

## Stellar Populations

The evolution of individual stars is well understood.

The light produced by a composite population of  $\sim 10^{11}$  stars can get a bit complicated.

We measure light.

For dynamics, we need to know the mass.

For a single burst of star formation (SSP),  
much depends on the IMF (especially the composite  
mass-to-light ratio  $\Upsilon_* = \frac{M_*}{L_*}$ )

IMF = Initial Mass Function

The number of stars that form as a fun of mass

Initial attempt a power law due to Salpeter (1955)

$$\xi(M) = \frac{dN}{dM} = \xi_0 M^{-\Gamma} \quad \Gamma = -2.35$$

"Salpeter slope"

|                  |                     |  |
|------------------|---------------------|--|
| # of stars       | $N = \int \xi dM$   | integral performed over a finite range<br>from the minimum to maximum<br>stellar mass. |
| total mass       | $M = \int M \xi dM$ |  |
| total luminosity | $L = \int L \xi dM$ |  |

$L$  is a strong fun of  $M$ ;  $L \sim M^{3.5}$  for main  
sequence stars.  $L$  goes way up during  
giant phase.

Most of the light is produced by massive stars  
while most of the mass is contained in low mass stars.  
Nevertheless,

$$\Upsilon_* = \frac{M_*}{L} = \frac{\int M \xi dM}{\int L \xi dM} \approx 1 \frac{M_\odot}{L_\odot}$$

$\Upsilon_*$  varies with bandpass and age, but is almost always  $0.5 < \Upsilon_* < 5 \frac{M_\odot}{L_\odot}$

Modified inertia

Note that the Salpeter IMF blows up when integrated to a lower limit  $M_2 \rightarrow 0$ . Usually truncate at  $M_2 \sim 0.1 M_\odot$  (brown dwarf limit)

Subsequent observations

show that the power law is broken (as it must be: Kroupa IMF) so integral is finite.

Numbers of stars peaks somewhere around  $M \approx \frac{1}{3} - \frac{1}{2} M_\odot$

That's just for a simple population in which all the stars form at once.

In spiral galaxies, of must also consider the star formation history (SFH)

The SFH can be viewed as the sum of many individual star forming events. In principle, each event might have its own unique IMF.

Fortunately, galaxies appear to be consistent with a single universal IMF (Kroupa; Chabrier) which may simply result from averaging over many events.

Elaborate models can be made to estimate  $M_*/L$ .

These are good to a factor of  $\sim 2$ .

Hard to do much better (the IMF being the biggest uncertainty, esp. the low mass end.)

Typical values for spiral galaxies

$$\text{Band } \Upsilon_* = \begin{array}{c} \text{B} \quad \text{V} \quad \text{I} \quad \text{K} \quad \text{[3.6]} \\ \hline 1.5 \quad 1.4 \quad 1.2 \quad 0.6 \quad 0.5 \end{array} M_\odot/L_\odot$$

The  $\Upsilon_*$  in the near-infrared (K & [3.6]) is fairly stable and apparently universal. Fluctuations around the mean get larger as one goes to bluer bands.

In practice, build detailed models  
that incorporate known spectra of stars

Major uncertainties

- IMF
- Star formation history

usually modeled as  $SFR \propto e^{-t/\tau}$  \*

E galaxies old: short  $\tau$ : all SF over early on

S galaxies young:  $\tau \rightarrow \infty$ , roughly constant SFR

negligible minor uncertainties

- effect of  $z$ -distribution
- contribution of poorly modeled  
late stages of stellar evolution (TP-AGB)  
Stars

Nevertheless, get decent models like Bell & de Jong (2001)  
Panthari et al (2004)  
Schombert & McGaugh (2014)

\* In addition to smooth, continuous star formation rates  
like

$$SFR \sim e^{-t/\tau}$$

one can also impose sporadic bursts of star formation

$$SFR \sim \delta(t - t_{burst})$$

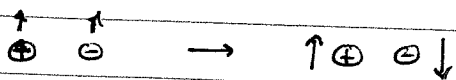
to construct model SFH of arbitrary complexity.

Old ~~stars~~ stars fade, & massive stars fade fast, so most of  
the details of early SFH get washed out.

Modified inertia

HI Atomic gas

detected by spin-flip transition of H



transition frequency very low energy

$$\nu_{10} = \frac{8}{3} g_F \left( \frac{m_e}{m_p} \right) \alpha^2 (cR_H) = 1420.4 \text{ MHz}$$

nuclear g-factor

$g_F = 5.6$  for proton

fine structure constant

$$\alpha = \frac{1}{137}$$

the 21cm line

Rydberg frequency

Emission coefficient

$$A_{ul} = \frac{64 \pi^4 \nu_{ul}^3}{3 h c^3} |\mu_{10}^*|^2$$

numerically

$$A_{10} = 2.85 \times 10^{-15} \text{ s}^{-1}$$

Bohr magneton

(dipole moment of  $e^-$ )

$$|\mu_{10}^*| = \frac{\hbar}{2} \frac{e}{m_e c}$$

radiative half-life

$$\tau_{1/2} = \frac{1}{A_{10}} \approx 11 \times 10^6 \text{ yr} \quad (3.5 \times 10^{14} \text{ s} = 11 \text{ Myr}) = \frac{1}{\tau_{1/2}}$$

Very low critical density

( $\ll 1 \text{ cm}^{-3}$ )

so almost always in LTE through collisional excitation

Can also define "spin temperature"

$$\frac{N_1}{N_0} = \frac{g_1}{g_0} e^{-\frac{h\nu_{10}}{kT}}$$

$g_1 = 3$  upper states

$g_0 = 1$  ground state

Note  $\frac{h\nu}{k} \ll 1 \text{ K}$  very small, so

$$e^{-\frac{h\nu_{10}}{kT}} = 1 \quad \text{if } T_s \approx T$$

$$\text{so } \frac{N_1}{N_0} = \frac{3}{1}$$

$$\& N_H = N_0 + N_1 = 4N_0 \text{ good for counting atoms}$$

anywhere near equilibrium

counting 21 cm photons  $\rightarrow$  counting HI atoms

$$M_{\text{HI}} = \frac{16\pi M_{\text{H}}}{3A_{\text{ul}} hc} D^2 \int F_{\nu} dv$$

flux integral in  $\text{Jy} \cdot \text{km/s}$

Numerically

$$1 \text{ Jansky} = 10^{-26} \text{ W m}^{-2} \text{ Hz}^{-1}$$

$$M_{\text{HI}} = (2.34 \times 10^5 M_{\odot}) D^2 \int F_{\nu} dv$$

$$M_{\text{atomic gas}} = \frac{1}{X} M_{\text{HI}}$$

Can measure HI masses

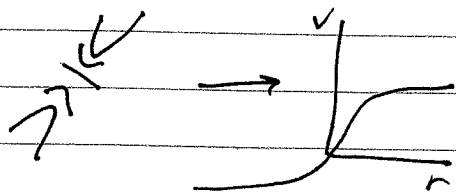
Hydrogen mass fraction

accurately to a few % IF care is taken.

$D$  in Mpc ( $(1+z) \times D_L$  luminosity distance in cosmology) because it's on line

HI emission ALSO gives velocity field from Doppler effect - important tracer of the gravitational potential

Fit velocity field with tilted ring model to obtain rotation curve



modified gravity  
Modified inertia