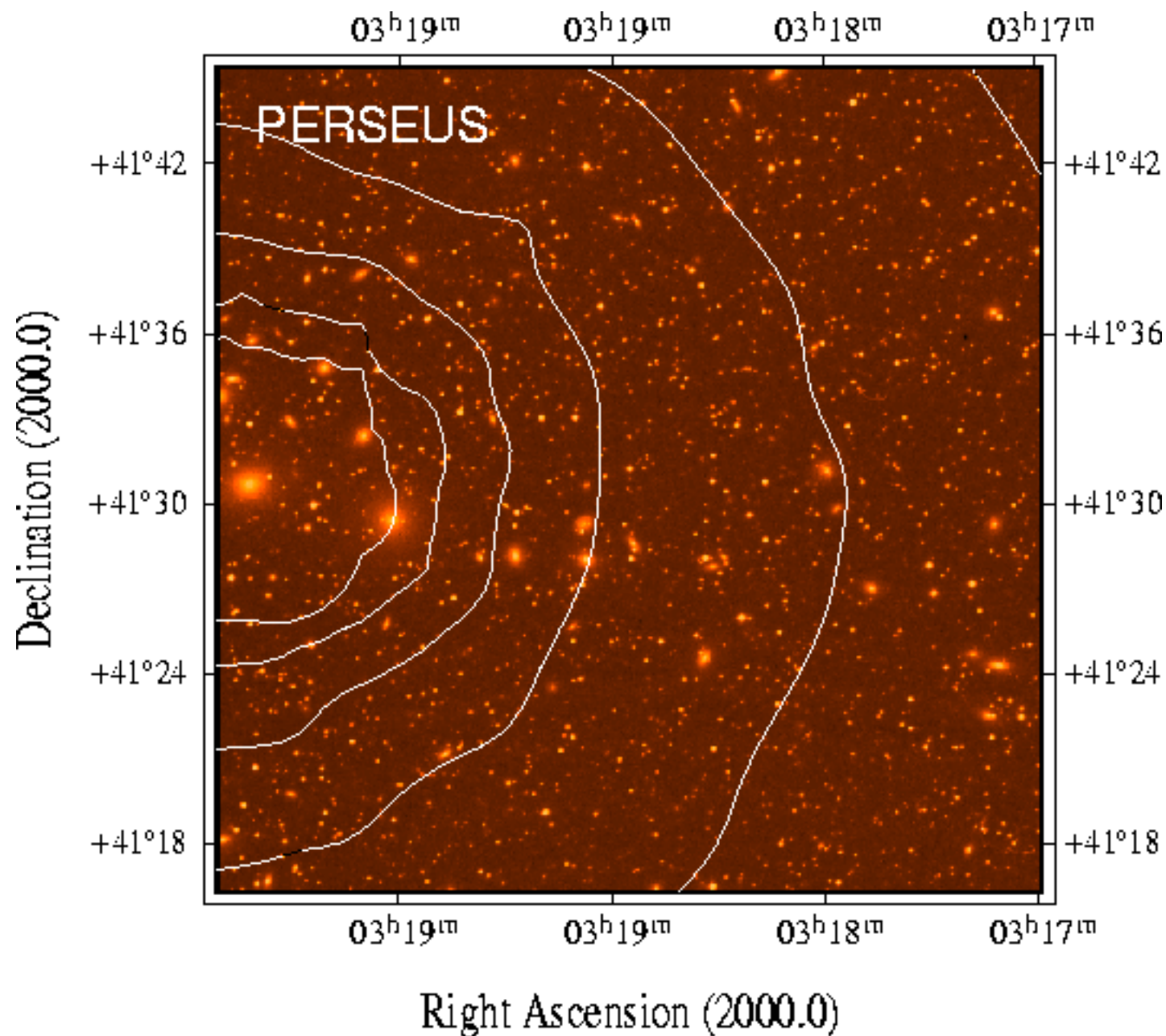
4 distinct measures: velocity dispersion, gravitational lensing, hydrostatic equilibrium of X-ray gas, and the Sunyaev-Zel'dovich effect



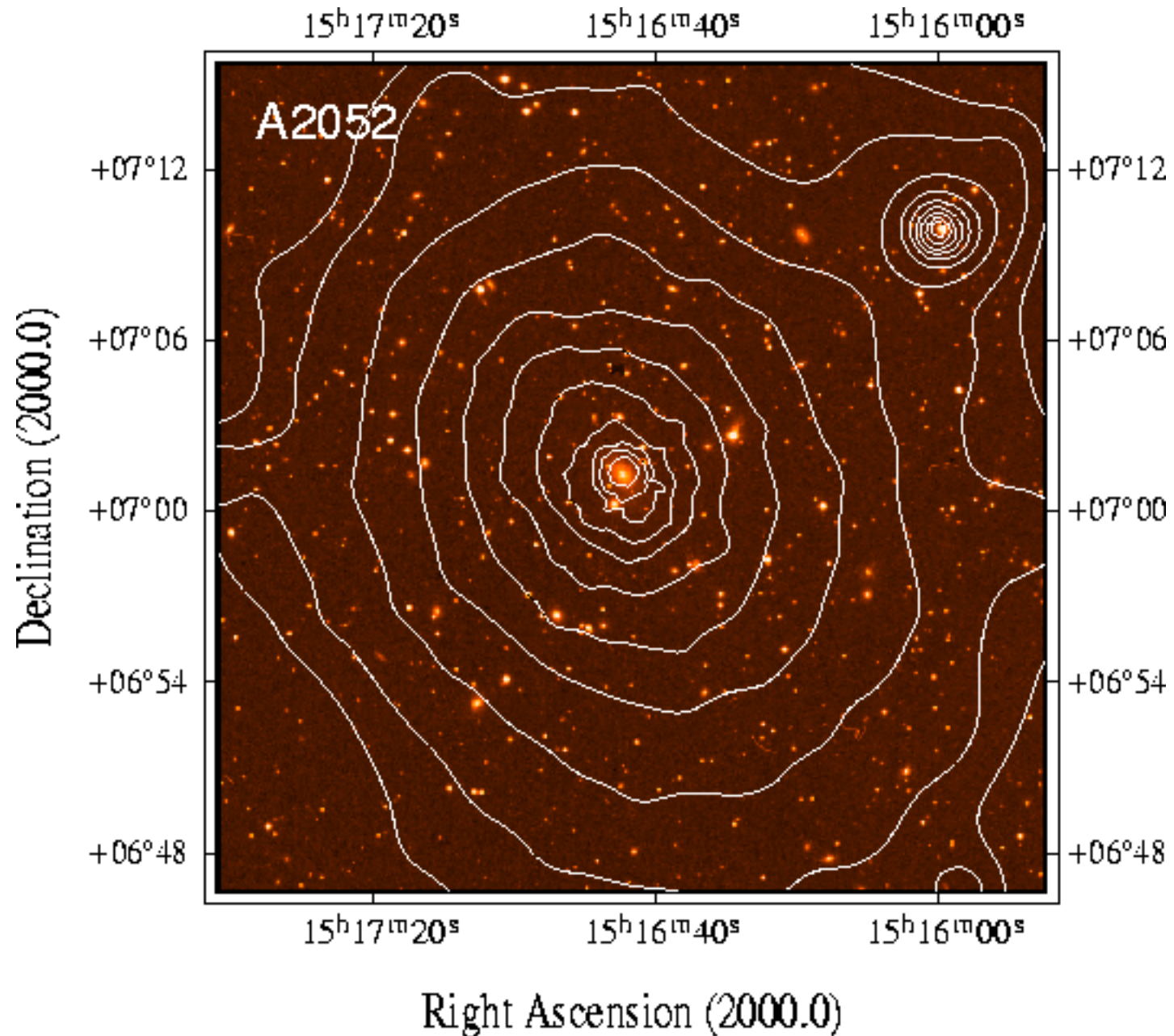
# Clusters in optical and X-ray (contours)



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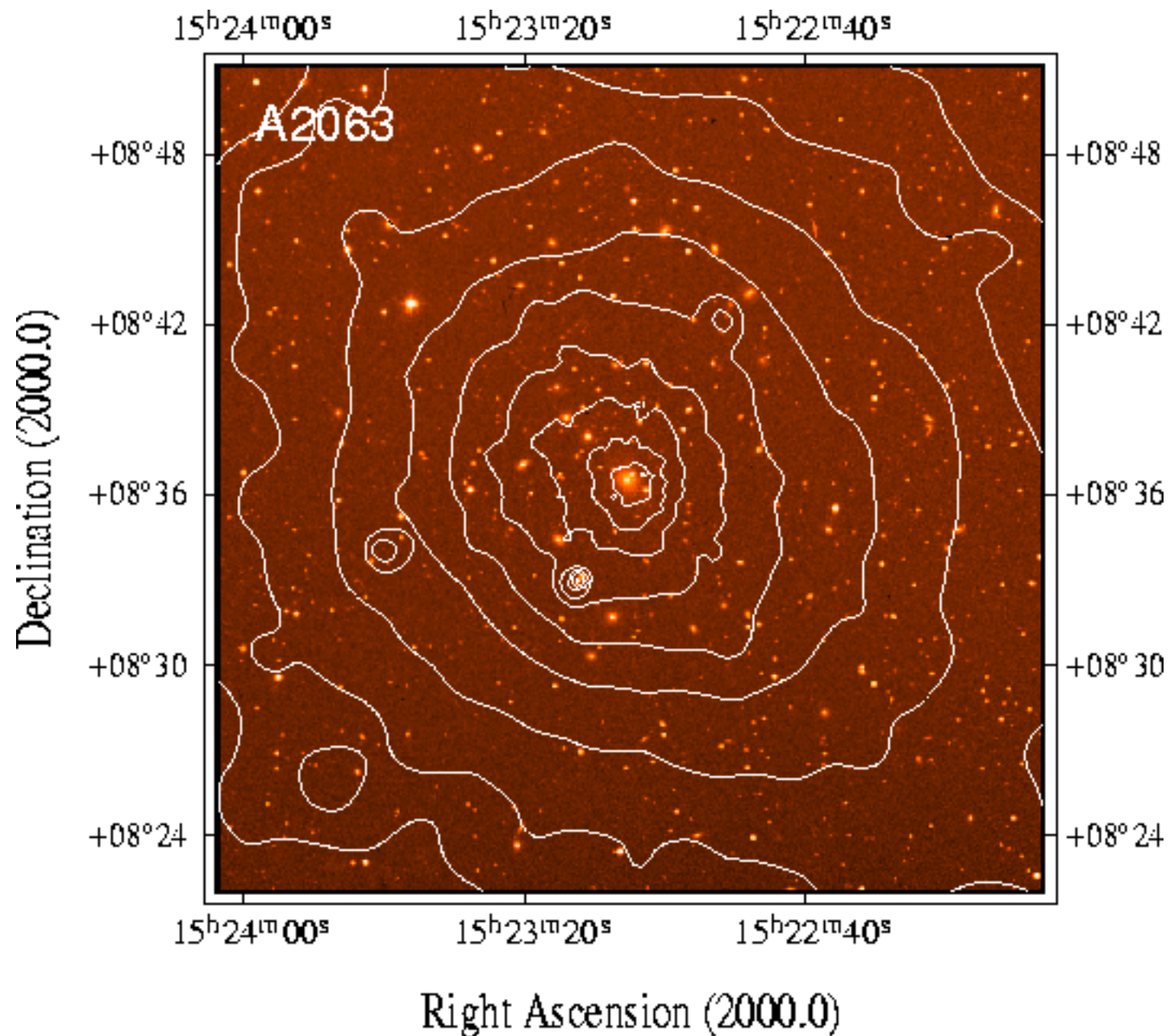


# Clusters in optical and X-ray (contours)

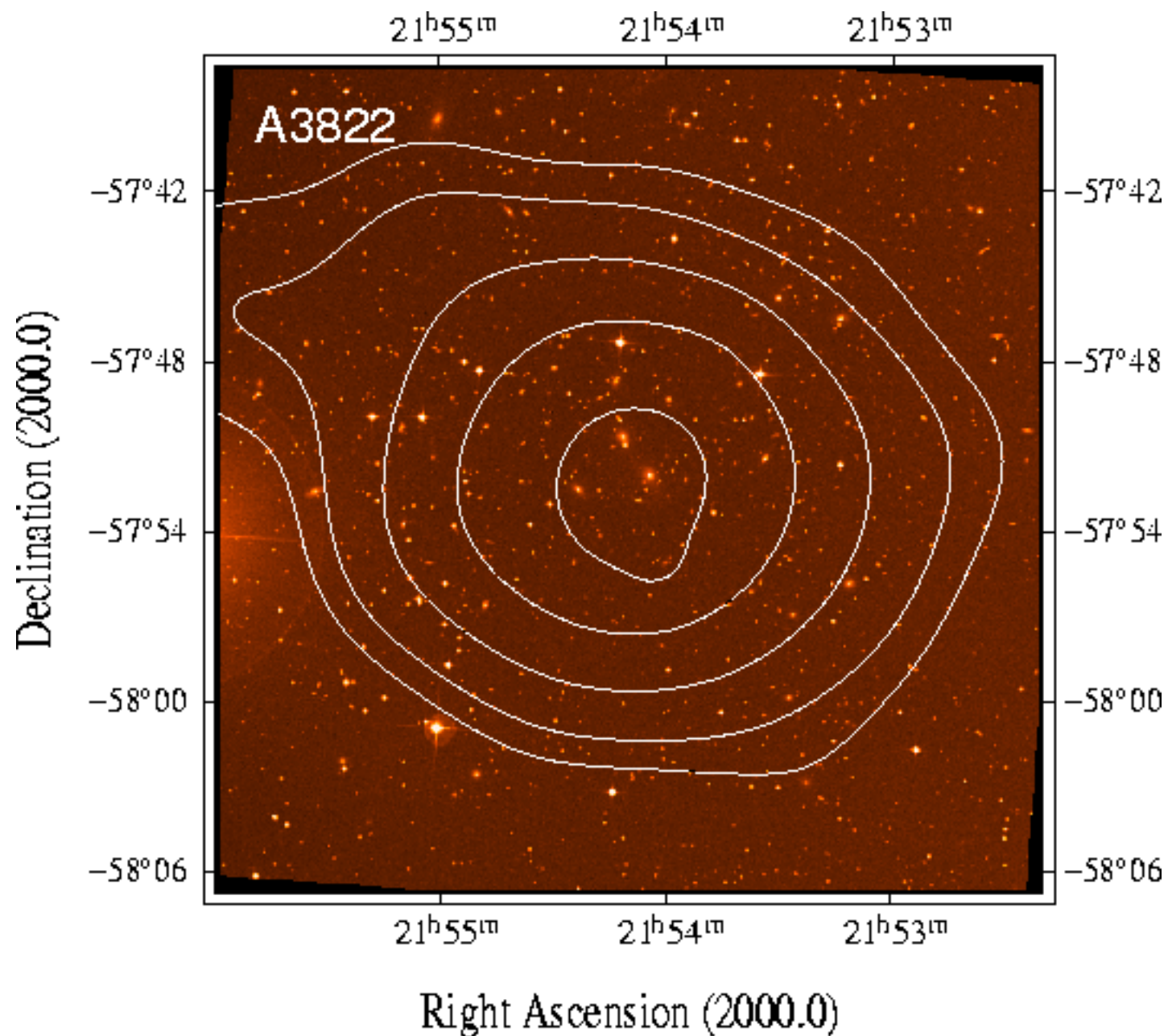




# Clusters in optical and X-ray (contours)



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Reiprich ApJ, 567, 716-740 (2002)

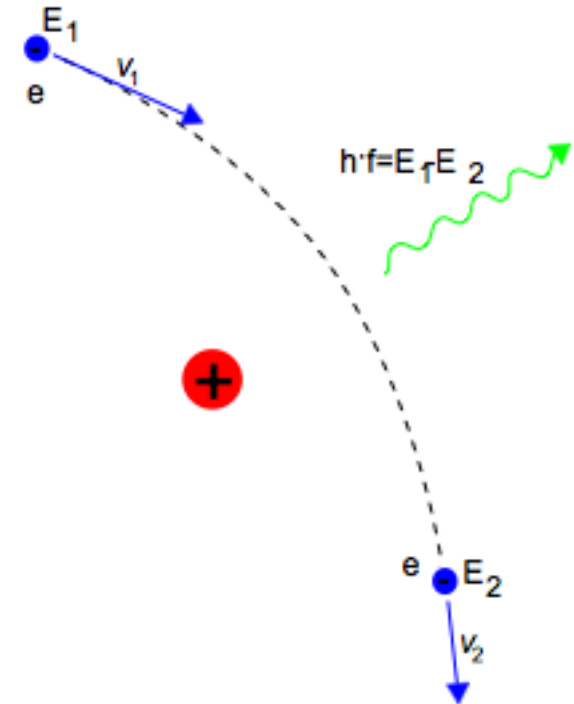


# Bremsstrahlung

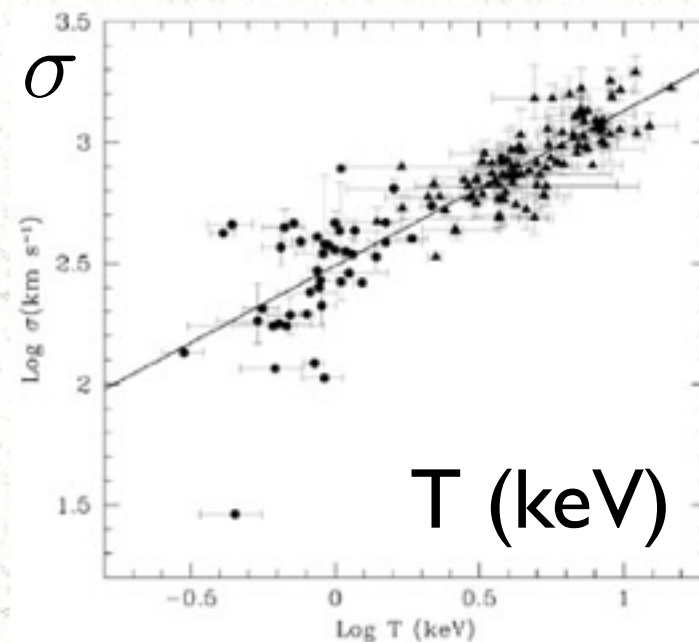
Gas falling into clusters shock heats to the virial temperature of the potential,  $kT \sim mV^2$  resulting in an intracluster medium (ICM) composed of hot plasma. This plasma radiates in X-rays via Bremsstrahlung (braking radiation).

[Sometimes also called free-free radiation]

Just classical radiation from accelerated charges.



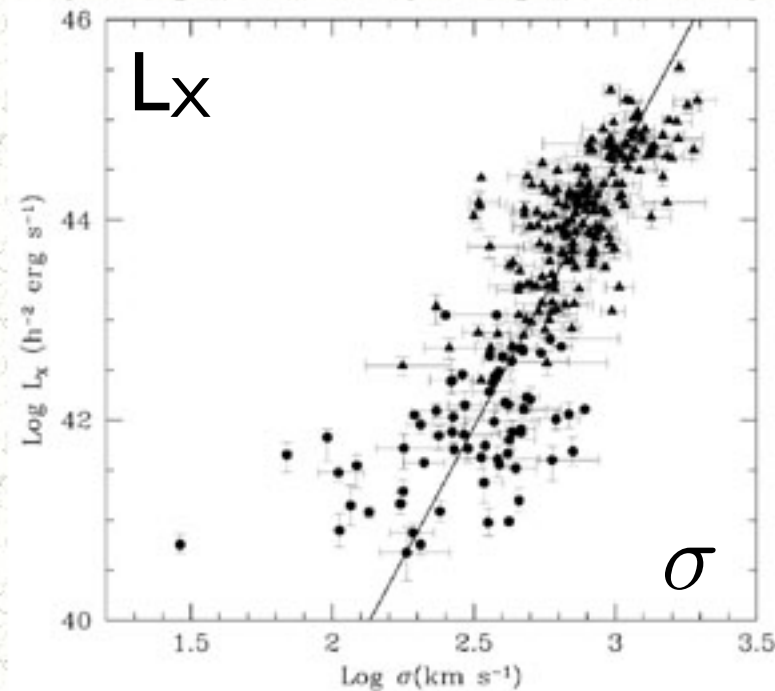
# Global correlations in galaxy clusters



**Figure 4.** Logarithm of the X-ray temperature versus logarithm of optical velocity dispersion for a sample of groups (circles) and clusters (triangles). The group data are taken from the literature compilation of [Xue & Wu \(2000\)](#), with the addition of the groups in [Helsdon & Ponman \(2000\)](#). The cluster data are taken from [Wu et al \(1999\)](#). The solid line represents the best-fit found by [Wu et al \(1999\)](#) for the clusters sample (using an orthogonal distance regression method). Within the large scatter, the groups are consistent with the cluster relationship.



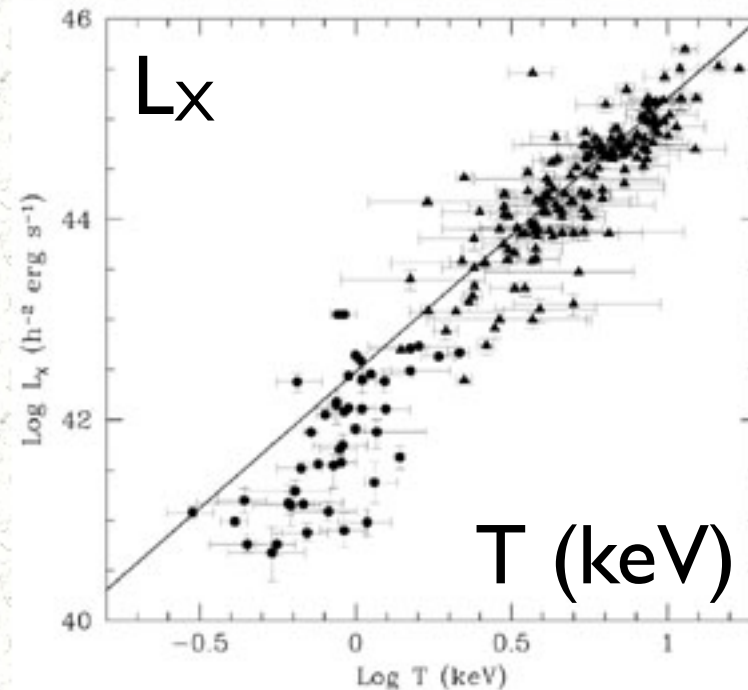
# Global correlations in galaxy clusters



**Figure 5.** Logarithm of optical velocity dispersion versus logarithm of X-ray luminosity for a sample of groups (circles) and clusters (triangles). The data are taken from the same sources cited in [Figure 4](#). The solid line represents the best-fit found by [Wu et al \(1999\)](#) for the clusters sample (using an orthogonal distance regression method).



# Global correlations in galaxy clusters



**Figure 6.** Logarithm of the X-ray temperature versus logarithm of X-ray luminosity for a sample of groups (circles) and clusters (triangles). The data are taken from the same sources cited in [Figure 4](#). The solid line represents the best-fit found by [Wu et al \(1999\)](#) for the clusters sample (using an orthogonal distance regression method). The observed relationship for groups is somewhat steeper than the best-fit cluster relationship.

## Beta models

The X-ray surface brightness at a projected radius  $R$   
for an isothermal sphere is given by:

$$S(R) = S_0 [1 + (R/r_c)^2]^{-3\beta+1/2}$$

$S_0$                       central surface brightness

$r_c$                       core radius of gas distribution

$$\beta \equiv \frac{\mu m_p \sigma^2}{kT_g} = \frac{\text{specific energy in galaxies}}{\text{specific energy in the hot gas}}$$

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$\mu$  is the mean molecular weight

$m_p$  is the mass of the proton

$\sigma$  is the one-dimensional velocity dispersion of the galaxies

$T_g$  is the temperature of the ICM

Typically the gas is assumed to be isothermal

$\beta$  treated as fit parameter; typically  $\sim 2/3$   
 BUT often higher when sigma well measured  
 and often lower in groups



# Mass Estimator

$$M_{tot}(< R) = \frac{kT_g(R)}{G\mu m_p} \left[ \frac{\partial \log \rho}{\partial \log r} + \frac{\partial \log T}{\partial \log r} \right] R$$



the gas density profile is determined by fitting the standard beta model to the surface brightness profile.

the gas temperature is measured directly from the X-ray spectrum



Assumes

hydrostatic equilibrium

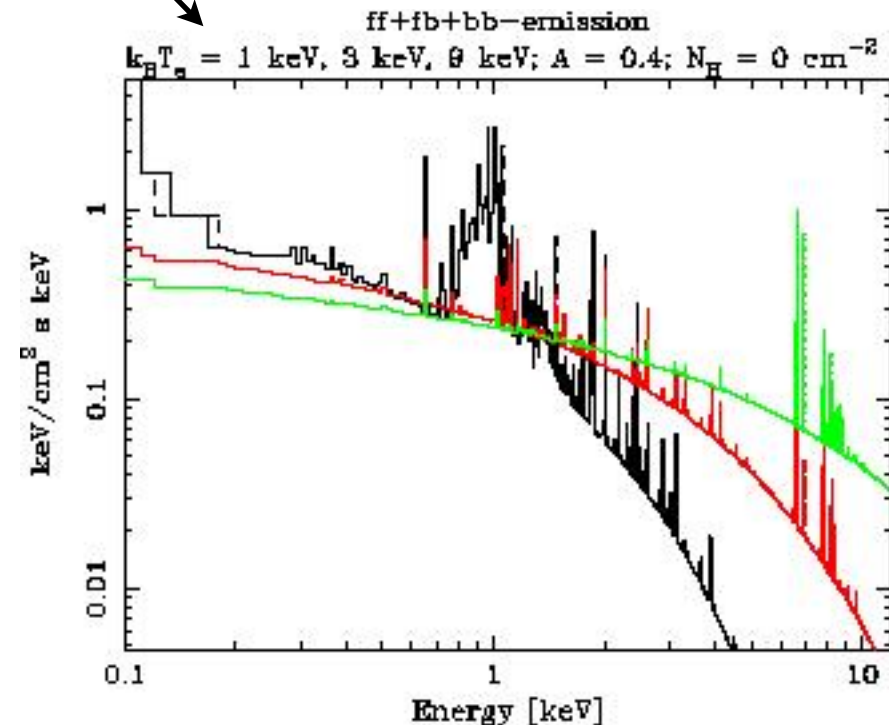
sphericity

often assumes

isothermality



$$\frac{\partial \log T}{\partial \log r} = 0$$

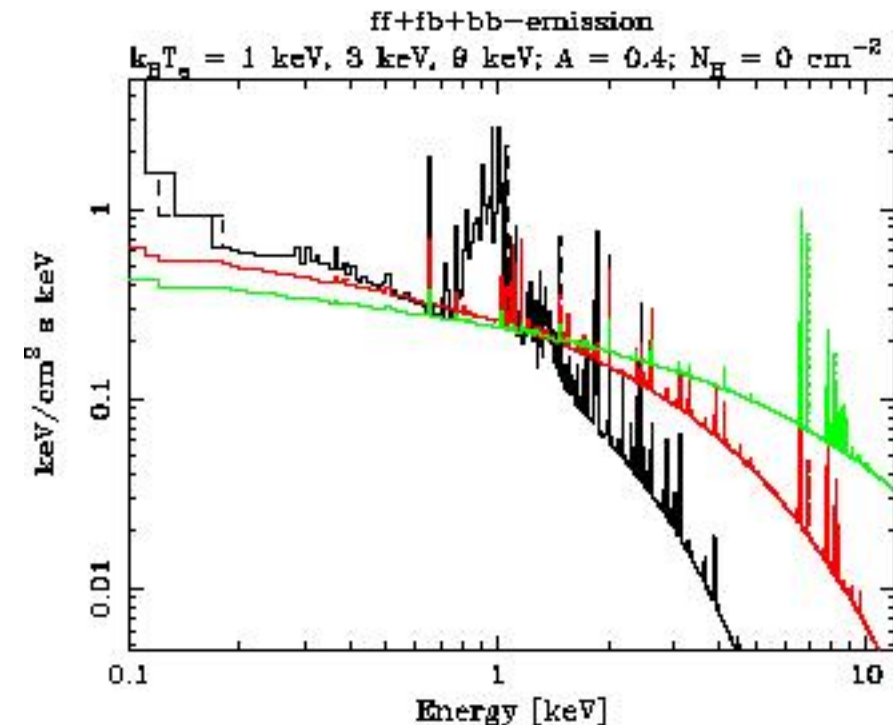


# Mass Estimator

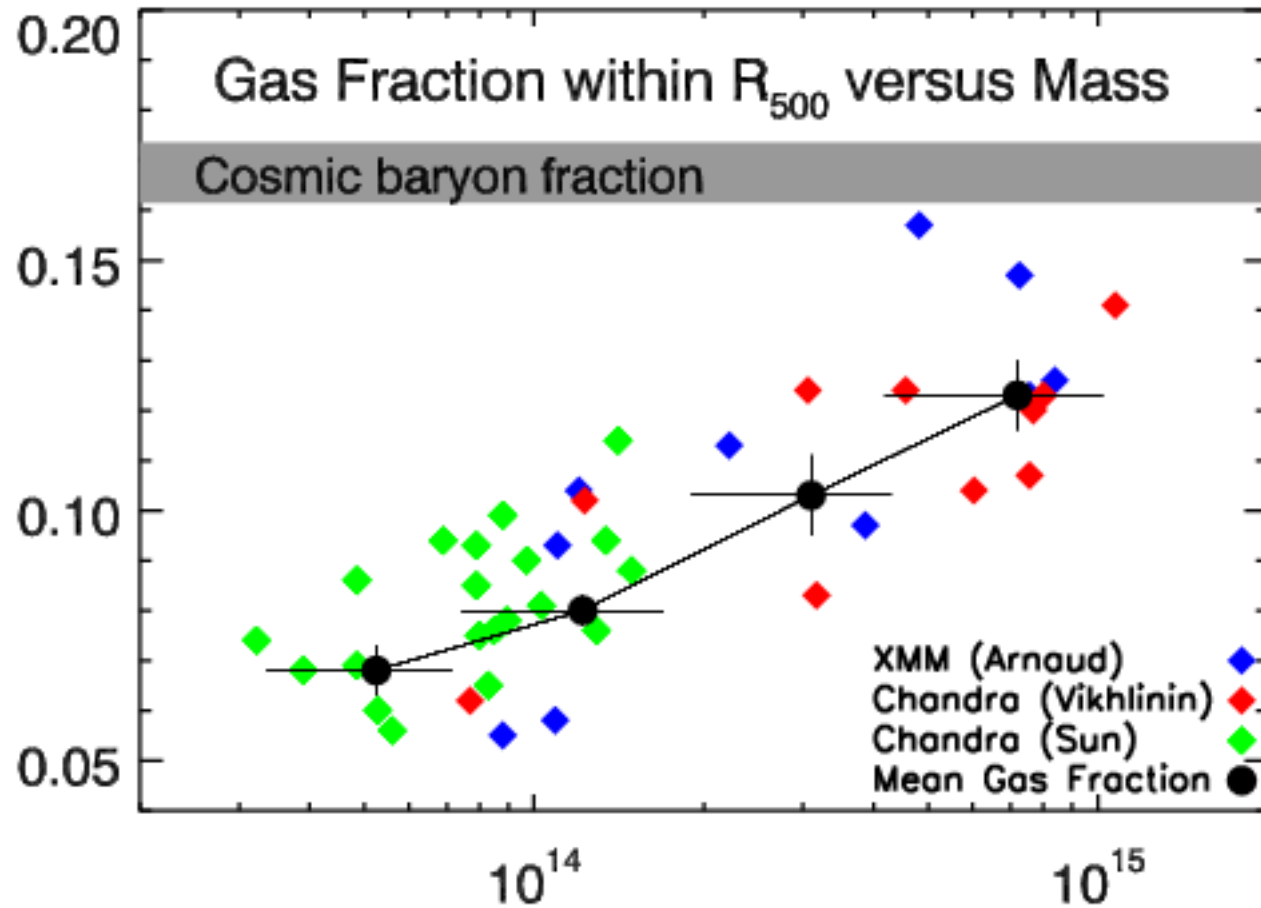
$$M_{tot}(< R) = \frac{kT_g(R)}{G\mu m_p} \left[ \frac{\partial \log \rho}{\partial \log r} + \frac{\partial \log T}{\partial \log r} \right] R$$

basically,

$$M_{tot}(< R) \sim T_{\text{gas}} R$$



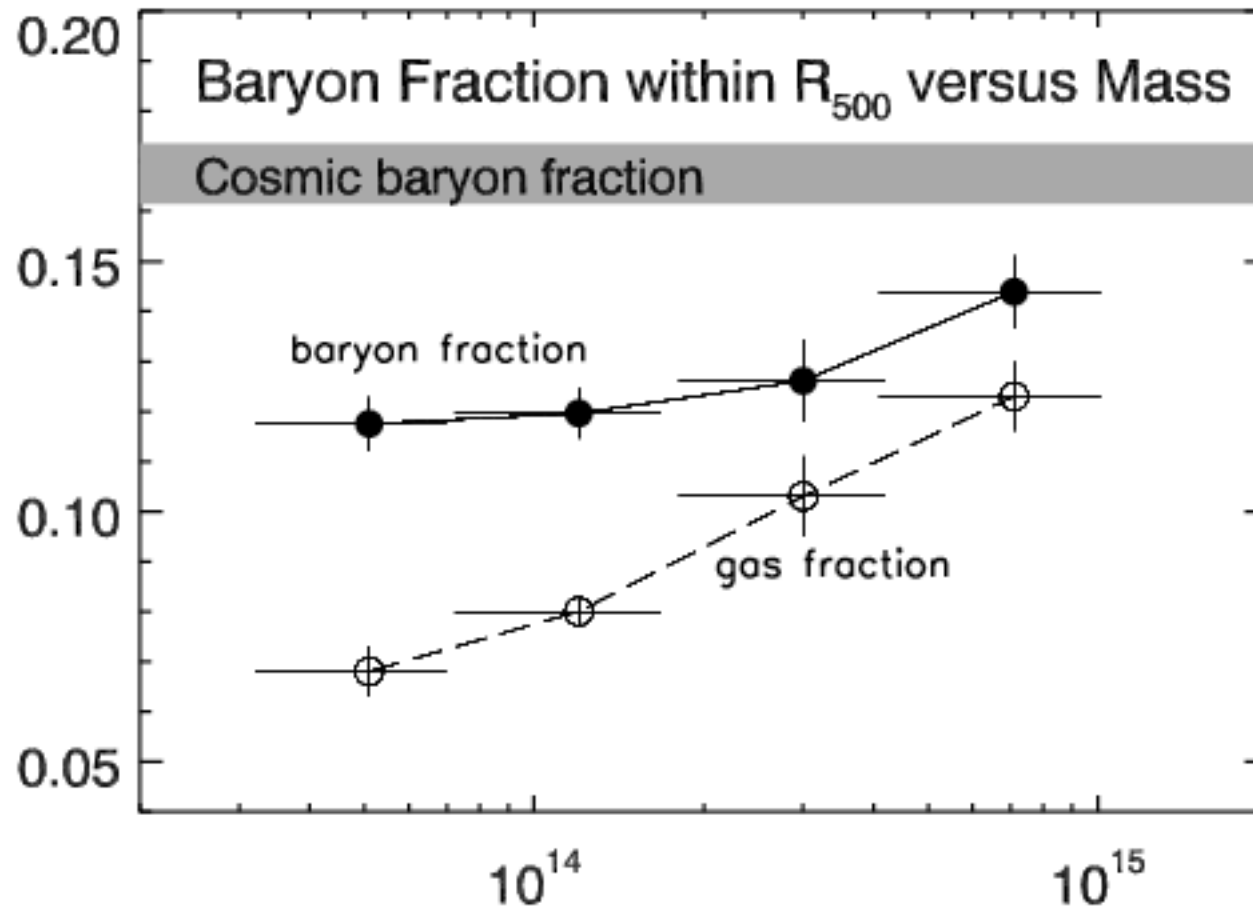
# Rasheed (2010)



Typical result:  
clusters have close to, but not quite, expected  
baryon fraction



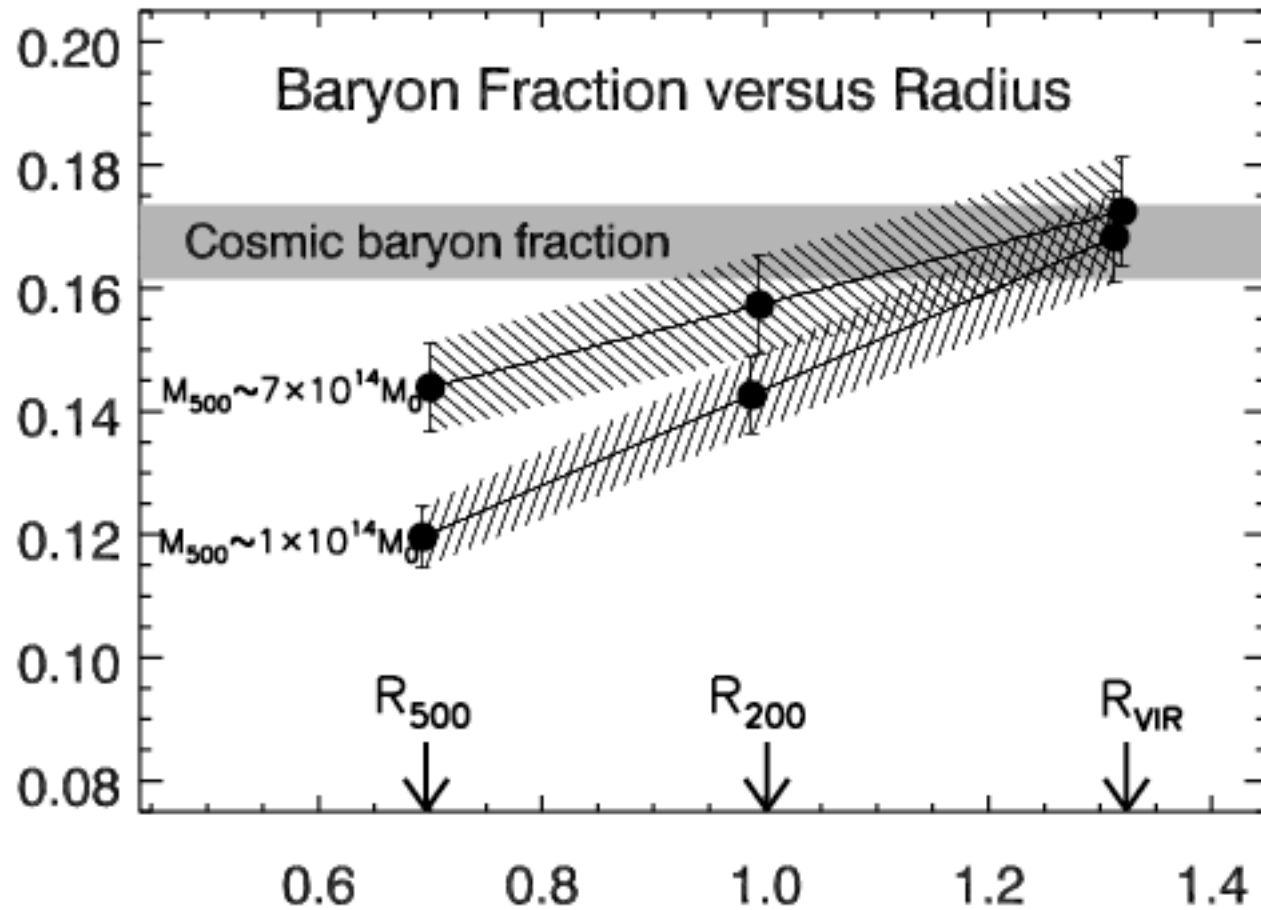
# Rasheed (2010)



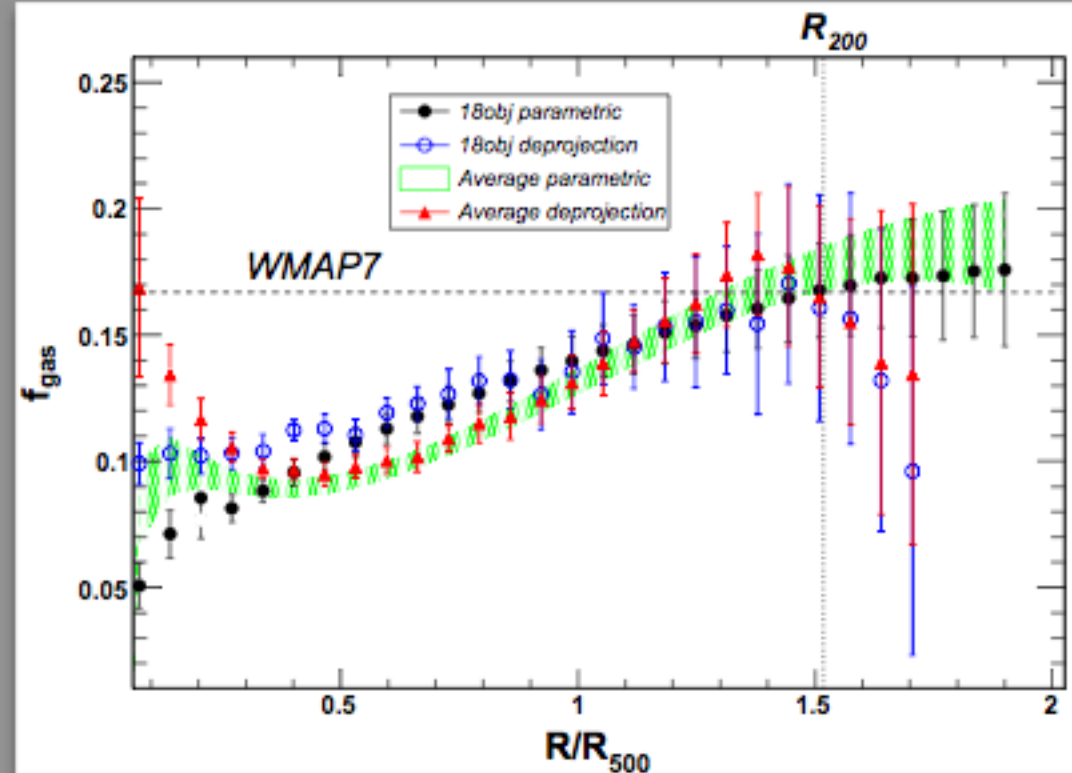
Typical result:

clusters have progressively more gas than stars  
at higher masses

# Rasheed (2010)



Typical result:  
the baryon fraction increases with radius



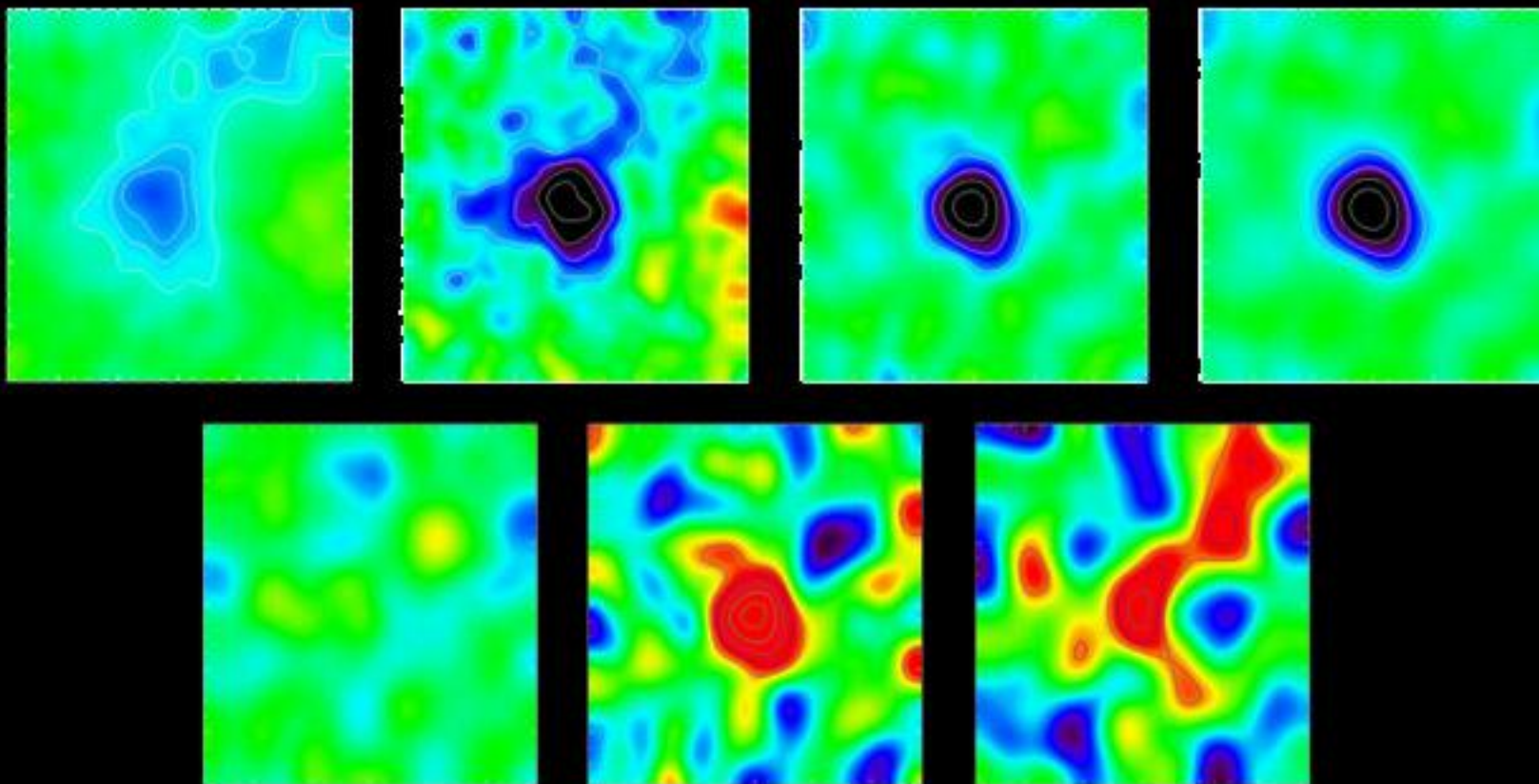
Typical result:

ICM gas outweighs the stars by factor of  $\sim 6$ ;  
outweighed by dark matter by same factor

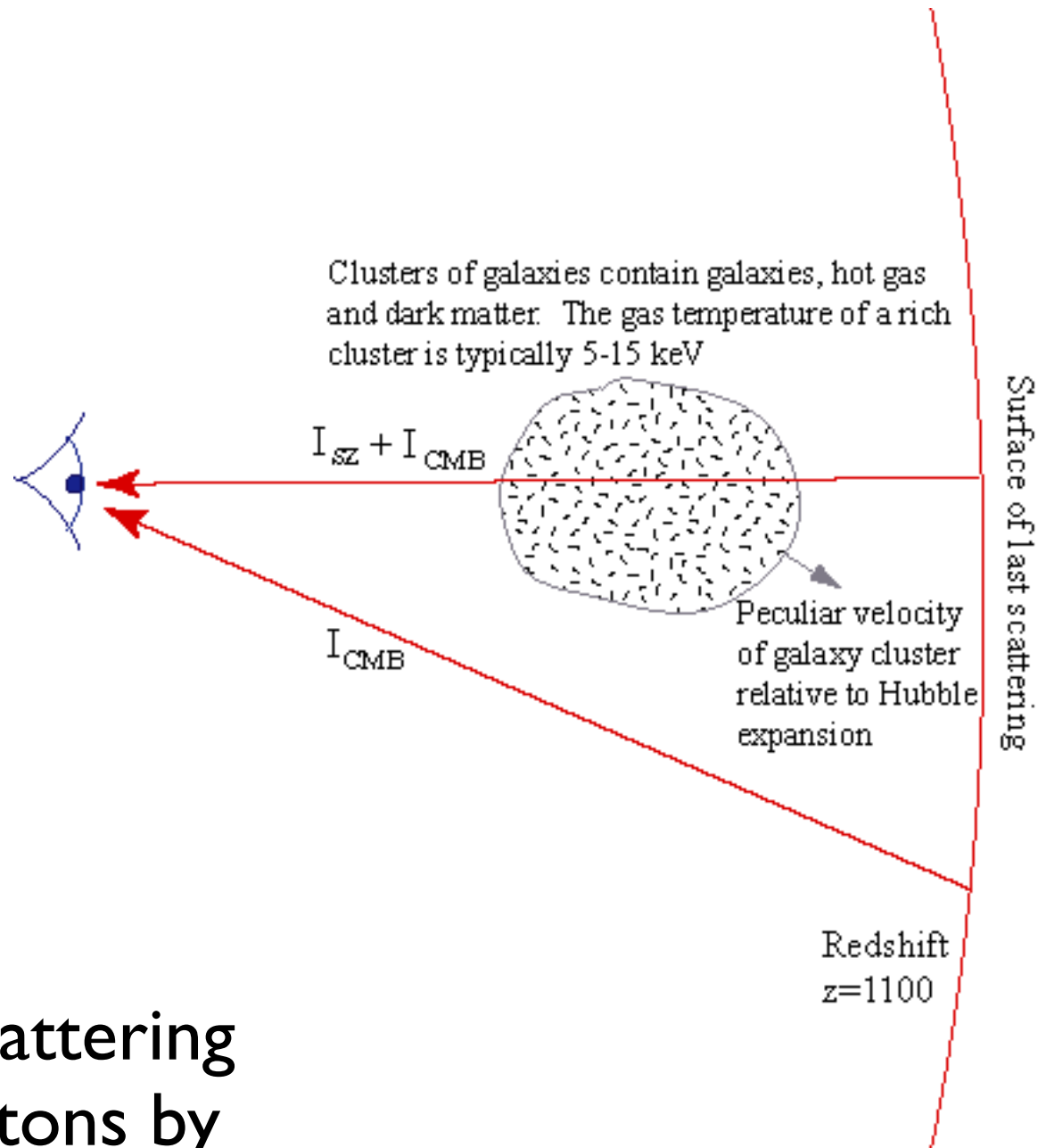
there seems to be more dark matter towards  
the centers of clusters



# SUNYAEV-ZEL'DOVICH EFFECT



# SUNYAEV-ZEL'DOVICH EFFECT



Compton scattering  
of CMB photons by  
hot ICM plasma

frequency dependent change in intensity

$$\frac{\delta I_{nu}}{I_\nu} = -y \frac{x e^x}{e^x - 1} \left[ 4 - x \coth \left( \frac{x}{2} \right) \right]$$

where  $x = \frac{h\nu}{kT_{rad}}$  and  $y = \int \sigma_T n_e \frac{kT_g}{m_e c^2} d\ell$

↑  
CMB

y is the Compton y-parameter  
which quantifies how much  
effect the plasma has

↑  
electron density

↑  
Thomson scattering cross-section

frequency dependent change in intensity

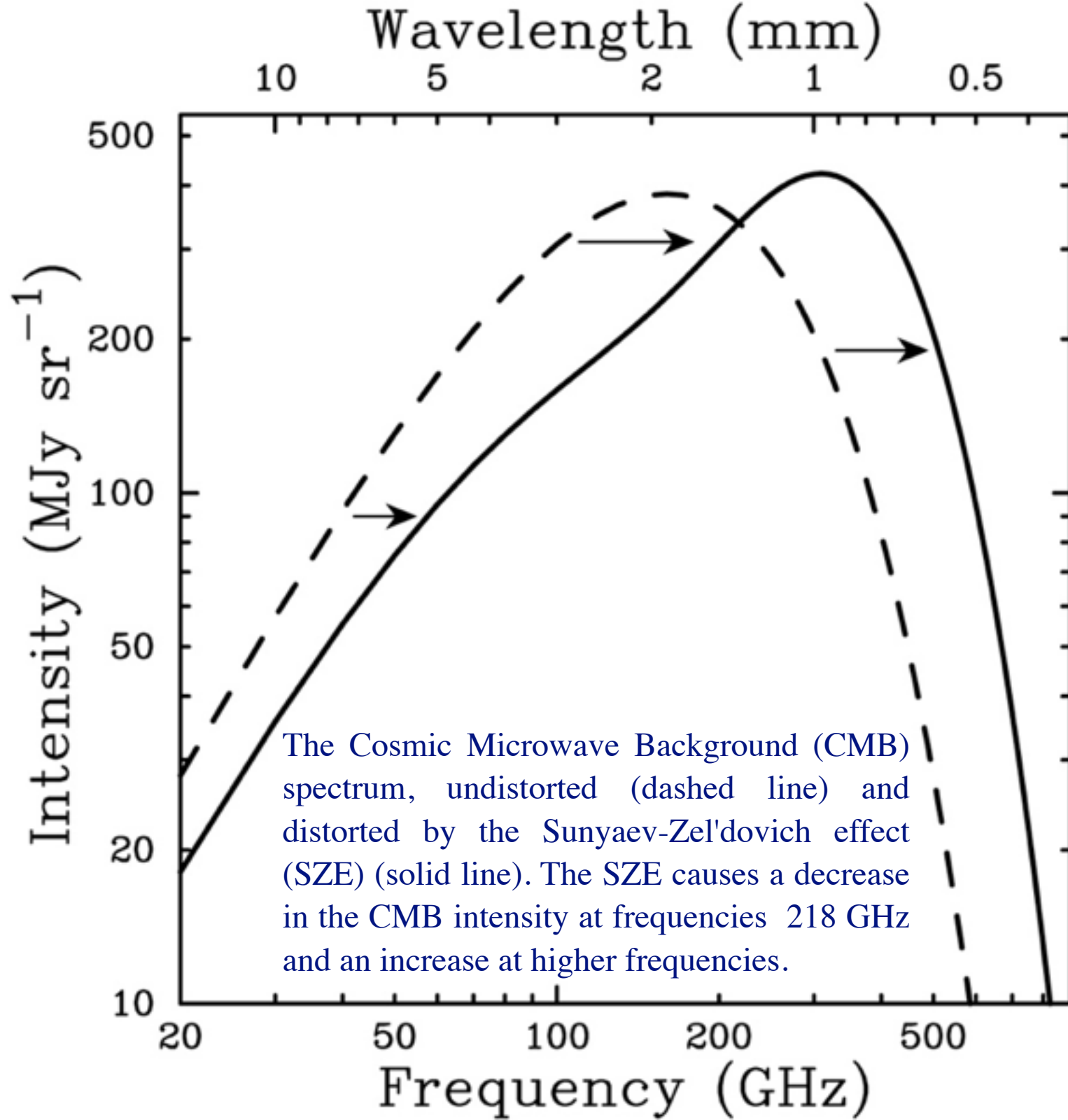
$$\frac{\delta I_{\nu}}{I_{\nu}} = -y \frac{x e^x}{e^x - 1} \left[ 4 - x \coth \left( \frac{x}{2} \right) \right]$$

where  $x = \frac{h\nu}{kT_{rad}}$  and  $y = \int \sigma_T n_e \frac{kT_g}{m_e c^2} d\ell$

at low frequency in the Rayleigh-Jeans tail,

$$\frac{\delta I}{I} = \frac{\delta T}{T} = -2y$$

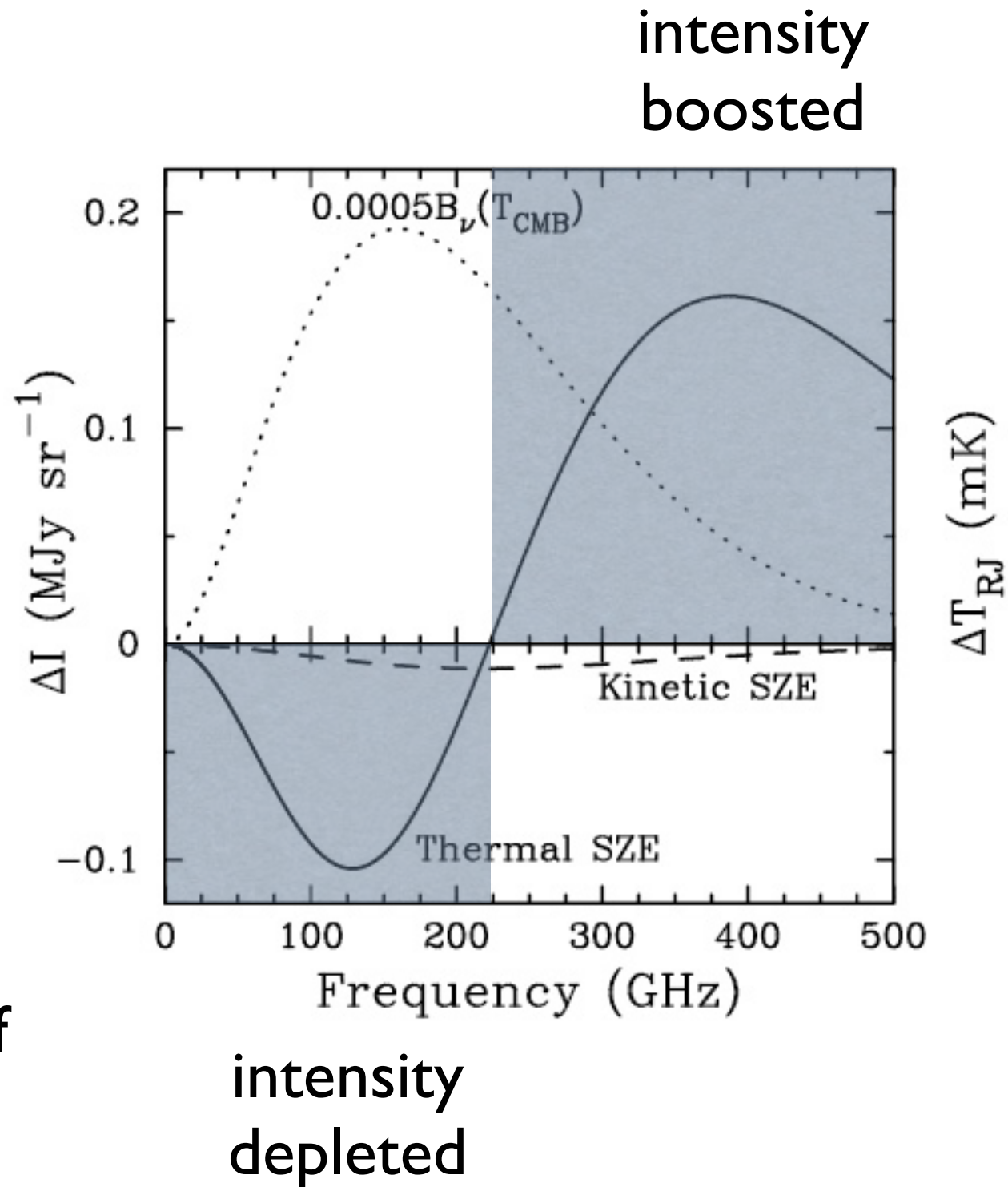


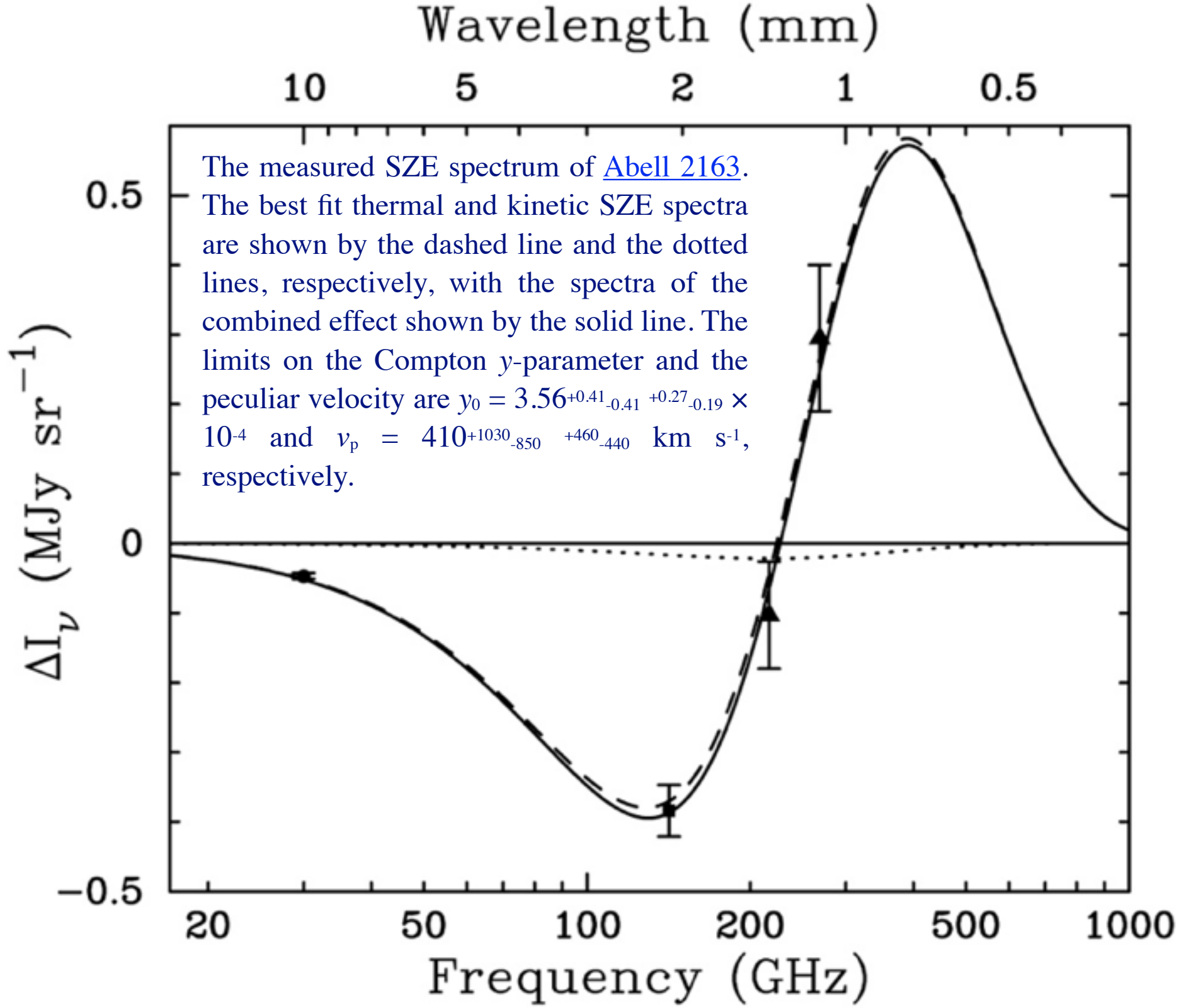


The Cosmic Microwave Background (CMB) spectrum, undistorted (dashed line) and distorted by the Sunyaev-Zel'dovich effect (SZE) (solid line). The SZE causes a decrease in the CMB intensity at frequencies 218 GHz and an increase at higher frequencies.

Thermal SZ effect  
from Compton  
scattering of CMB  
photons by  
cluster plasma

Kinematic SZ effect  
from peculiar velocity of  
cluster wrt CMB frame

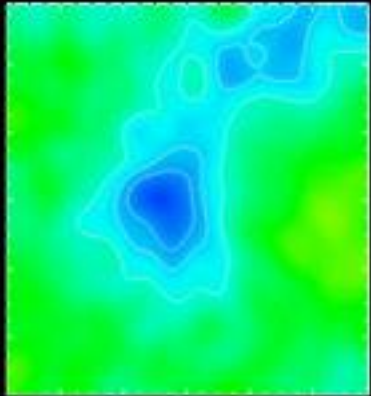




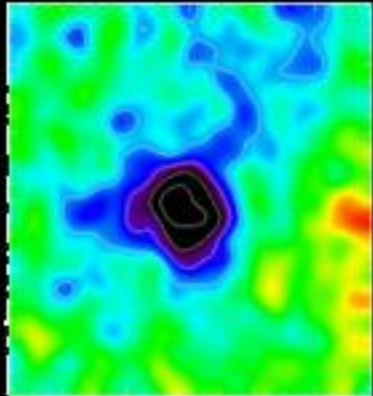
# SUNYAEV-ZEL'DOVICH EFFECT

detected by Planck

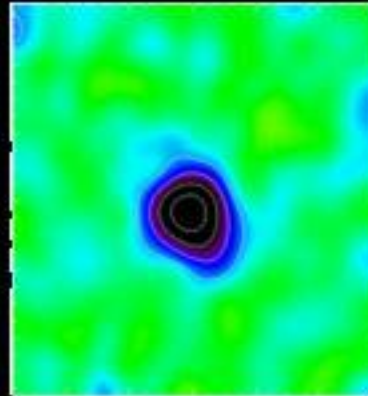
44 GHz



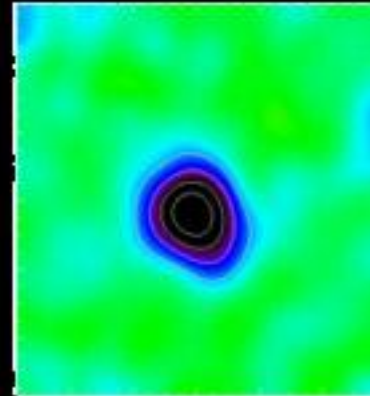
70 GHz



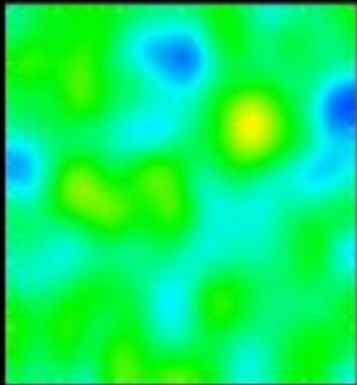
100 GHz



143 GHz

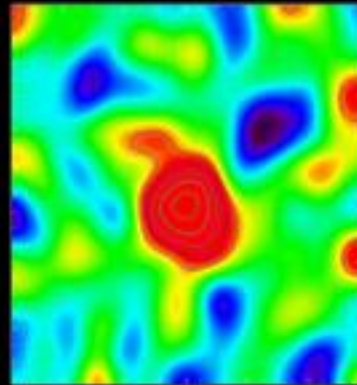


low  
frequency  
deficit

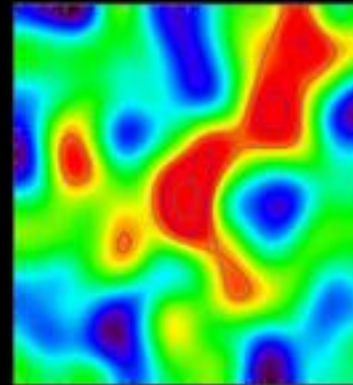


217 GHz

cross-over  
frequency



353 GHz



545 GHz

high  
frequency  
excess



integrated change in CMB temperature

$$\int \Delta T d\Omega \propto \frac{N_e \langle T_e \rangle}{D_A^2} \propto \frac{M \langle T_e \rangle}{D_A^2}$$

depends on the total number of electrons, their temperature, and the area they subtend on the sky. In effect measures Pressure, or mass if T known.

$D_A$  is the angular diameter distance.

At high  $z$ , it varies slowly, while the density increases as  $(1+z)^3$

... SZ effect weak, but nearly independent of redshift!