

DARK MATTER

ASTR 333/433

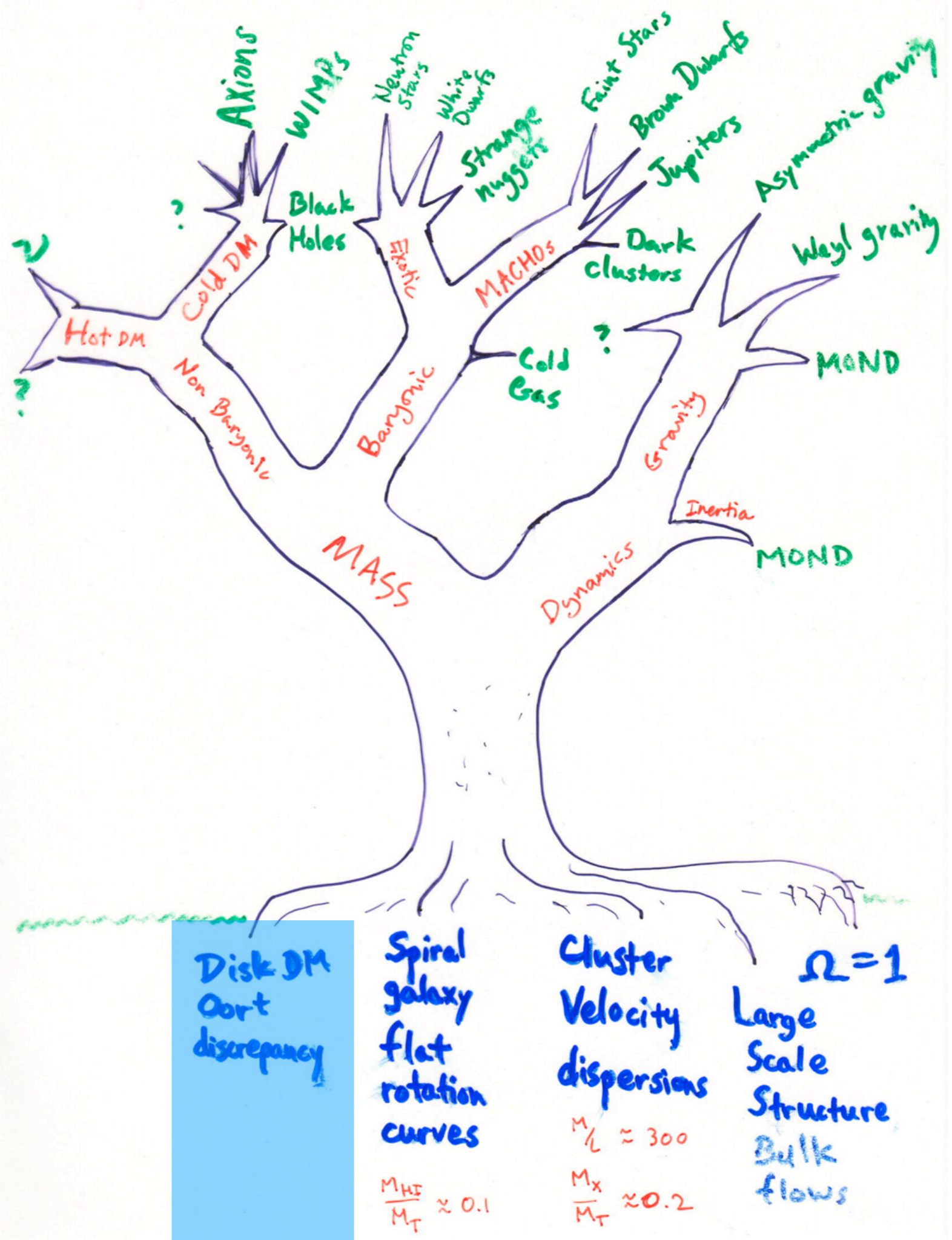
TODAY

Contents of the Milky Way

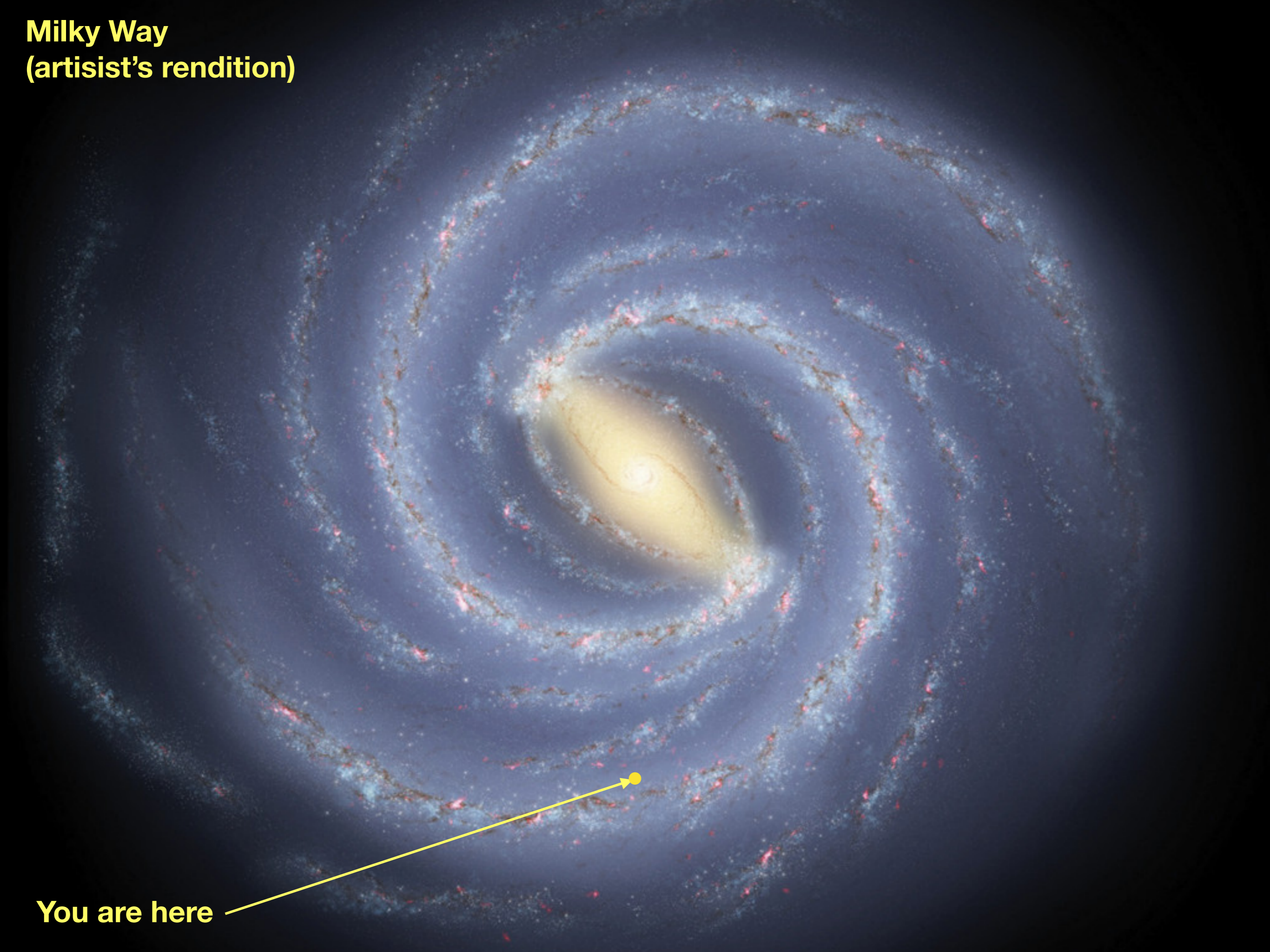
the Oort limit

The Bar Instability

Ostriker & Peebles; Sellwood



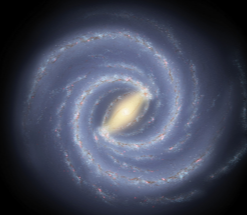
**Milky Way
(artist's rendition)**



You are here

Basic Picture:

Dark Matter Halo



Luminous Galaxy
stars, gas, dust, etc.

Galaxies are embedded in extended,
quasi-spherical halos of dark matter

$$R_{vir} \gg R_*$$

The virial radius of the dark
matter halo is much larger
than the luminous galaxy

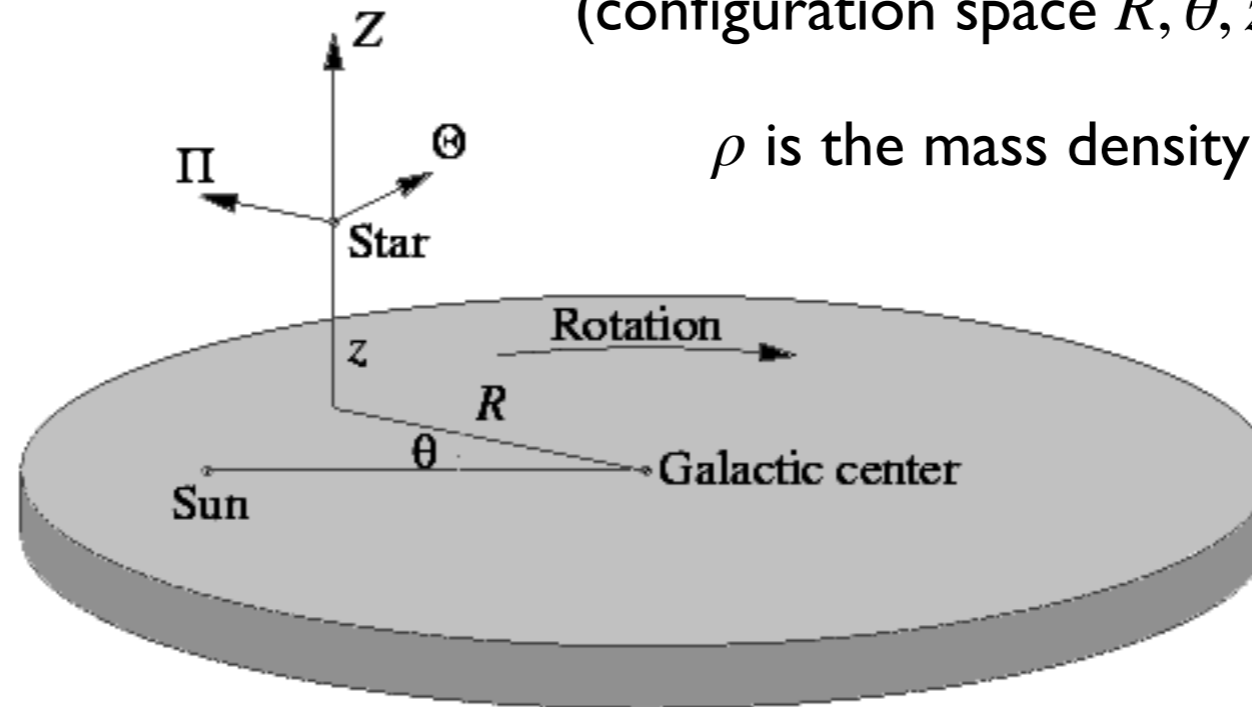
Cylindrical coordinates

Poisson equation: $\nabla^2 \Phi = 4\pi G \rho$

in cylindrical coordinates $\nabla^2 \Phi = \frac{1}{R} \frac{\partial}{\partial R} \left(R \frac{\partial \Phi}{\partial R} \right) + \frac{1}{R^2} \frac{\partial^2 \Phi}{\partial \theta^2} + \frac{\partial^2 \Phi}{\partial z^2}$

Let's define a coordinate system:

Galactocentric cylindrical coordinates



We wish to extract the gravitational potential Φ from observations of the 6D phase space of stars (configuration space R, θ, z ; momentum Π, Θ, Z)

ρ is the mass density (including dark matter)

Position : (R, θ, z)

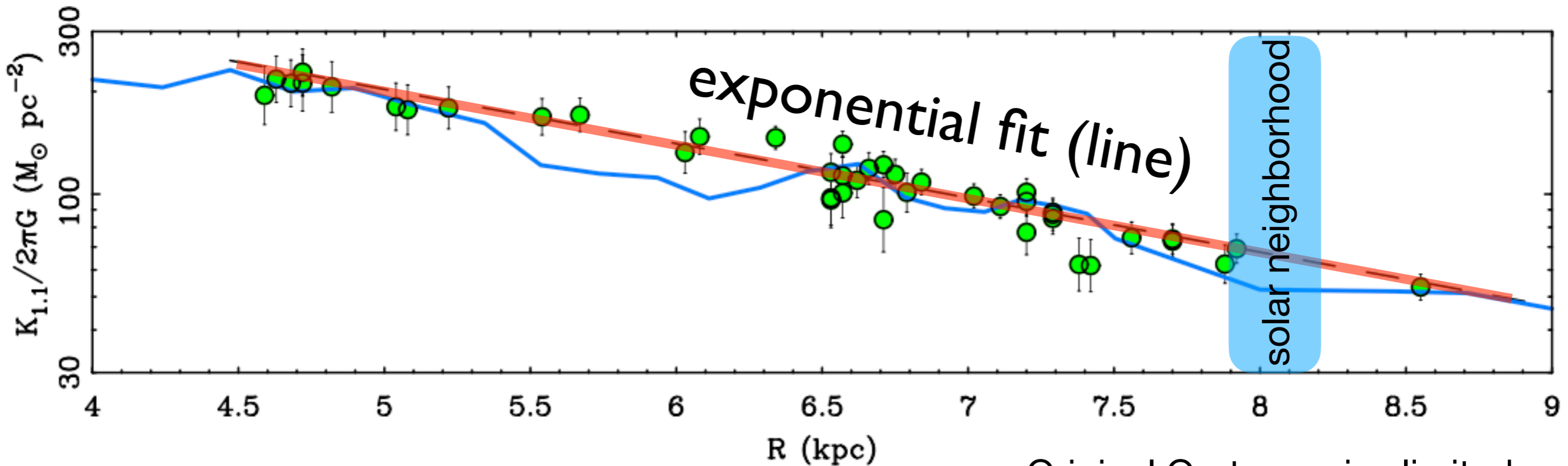
- R = galactocentric distance
- θ = azimuthal coordinate
- z = height above/below the plane

Velocity : (Π, Θ, Z)

- Π = velocity in/out from center
- Θ = tangential velocity
- Z = velocity up and down

OR Cartesian $(X, Y, Z; U, V, W)$ centered on either the sun or the Galactic Center.

Assuming axial symmetry and that $\Phi(R, z)$ is separable, the vertical force is $K_Z = 2\pi G\Sigma + \frac{Z}{R} \frac{\partial V^2}{\partial R}$



$$\Sigma(R) = \Sigma_{\odot} e^{-\frac{(R - R_{\odot})}{R_d}}$$

$$\Sigma_{\odot} = 38 M_{\odot} \text{pc}^{-2}$$

$$R_d = 2.15 \text{ kpc}$$

(stars only)

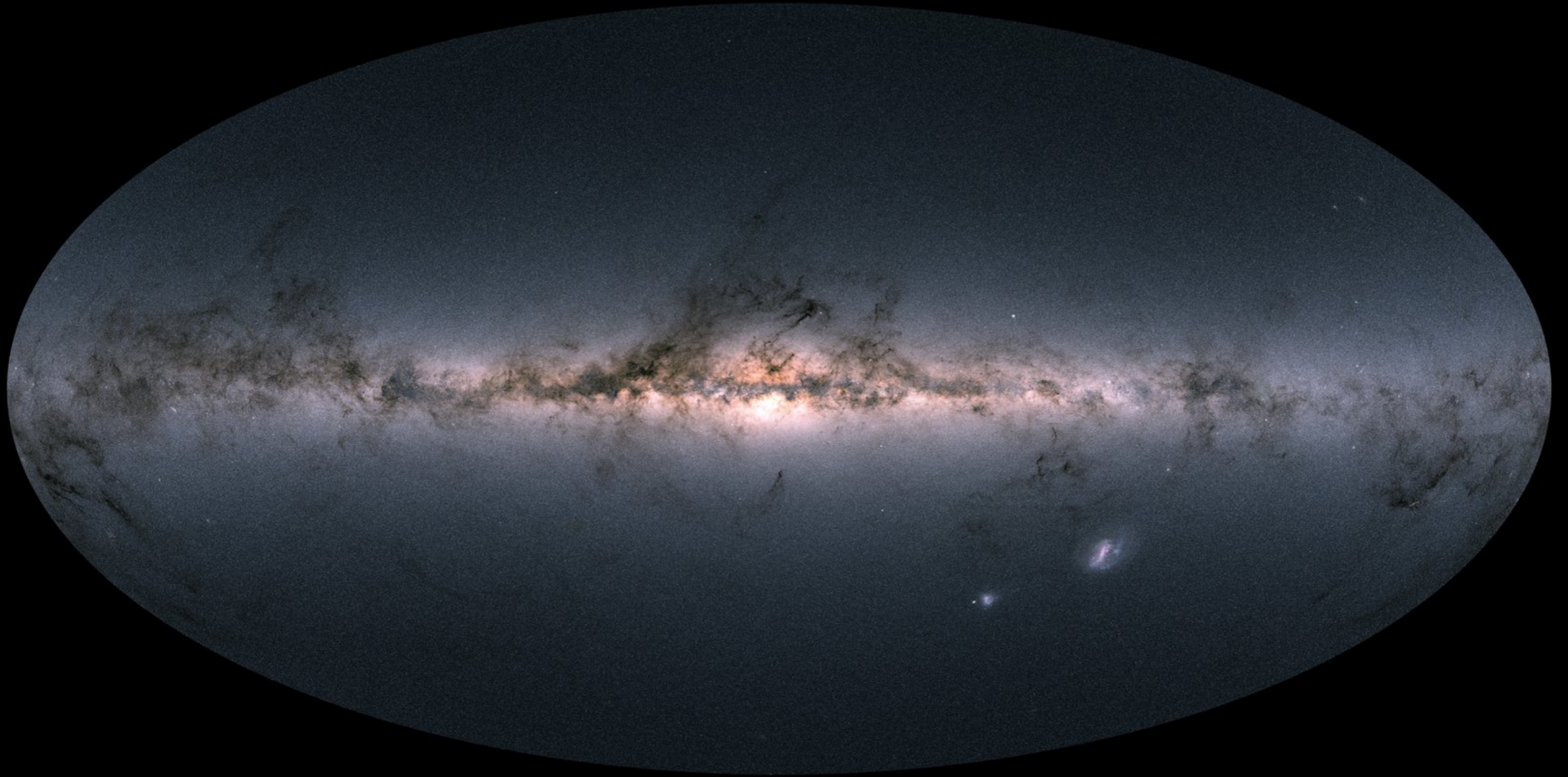
Bovy & Rix (2013)

Original Oort exercise limited to the solar neighborhood.
Can now expand to other radii.

Continues to improve with surveys like Gaia and APOGEE, e.g.,

Price-Whelan et al. (2021, ApJ, 910, 17)
Eilers et al. (2019, ApJ, 871, 120)
McGaugh (2019, ApJ, 885, 87)

Milky Way in the optical (Gaia data)



Baryonic Content of Galaxies

● **Stars**

- Majority of baryonic mass in bright galaxies

● **Gas**

- *Atomic gas - H I*

- traced by 21 cm line Majority of baryonic mass in faint galaxies

- *Molecular gas - H₂*

- traced by CO Mass usually a distant third to stars and atomic gas

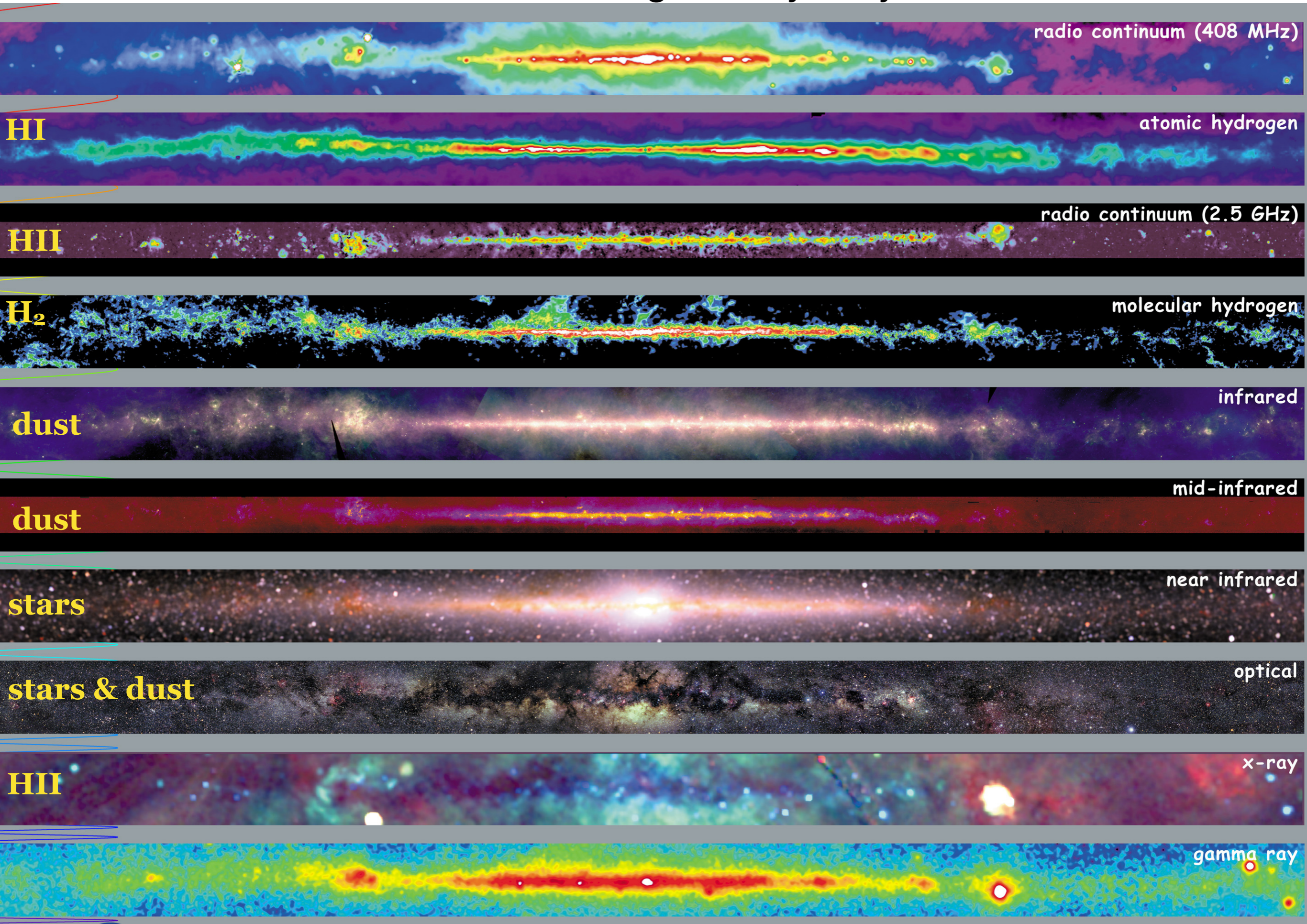
- *Ionized gas - H II*

- traced by H α Large volume but little mass where stars are; there might be a lot out to the virial radius.

● **Dust**

- little mass, but it does get in the way.

Multi-wavelength Milky Way



Disk Stability

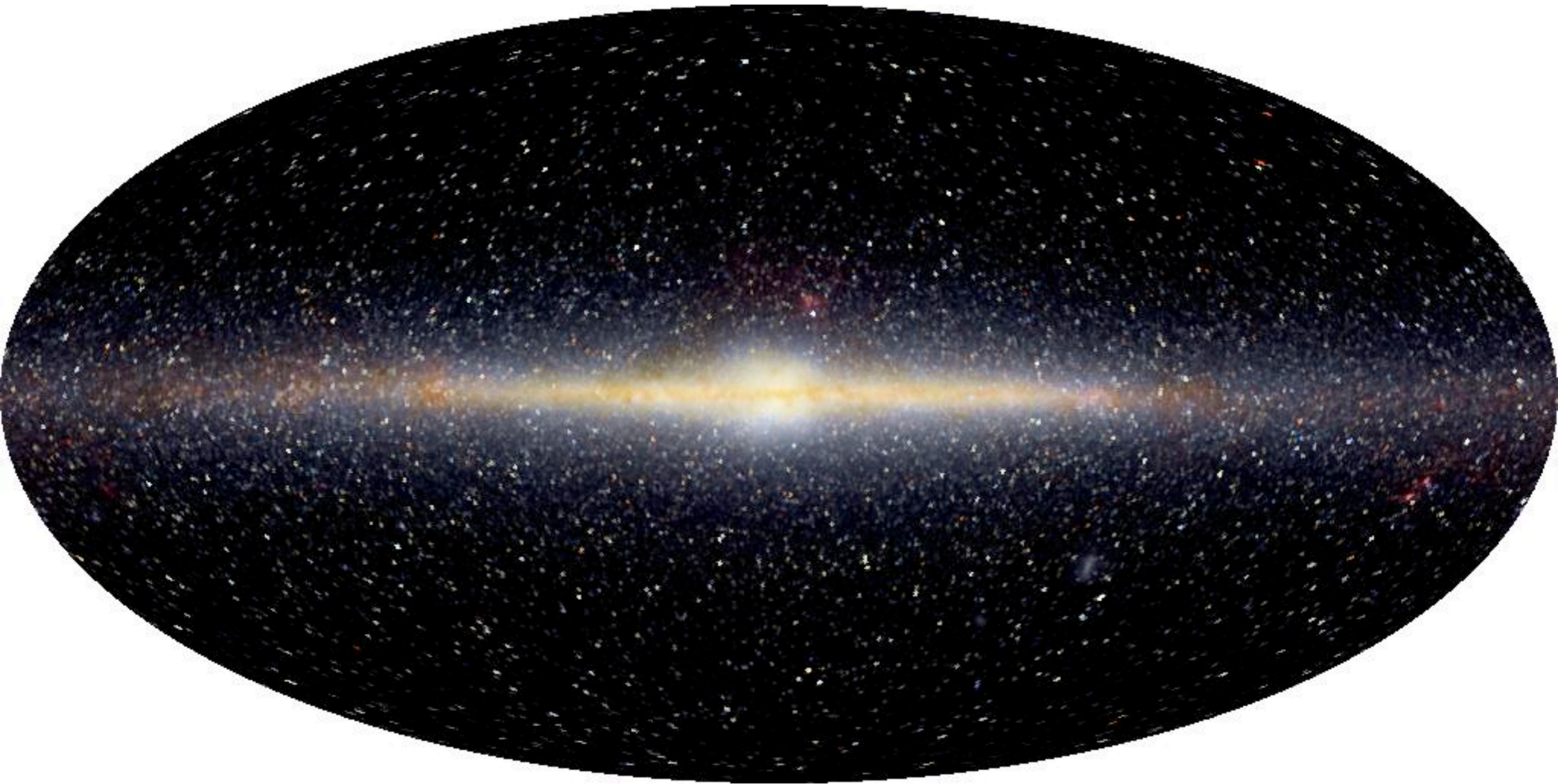


NGC 628: a spiral galaxy



NGC 1300: a barred spiral galaxy

The Milky Way is a barred spiral



Peanut-shaped bulge is the signature of a bar seen edge-on.
Our viewing angle is $20 - 30^\circ$ from the major axis of the bar.

The Bar Instability

Spiral disks unstable to the development of $m=2$ bar modes.

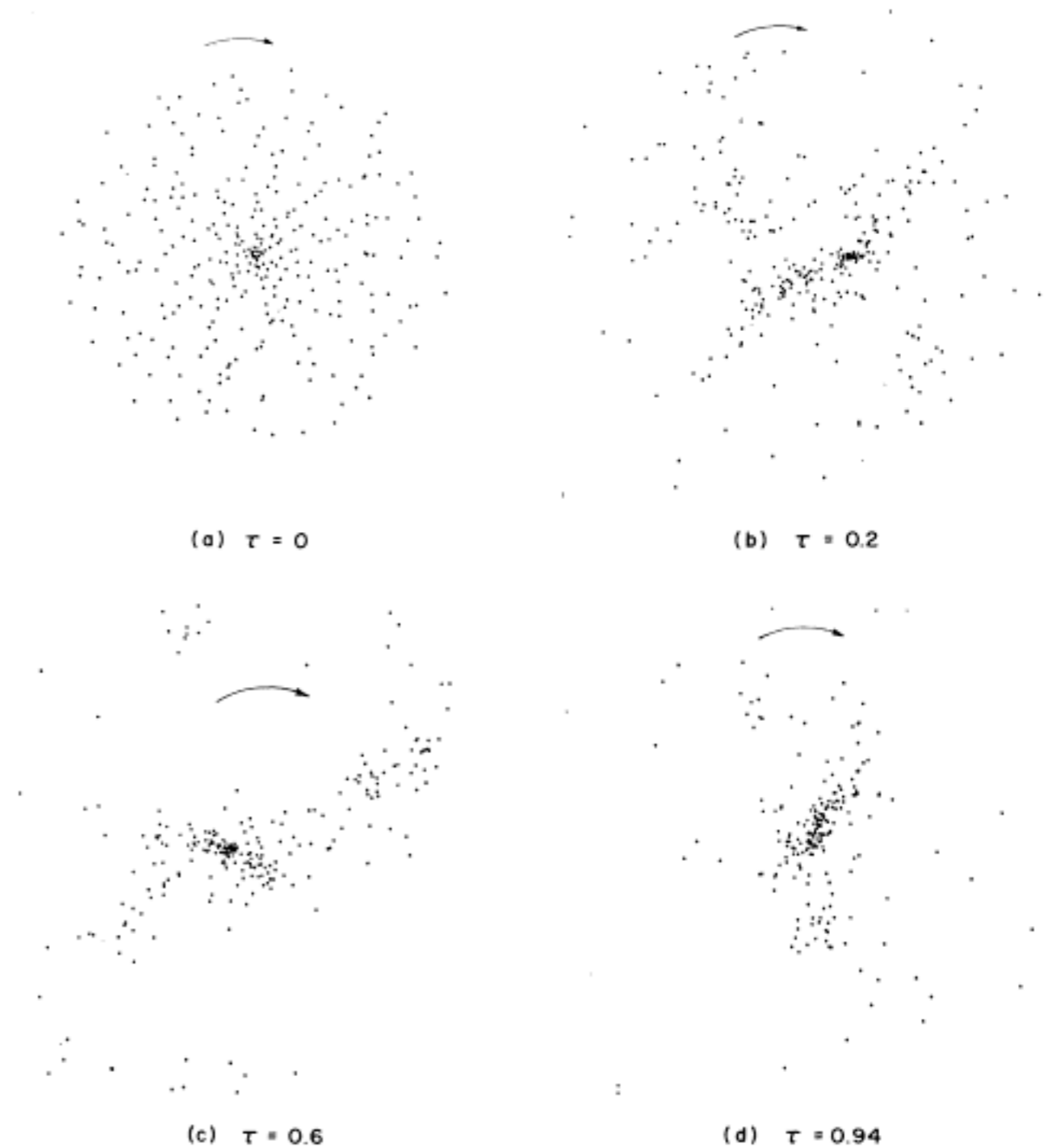
Left to themselves, spiral disks fall apart in just a few dynamical times (< 1 Gyr for the Milky Way).

Cold disks are unstable if left to themselves, So Ostriker & Peebles suggested embedding them in dark matter halos.

By “cold” we mean that ordered rotation exceeds random motions: $V \gg \sigma$.

Ostriker & Peebles (1973)

Sellwood (2016)



<http://burro.astr.cwru.edu/Academics/Astr222/Galaxies/Spiral/nohalo.mpg>

<http://burro.astr.cwru.edu/Academics/Astr222/Galaxies/Spiral/halo.mpg>

Sellwood (2016)

Time evolution of the bar amplitude in models with differing $\frac{M_{halo}}{M_{disk}}$

