

A few notional time scales

• crossing time $t_c = \frac{2R}{v}$ $\frac{\text{diameter}}{v \text{ or } \sigma}$

typical time to go from one side of a system to the other

Question: will an O star live many crossing times?

• dynamical time $t_d = \sqrt{\frac{3\pi}{16G\rho}}$

typical orbital time in homogeneous sphere of density ρ

• relaxation time $\frac{t_r}{t_c} = \frac{N}{48f^2} \approx \frac{N}{6 \ln(N/2)}$

↳ N objects carrying a fraction f of the mass

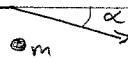
typical time to forget initial conditions

for MW w/ $N \approx 10^{11}$, $t_r \gg$ age of Universe

for GC w/ $N \approx 10^6$, $t_r \approx 10$ Gyr \sim age of Universe

Relaxation is the ^{cumulative} result of many weak gravitational encounters

that only nudge the vector $\alpha = \frac{\Delta v_{\perp}}{v} = \frac{2Gm}{bv^2}$



Strong encounters (w/ $\Delta P.E. \sim K.E.$)

are rare in the solar neighborhood

$t_{\text{strong}} \sim 10^{15}$ yr $\gg U$

Galactic Structure & Kinematics

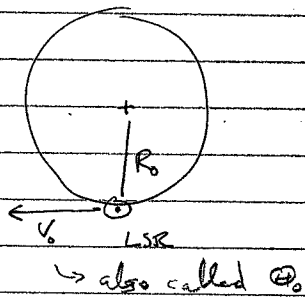
How to find

R ₀ :	V ₀ :
- Centroid of Globular Clusters	- Solar motion wrt G.C.s but do " GCS rotation
- " " Halo tracers (e.g. RR Lyrae)	- Proper motion of Sgr A* (need R ₀ !)
- kinematic v _r = 0 along d = 2R ₀ cos(2l)	- local escape velocity -
- expanding masers @ G.C. R ₀ = 7.9 ± 0.8 kpc	V _{esc} ≈ √2 V _c (√2 depends on details of the mass model)
	sharp cut-off in # stars with v > V _c + 63 km/s

Galactic Constants

V₀, R₀

R₀ = distance to Galactic Center
 ≈ 8 kpc ± 0.5 all systematics
 7.9-8.3 recently



V₀ = orbital velocity of LSR
 ≈ 230 km s⁻¹ ± 20 all systematics
 official IAU values 220, 8.5 for many years

angular velocity of LSR now pretty well known from proper motion of Sgr A*

$$\Omega_0 = \frac{V_0}{R_0} \approx 30 \text{ km s}^{-1} \text{ kpc}^{-1} \pm 0.5 \text{ or so}$$

measured with VLBA long after IAU values were set

Oort constants

- A local shear (differential rotation)
 - B vorticity (spin or circulation of local fluid element)
- A ≈ 15 km s⁻¹ kpc⁻¹; B ≈ -13 km s⁻¹ kpc⁻¹

K epicyclic frequency
 K ≈ 37 km s⁻¹ kpc⁻¹

Also C & D ≈ 3 km s⁻¹ kpc⁻¹
 for non-axis-symmetric potentials e.g. the Galactic Bar