

# DARK MATTER

ASTR 333/433

SPRING 2016

T R 4:00-5:15PM

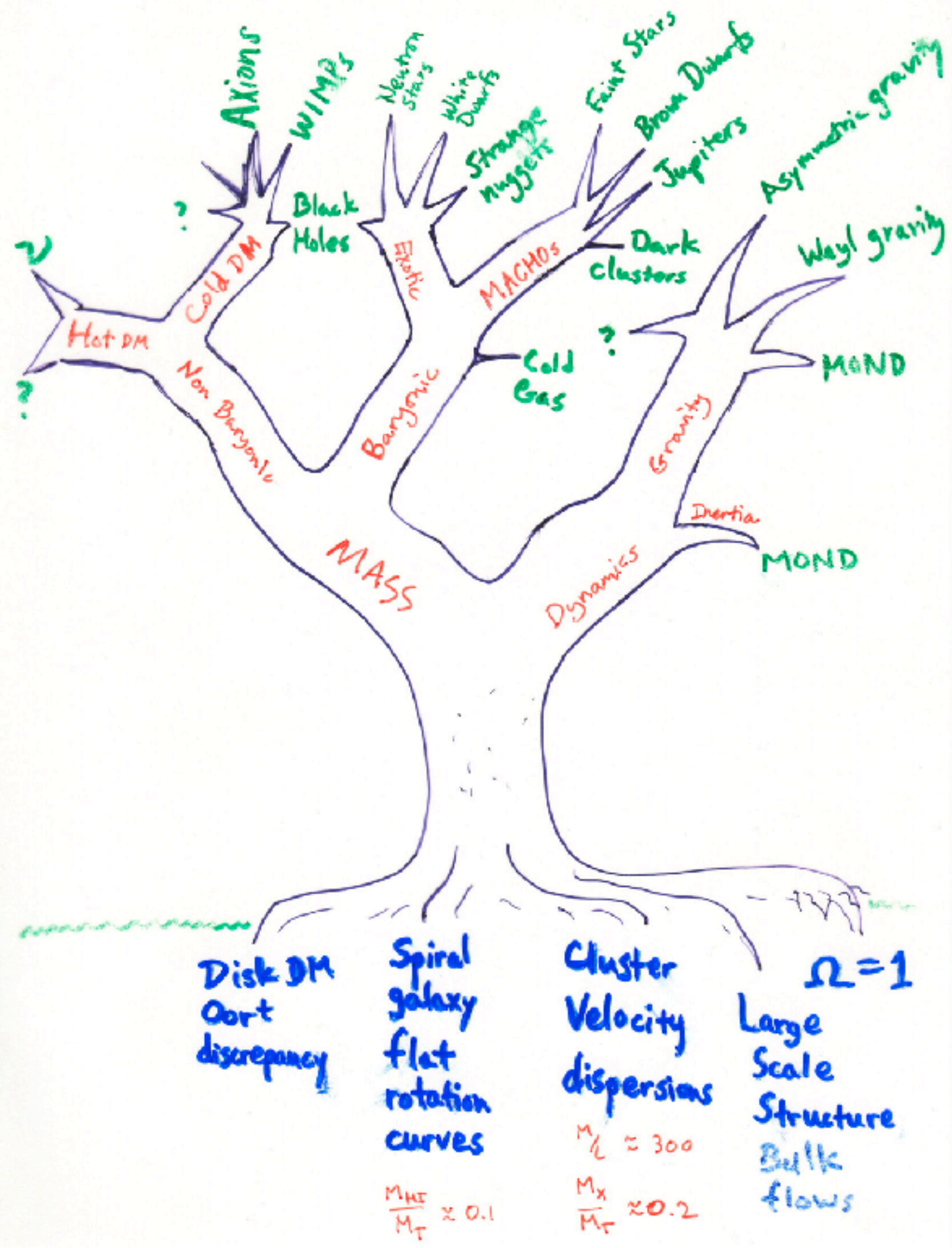
SEARS 552

## TODAY

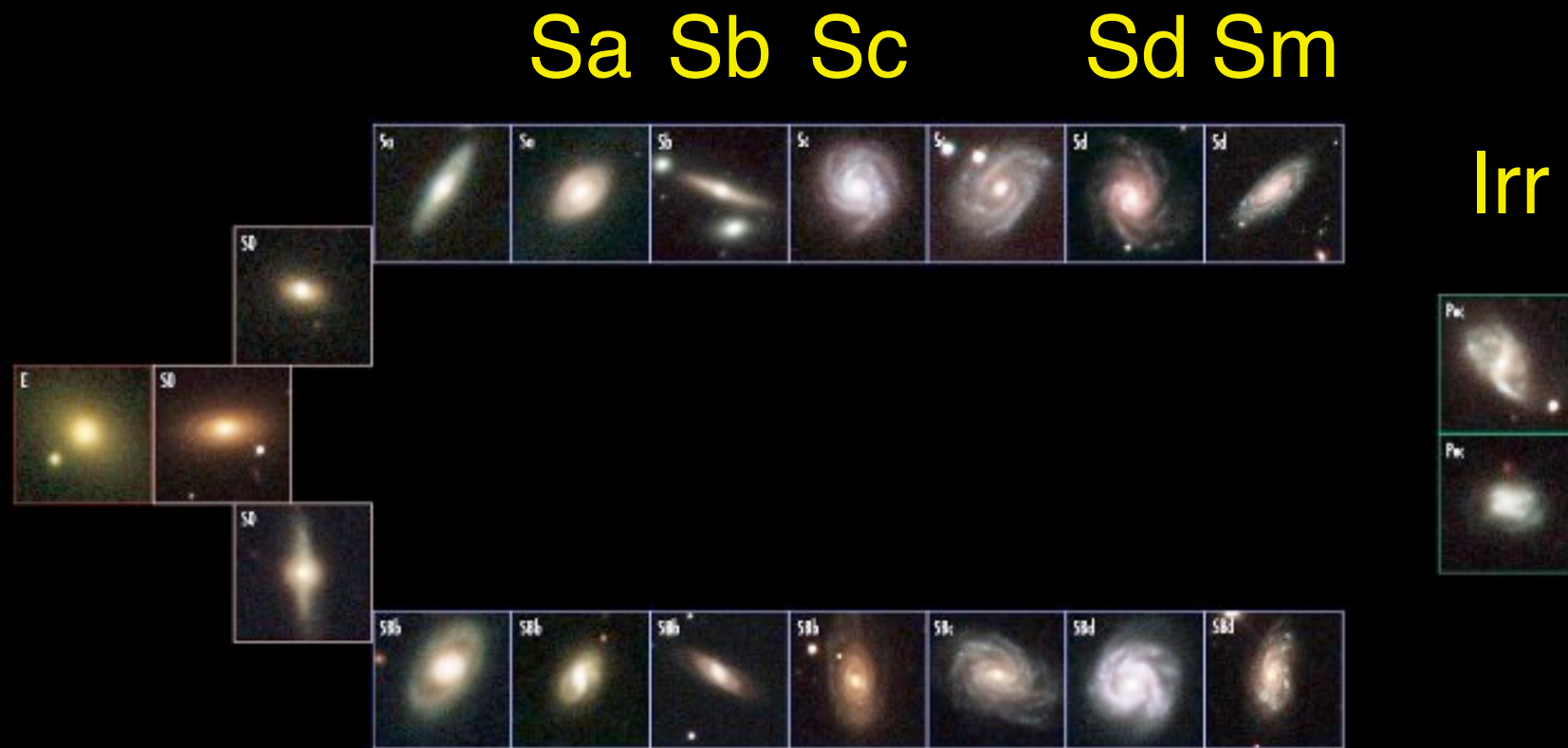
RANGE OF GALAXY PROPERTIES

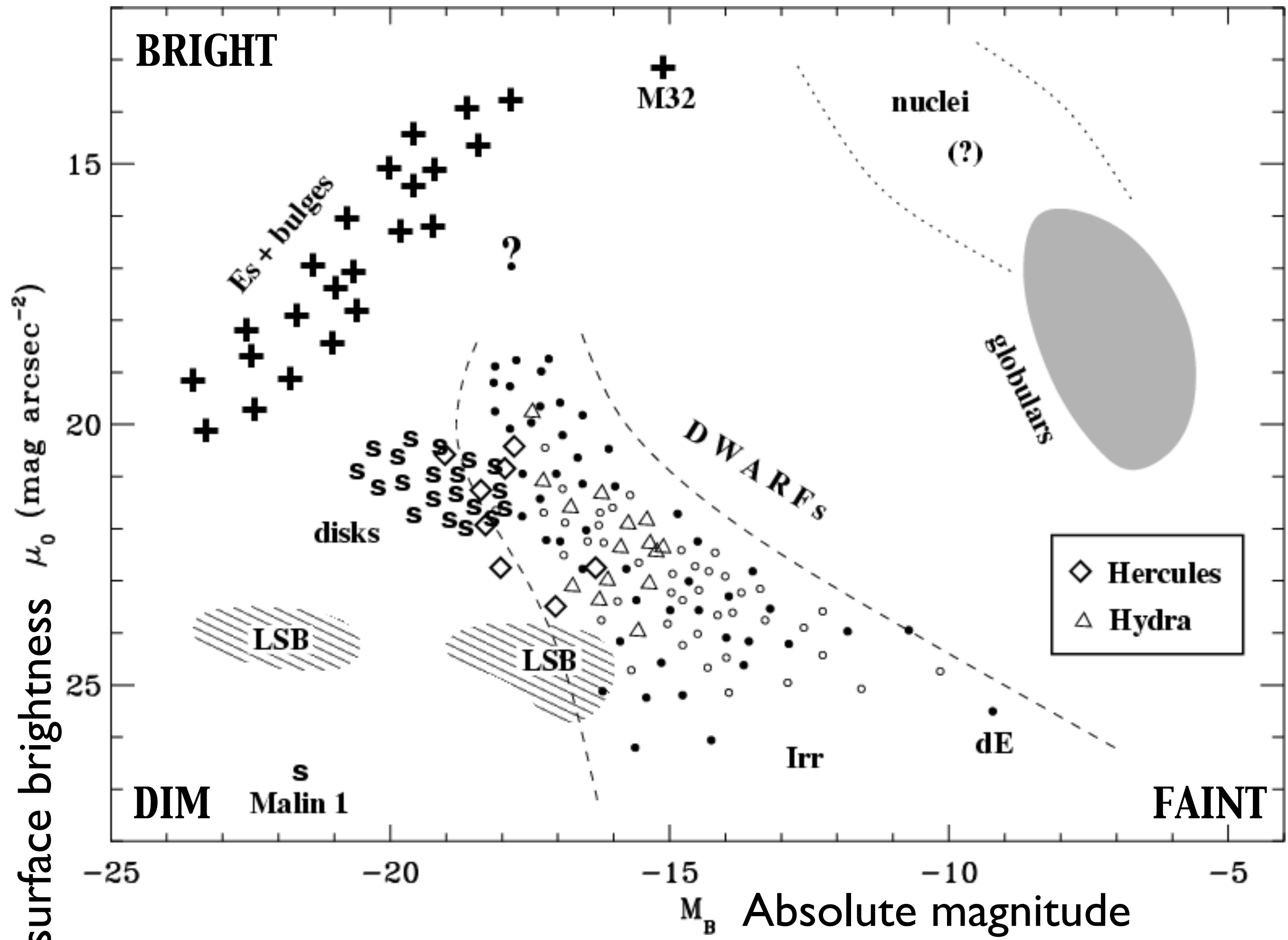
THE OORT LIMIT

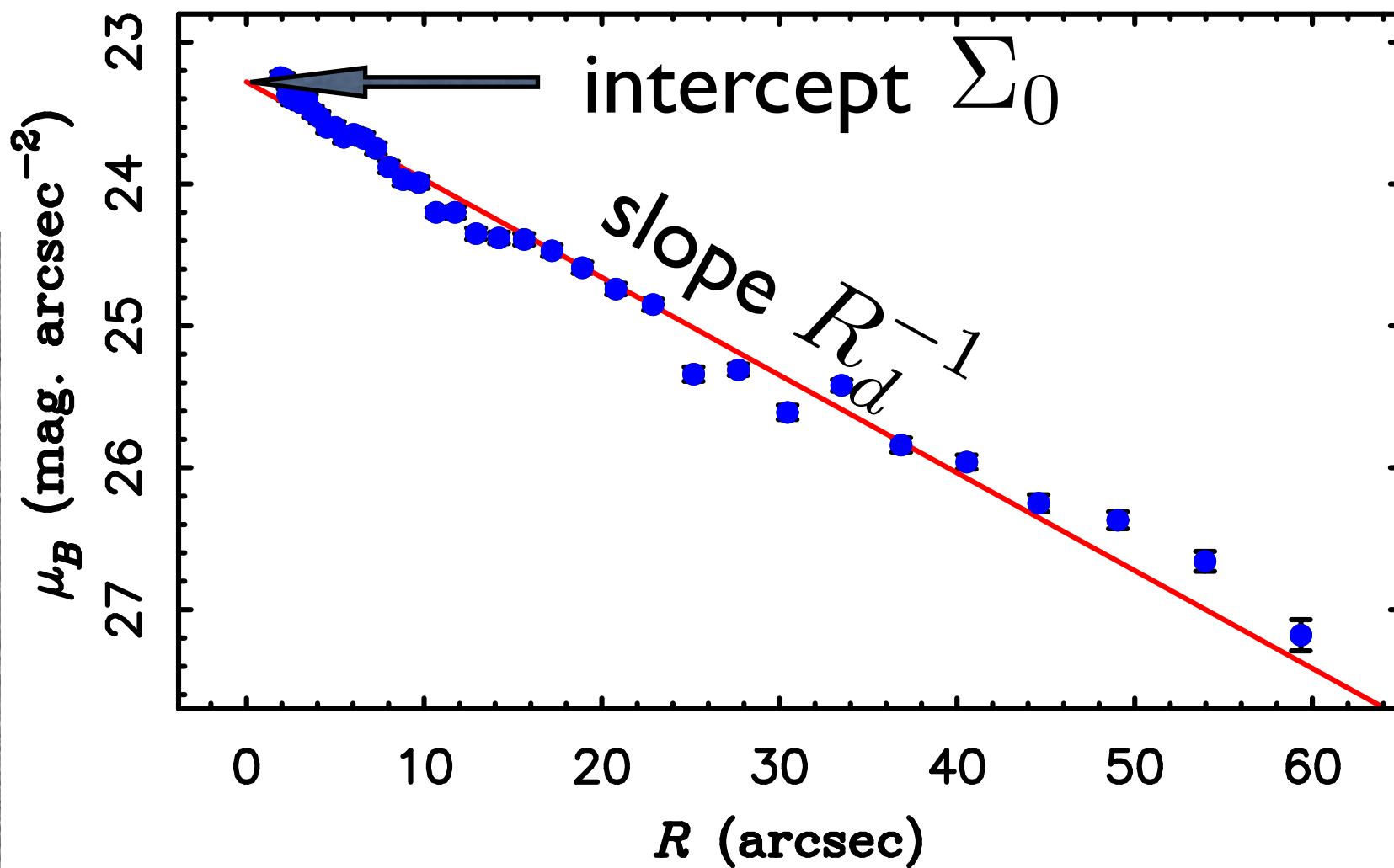
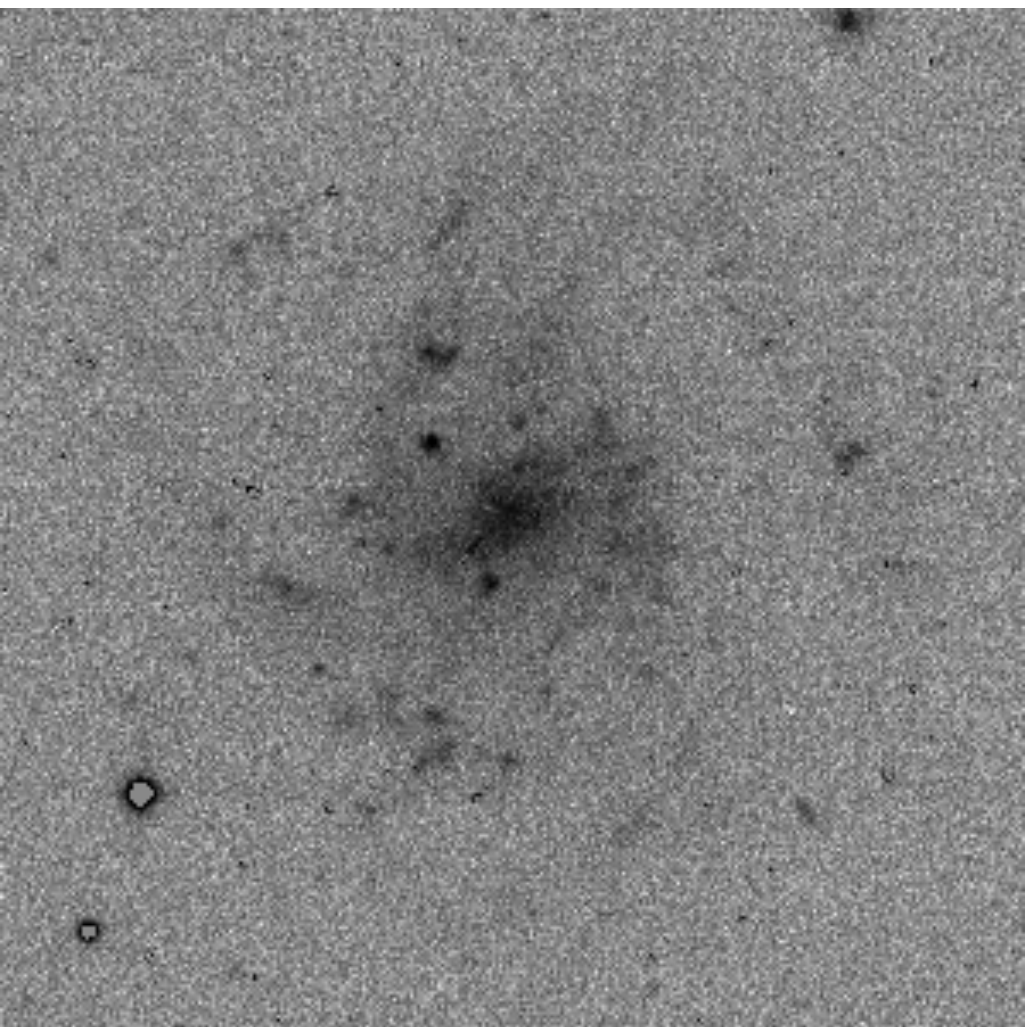
THE BAR INSTABILITY



# The original Hubble sequence extended to later types





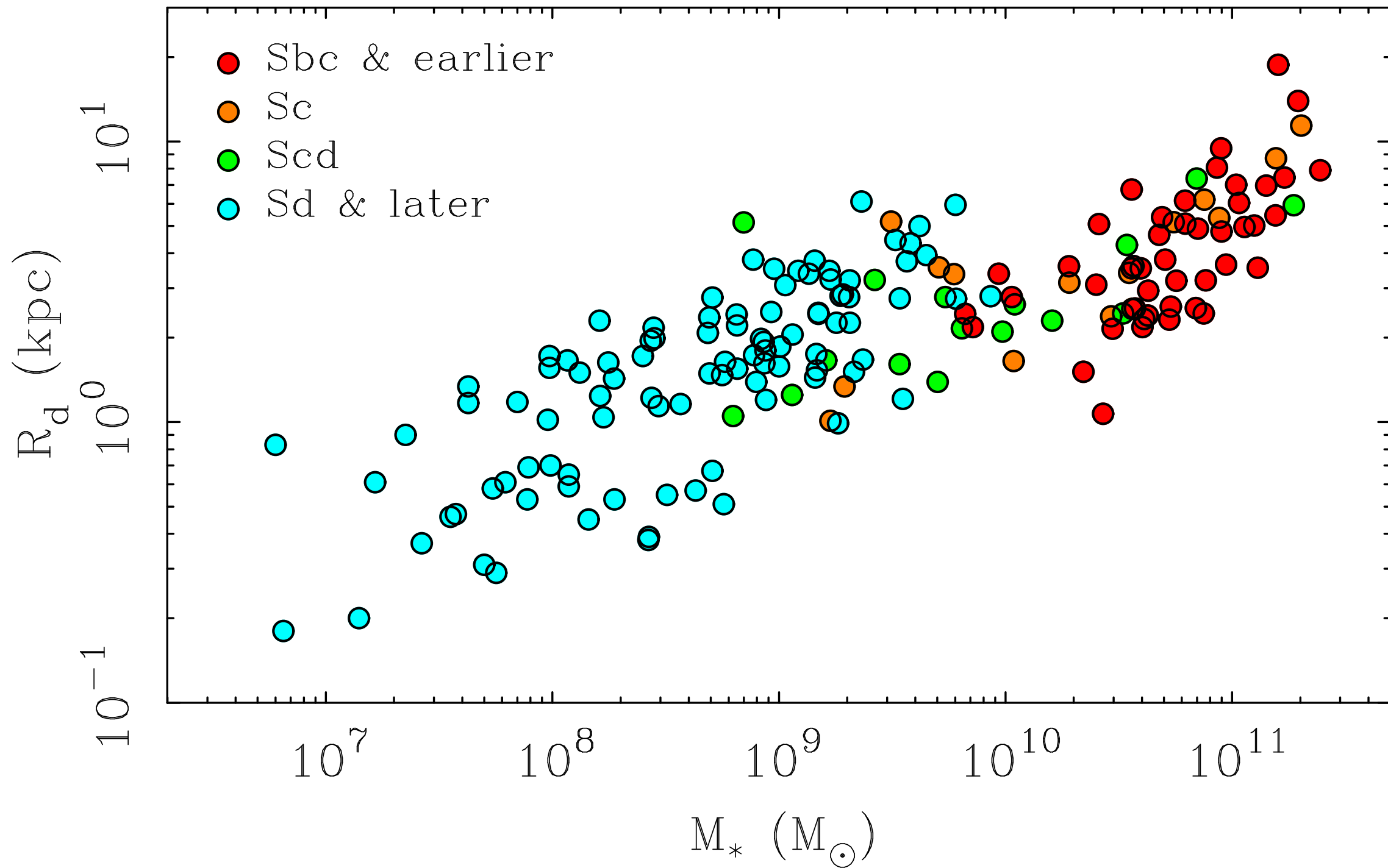


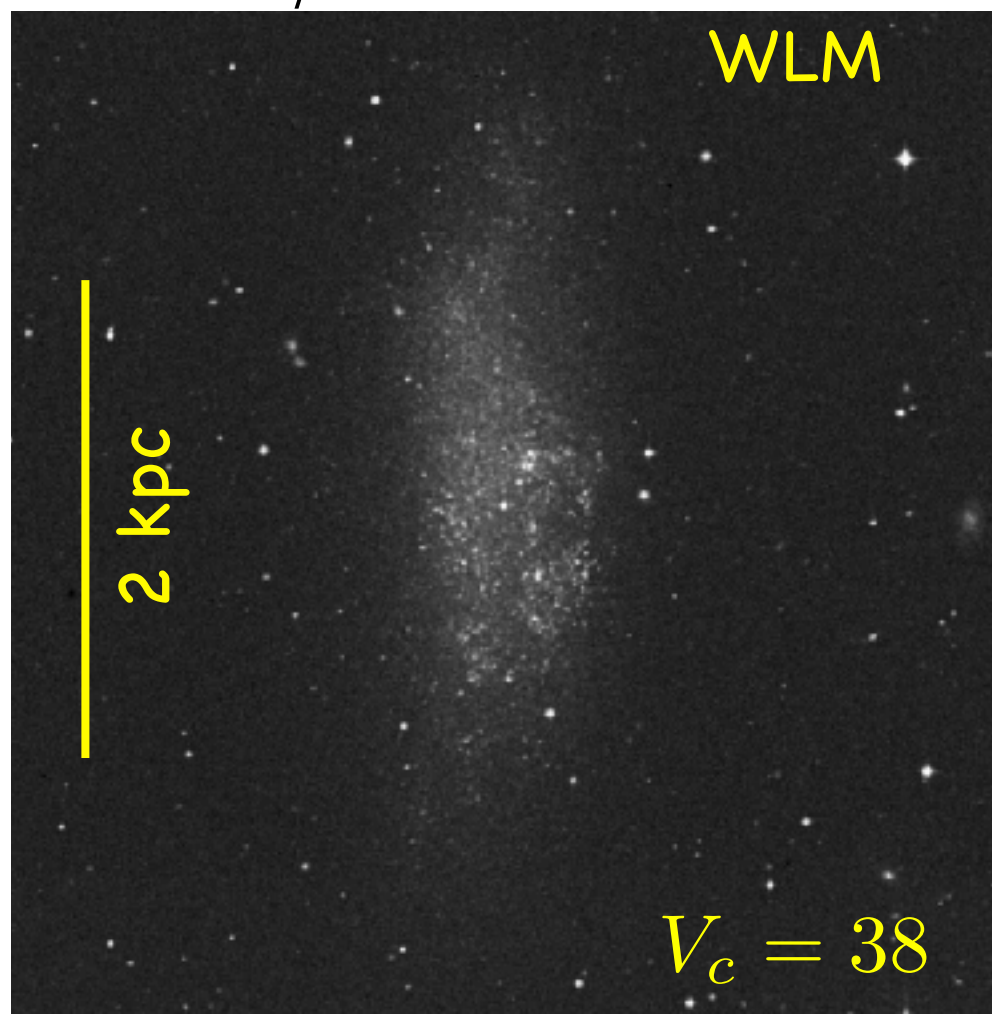
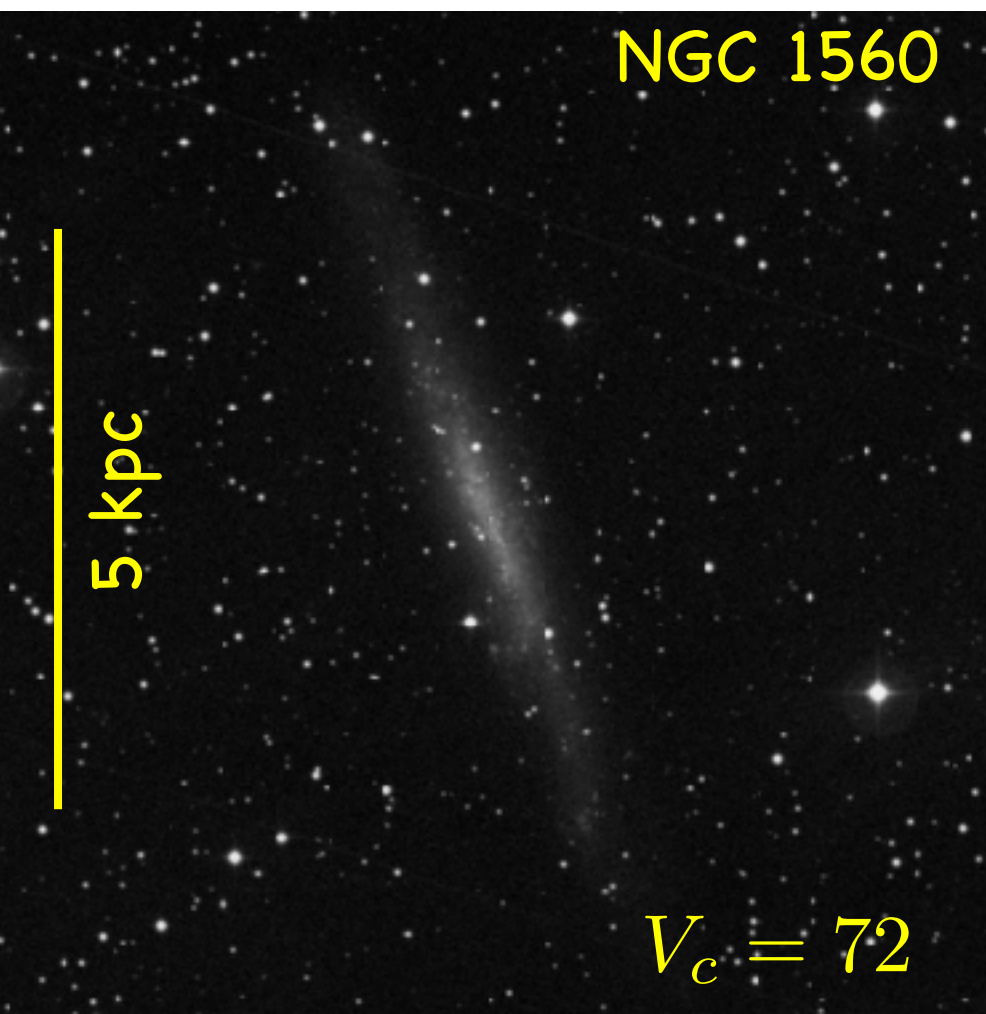
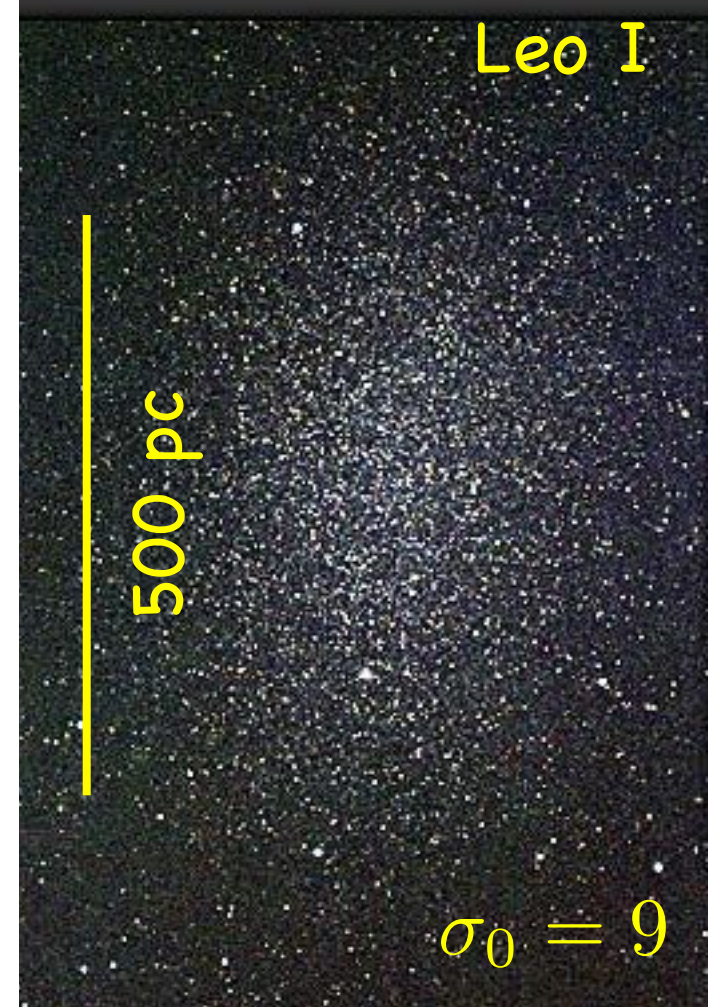
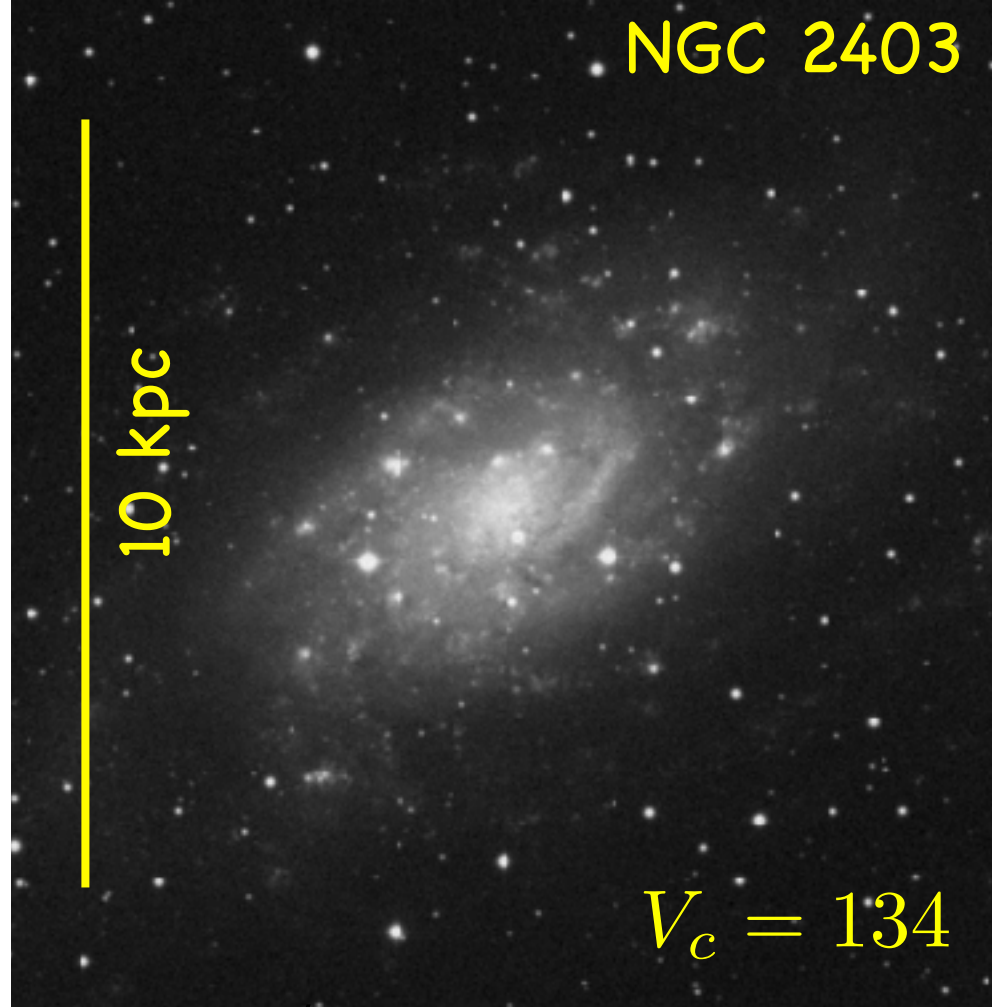
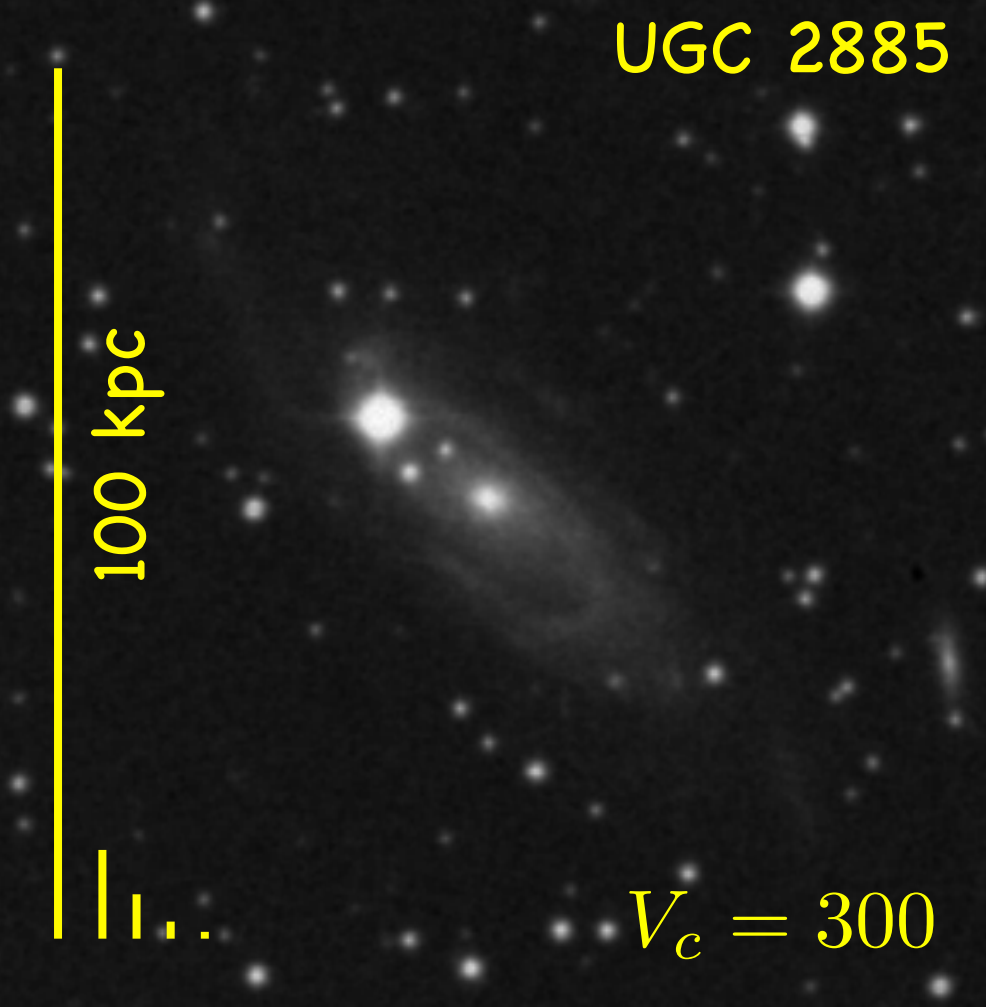
$$\Sigma(R) = \Sigma_0 e^{-R/R_d}$$

Azimuthally averaged light distribution  
approximately exponential for spiral disks.



## Sizes and masses of rotationally supported galaxies







The atomic gas of the ISM is often more extended than the stars

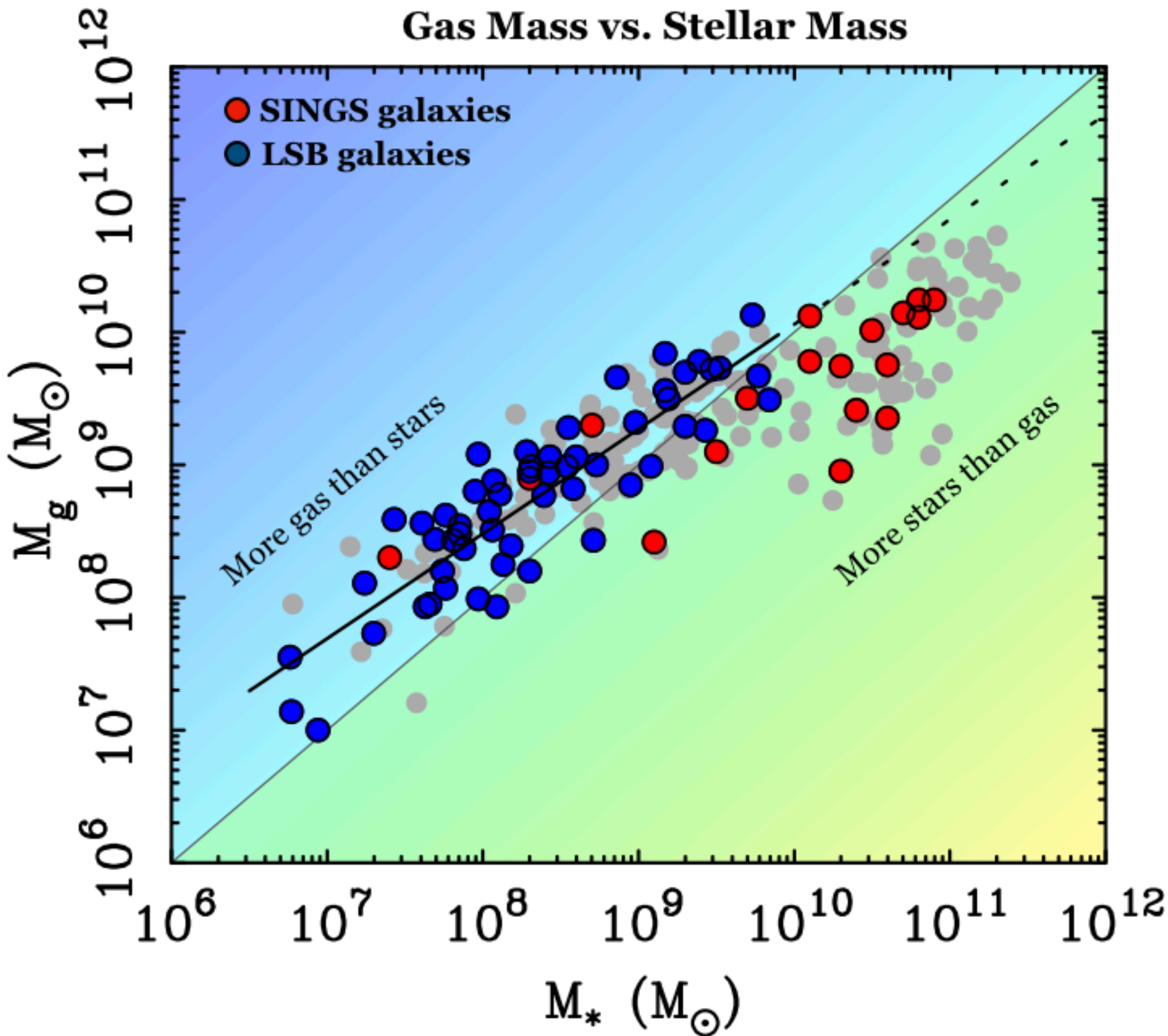
NGC 2403

stars

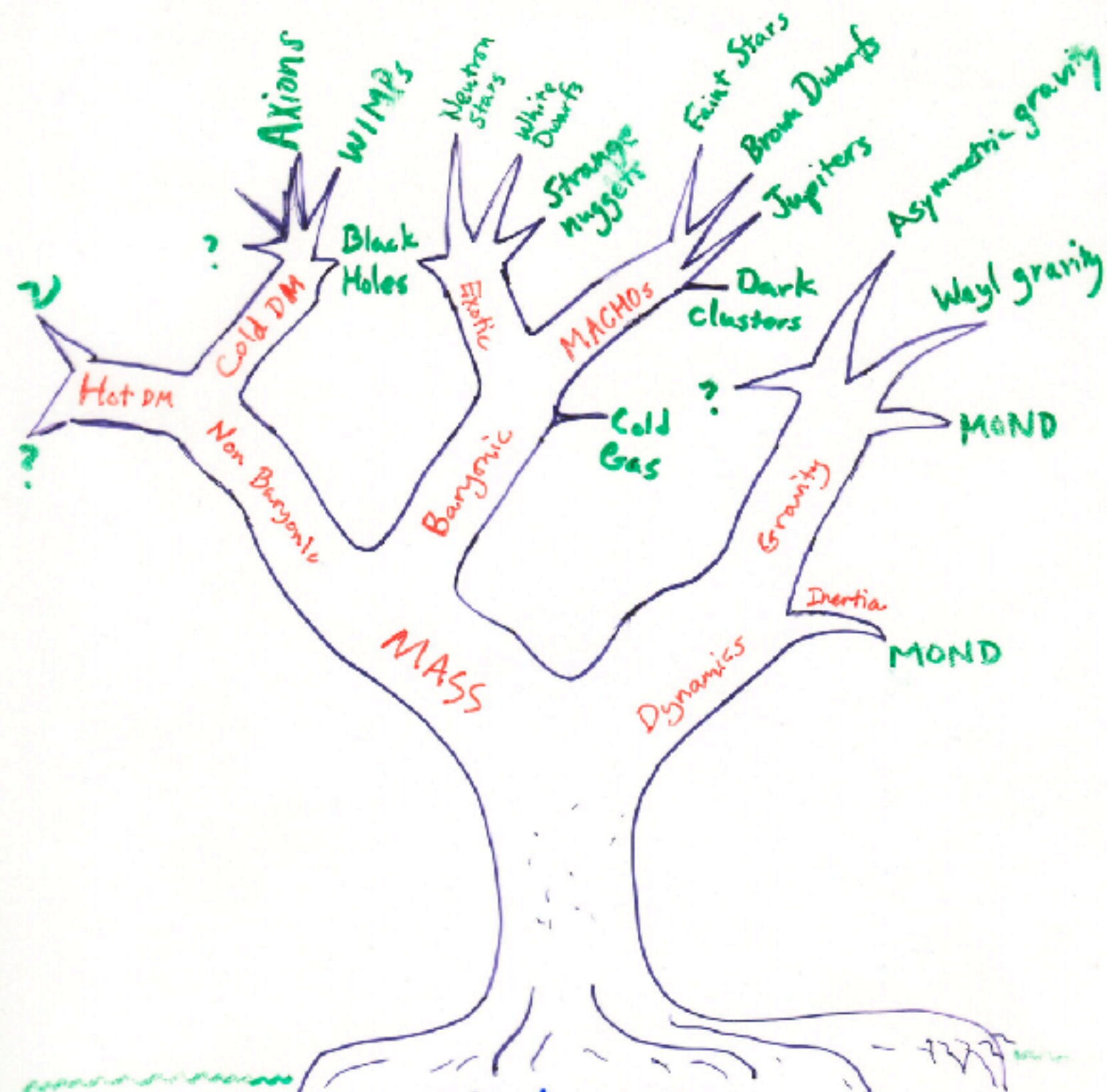
atomic gas

Fraternali, F., Oosterloo, T., Sancisi, R., van Moorsel, G.A. 2001, ApJ, 562, L47

# Rotationally supported galaxies (no Ellipticals)







Disk DM  
Oort  
discrepancy

Spiral  
galaxy  
flat  
rotation  
curves

$$\frac{M_{DM}}{M_T} \approx 0.1$$

Cluster  
Velocity  
dispersions

$$\frac{M_C}{L} \approx 300$$

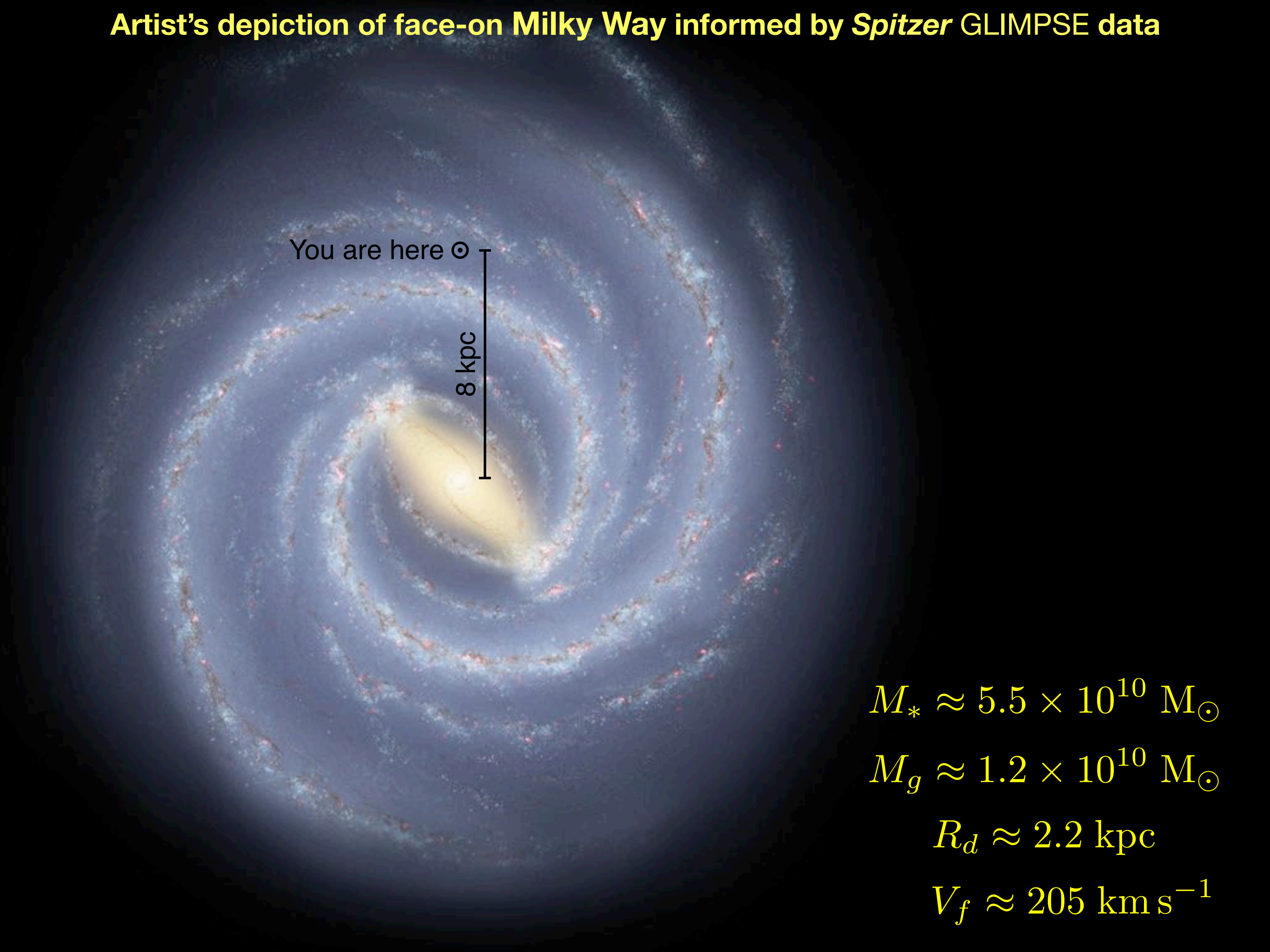
$$\frac{M_X}{M_T} \approx 0.2$$

$\Omega = 1$   
Large  
Scale  
Structure  
Bulk  
flows

## Vertical motion in the Milky Way

the Oort limit

# Artist's depiction of face-on Milky Way informed by *Spitzer* GLIMPSE data



You are here ☉

8 kpc

$$M_* \approx 5.5 \times 10^{10} M_\odot$$

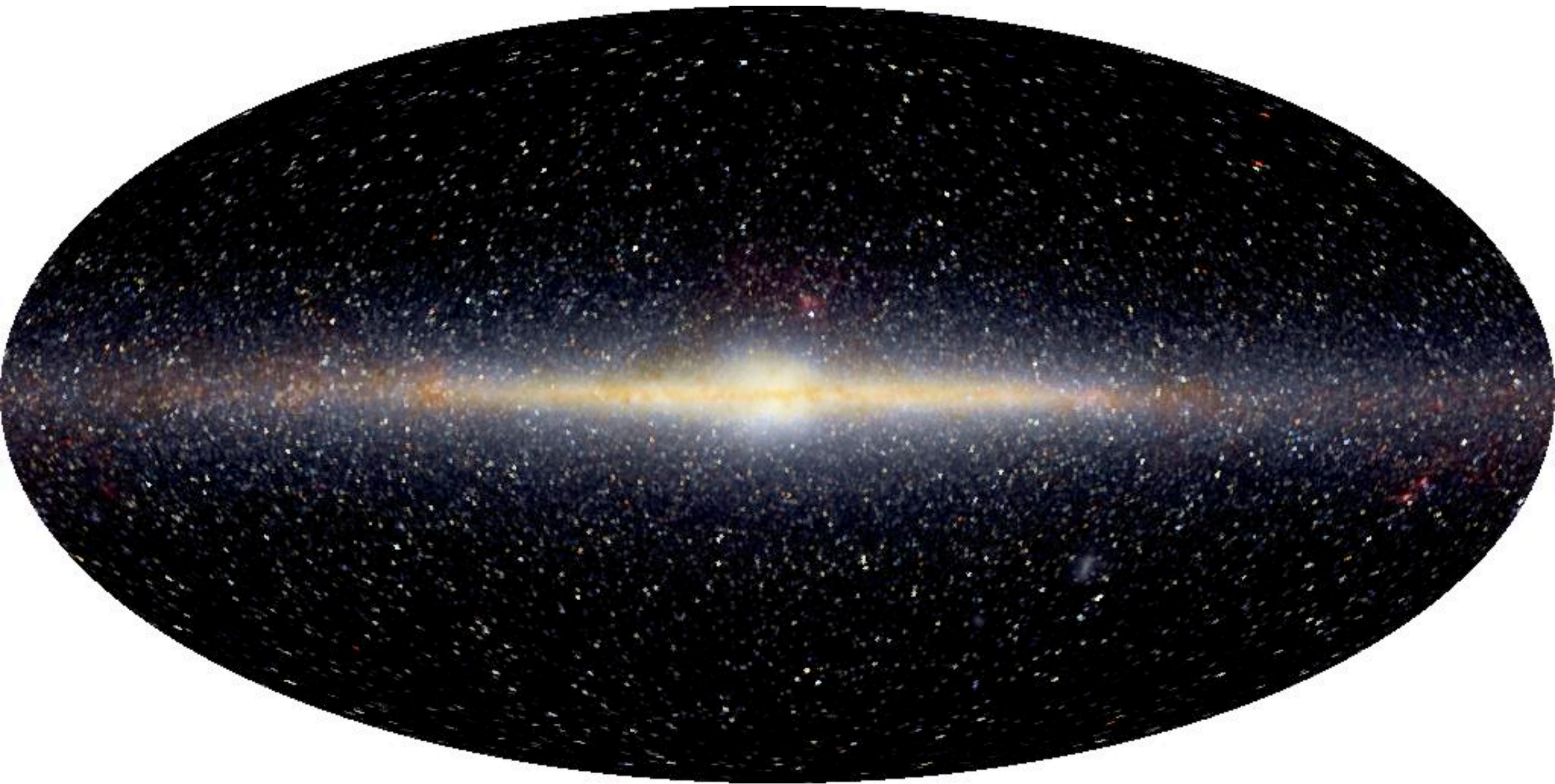
$$M_g \approx 1.2 \times 10^{10} M_\odot$$

$$R_d \approx 2.2 \text{ kpc}$$

$$V_f \approx 205 \text{ km s}^{-1}$$



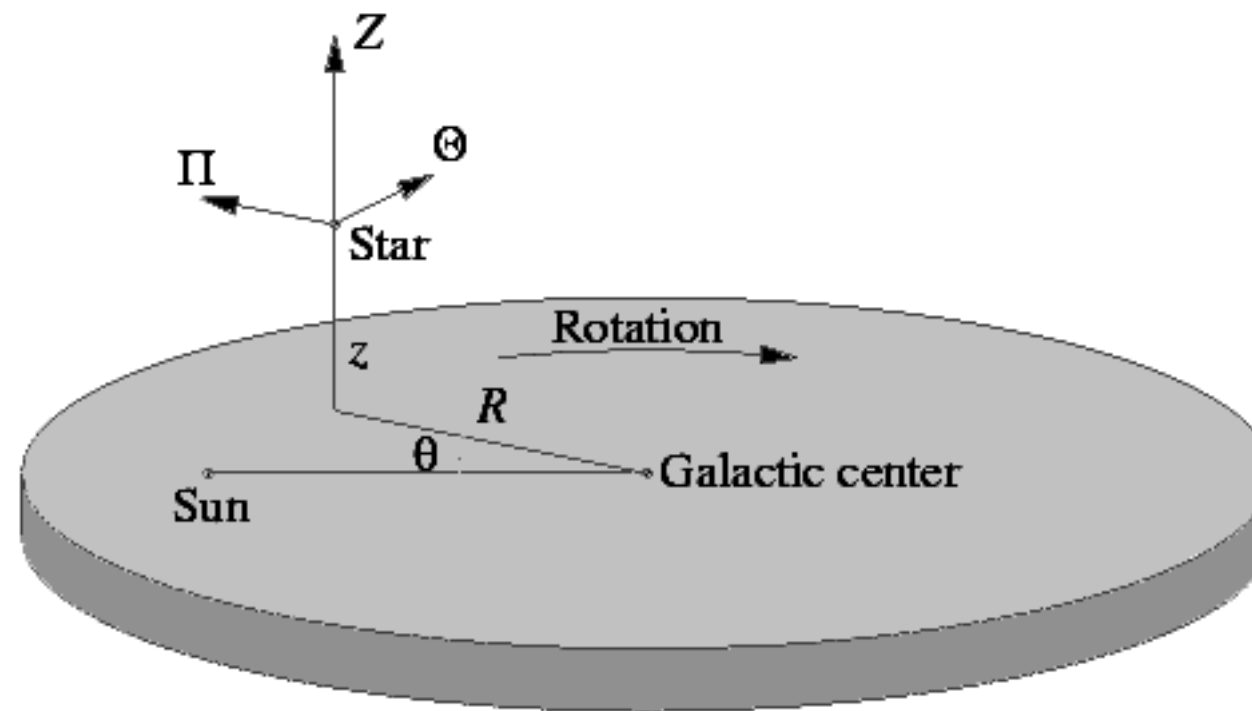
# Milky Way in the near-infrared





# Cylindrical coordinates

Let's define a coordinate system:



Position :  $(R, \theta, z)$

- $R$  = galactocentric distance
- $\theta$  = azimuthal coordinate
- $z$  = height above/below the plane

Velocity :  $(\Pi, \Theta, Z)$

- $\Pi$  = velocity in/out from center
- $\Theta$  = tangential velocity
- $Z$  = velocity up and down

OR  $(X, Y, Z)$  centered on either the sun or the G.C.

# Oort limit - imagine the disk as a plane parallel slab

from Sparke & Gallagher

First, think of balancing KE with PE for a small mass  $m$  orbiting a big mass  $M$ :  $\frac{1}{2}mv^2 \sim \frac{GMm}{r}$

So we can solve for the big mass  $M$ :  $v^2 \sim \frac{2GM}{r}$

Now, instead of a big mass  $M$ , think of a circular patch of radius  $r$  and surface density  $\Sigma$  (in  $M_{\text{sun}}/\text{pc}^2$ ). It has a total mass:  $M \sim \Sigma_0 \pi r^2$

So plug that in and get  $v^2 \sim 2\pi G \Sigma_0 r$

Or, now thinking about a group of stars:  $\sigma_z^2 \sim 2\pi G \Sigma_0 z_0$

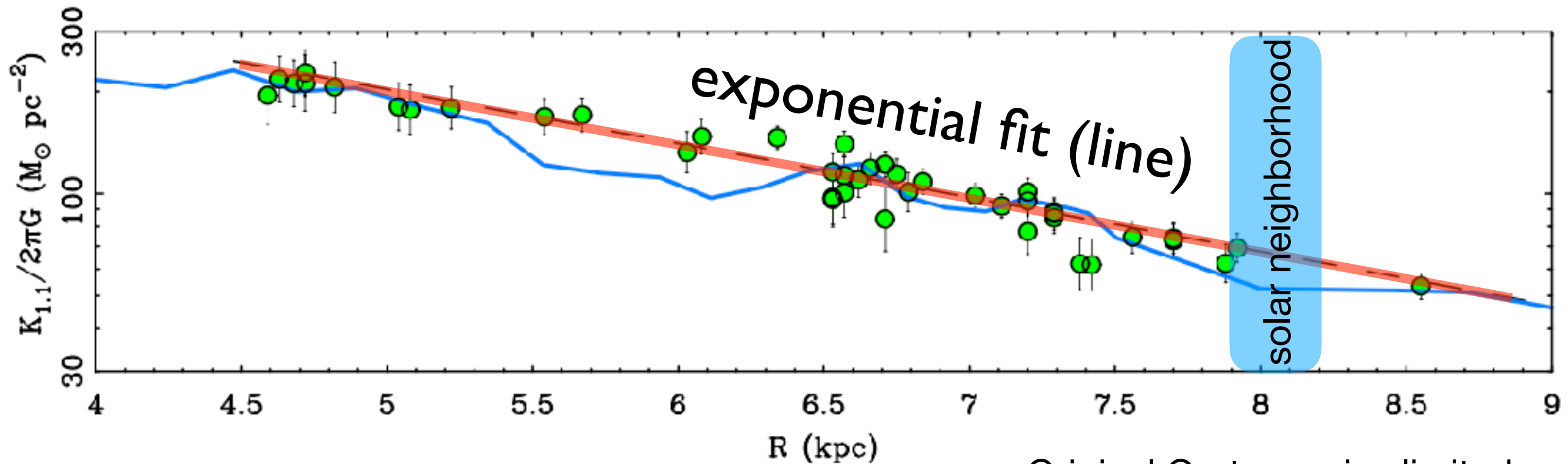
So if we measure velocity dispersions and scale heights for groups of stars, we can measure the mass density of the Galaxy's disk. This was first done in the early 1960s by Jan Oort and is called the **Oort limit**. A recent (and more sophisticated) analysis gives  $\sim 70 M_{\text{sun}}/\text{pc}^2$ .

Now let's just add up all the mass we see:

Stars	$25 M_{\text{sun}}/\text{pc}^2$
Stellar remnants (mostly WDs)	$20 M_{\text{sun}}/\text{pc}^2$
Gas (HI+H2)	$5 M_{\text{sun}}/\text{pc}^2$
<b>Total</b>	<b><math>50 M_{\text{sun}}/\text{pc}^2</math></b>

Are we happy with these sums?

$$K_Z = 2\pi\Sigma + \frac{Z}{R} \frac{\partial V^2}{\partial R}$$



$$\Sigma(R) = \Sigma_\odot e^{-\frac{(R - R_\odot)}{R_d}}$$

Original Oort exercise limited to the solar neighborhood.  
Can now expand to other radii.

$$\Sigma_\odot = 38 M_\odot \text{pc}^{-2} \quad (\text{stars only})$$

$$R_d = 2.15 \text{ kpc} \quad \text{Bovy \& Rix (2013)}$$