# DARK MATTER

ASTR 333/433

### <u>TODAY</u> Modified Gravity MOND





"No competent thinker, with the whole of the available evidence before him, can now, it is safe to say, maintain any single nebula to be a star system of coordinate rank with the Milky Way. A practical certainty has been attained that the entire contents, stellar and nebular, of the sphere belong to one mighty aggregation" [i.e., the Milky Way]

- Agnes Mary Clerke (1890)

Popular History of Astronomy during the Nineteenth Century

There is never a result in cosmology that it so secure that it cannot turn out to be completely wrong



The existence of dark matter has attained a practical certainty

or maybe we've been using the wrong equation

Recall our empirical laws - these are true in the data irrespective of their interpretation

• Flat rotation curves (Rubin-Bosma Law)

Rotation curves tend asymptotically towards a constant rotation velocity that persists to indefinitely large radii:  $V(R \to \infty) \to V_f$ 

- Tully-Fisher relation (Luminous, Stellar Mass, and Baryonic TF relations) The baryonic mass of galaxies scales as the fourth power of the flat rotation velocity:  $M_b = AV_f^4$
- Central density relation (lower surface brightness galaxies exhibit larger mass discrepancies) The central dynamical surface densities of galaxies is related to their central surface brightnesses:  $\Sigma_{dyn}(R \to 0) = f[\Sigma_*(R \to 0)]$
- Renzo's rule (Sancisi's Law)

"For any feature in the luminosity profile there is a corresponding feature in the rotation curve and vice versa." (Sancisi 2004).

• Radial acceleration relation

The observed centripetal acceleration is related to that predicted by the observed distribution of baryons:

$$g_{\rm obs} = \mathcal{F}(g_{\rm bar})$$

Over 25 decades in acceleration, galaxies only exist around 1 Å/s/s

Empirical laws are connected by this common acceleration scale



Not any theory will do - length scale based modifications can be immediately excluded as the discrepancy does not appear at a particular length scale.







There is no unique size scale in the data. Can generically exclude any modification of gravity where a change in the force law appears at a specific length scale [e.g., f(R) gravity].

Equivalent to the Radial Acceleration Relation



There is a characteristic acceleration scale in the data

#### MOND

Modified Newtonian Dynamics (Milgrom 1983)

Instead of invoking dark matter, modify gravity (or inertia). Milgrom suggested a modification at a particular acceleration scale  $a_0$  ARBITRAR

GRAVI

# $\frac{\text{Newtonian regime}}{a = g_N \text{ for } a \gg a_0} \qquad \qquad \frac{\text{MOND regime}}{a = \sqrt{g_N a_0} \text{ for } a \ll a_0}$

MOND regime invariant under transformations  $(t, \mathbf{x}) \rightarrow \lambda(t, \mathbf{x})$ 

http://www.scholarpedia.org/article/The\_MOND\_paradigm\_of\_modified\_dynamics

Regimes smoothly joined by

$$\mu\left(\frac{a}{a_0}\right)a = g_N$$

$$\mu(x) \to 1 \text{ for } x \gg 1$$

$$\mu(x) \to x \text{ for } x \ll 1 \qquad \qquad x = \frac{a}{a_0}$$

### Modified Poisson equation

$$\nabla \left[ \mu \left( \frac{\nabla \Phi}{a_0} \right) \nabla \Phi \right] = 4\pi G \rho$$

Derived from aquadratic Lagrangian of Bekenstein & Milgrom (1984) to satisfy energy conservation. ApJ, 270, 381

Milgrom 1983

No. 2, 1983

MODIFICATION OF NEWTONIAN DYNAMICS A major step in understanding ellipticals can be made if we can identify them, at least approximately, with idealized structures such as the FRCL spheres discussed above. I have also studied isotropic and nonisotropic isothermal spheres, in the modified dynamics, as such possible structures. I found that they have properties which reemble those galacti

#### VIII. PREDICTIONS

The main predictions conce low's.

Velocity curves calculate, with the modified dynamics on the basis of the observed mass in galaxies should agree with the observed curves. Elliptical and SO galaxies may be the best for this purpose since (a)practically no uncertainty due to obscuration is involved and (b) there is not much uncertainty due to the possible presence of molecular hydrogen.

2. The relation between the asymptotic velocity  $(V_{\infty})$ and the mass of the galaxy (M)  $(V_{\infty}^4 = MGa_0)$  is an absolute one.

3. Analysis of the z-dynamics in disk galaxies using the modified dynamics should yield surf densitie which same vield a discrepancy which increases with radius in a predictable manner.

4. Effects of the m be particularly stro review of property s s 1980). For example, those dwarfs believed to be bound to our Galaxy would have internal accelerations typically of order  $a_{in} \sim a_0/30$ . Their (modified) acceleration. g, in the field of the Galaxy is larger than the internal ones but still much smaller than  $a_0, g \approx (8$ kpc/d) $a_0$ , based on a value of  $V_{\infty} = 220 \text{ km s}^{-1}$  for the Galaxy, and where d is the distance from the dwarf galaxy to the center of the Milky Way ( $d \sim 70-220$ kpc). Whichever way the external acceleration turns out to affect the internal dynamics (see the discussion at the end of § II, the section on small groups in Paper III, and Paper I), we predict that when velocity dispersion data is available for the dwarfs, a large mass discrepancy will result when the conventional dynamics is used to determine the masses. The dynamically determined mass is predicted to be larger by a factor of order 10 or more than that which can be accounted for by stars. In case the internal dynamics is determined by the external acceleration, we predict this factor to increase with dand be of order (d/8 kpc) (as long as  $a_{in} \ll g$ ,  $h_{50} = 1$ ).

Prediction 1 is a very general one. It is worthwhile listing some of its consequences as separate predictions. numbered 5-7 below (note that, in fact, even prediction 2 is already contained in prediction 1).

5. Measuring local M/L values in disk galaxies (assuming conventional dynamics) should give the following results: In regions of the galaxy where  $V^2/r \gg a_0$ the local M/L values should show no indication of hidden mass. At a certain transition radius, local M/Lshould start to increase rapidly. The transition radius

381

canoration of M/L as we are concerned only with variations of this quantity; (b) Effects of the modified dynamics manifest themselve more clearly in lo

ior in the isk only while the spheroid can be neglected. This makes the determination of mass from velocity more certain.

6. Disk galaxies with low surface brightness provide particularly strong tests (a study of a sample of such galaxies is described by Strom 1982 and by Romanishin et al. 1982). As low surface brightness means small accelerations, the effects of the modification should be more noticeable in such galaxies. We predict, for example, that the proportionality factor in the  $M \propto V_{\pi}^4$  relation for these galaxies is the same as for the high surface density grinxies. In to trast, if one was relation:  $V_{\infty}^{4}$  (i.e. for example, Aaronson, Huchra, and would  $\Sigma = V_{\infty}$  (re. for example, Autonson, fractions brightness, 1979), where  $\Sigma$  is the average surface brightness, implies that low surface lens  $\nabla$  ga ky s, of  $\omega$ the fight of the surface lens  $\nabla$  ga ky s, of  $\omega$ is low fight of the surface density gal sur-iation delived for normal surface density gal su-We also predict that the lower the average surface of a galaxy is, the smaller density le g . S at the average set acceler lity small we may have contact in which  $V^2/r < a_0$ 

everywhere, and analysis with conventional dynamics should yield local M/L values starting to increase from verv small radii. 7. As the study of model rotation curves shows, we

predict a correlation between the value of the average surface density (or brightness) of a galaxy and the steepness with which the rotational velocity rises to its asymptotic value (as measured, for example, by the radius at which  $V = V_{\infty}/2$  in units of the scale length of the disk). Small surface densities imply slow rise of V.

#### IX. DISCUSSION

The main results of this paper can be summarized by the statement that the modified dynamics eliminates the need to assume hidden mass in galaxies. The effects in galaxies which I have considered, and which are commonly attributed to such hidden mass, are readily explained by the modification. More specifically:

## MOND predictions

The Tully-Fisher Relation

 Surface brightness
 Normalization = 1/(a<sub>0</sub>G)
 Surface brightness
 Surface brightness
 Surface brightness Mass and V<sub>flat</sub>

No Dependence on Surface Brightness

• Dependence of conventional M/L on radius **ddt** An Gyff of Trentress **1983** ess. This Carve Shapes dely to exist. Surface Density ~ Surface Brightness

- **Detailed Rotation Curve Fits**
- Stellar Population Mass-to-Light Ratios



- The Tully-Fisher Relation
  - Slope = 4
     Normalization = 1/(a<sub>0</sub>G)
     Fundamentally a relation between Disk Mass and V<sub>flat</sub>
     No Dependence on Surface Brightness
- Dependence of conventional M/L on radius and surface brightness
- Rotation Curve Shapes
- Surface Density ~ Surface Brightness
- Detailed Rotation Curve Fits
- Stellar Population Mass-to-Light Ratios

### In MOND limit of low acceleration

$$a = \sqrt{g_N a_0}$$

$$\frac{V^2}{R} = \sqrt{\frac{GM}{R^2}} a_0$$

Simple (point mass) example: note that radial dependence cancels; squaring both sides gives TF relation:

$$V^4 = a_0 G M$$

In general (not a point mass):

$$M_b = AV_f^4$$
 with  $A = \frac{\zeta}{a_0 G}$ 

where

 $\zeta \approx 0.8$ 

for disk galaxies of finite thickness (recall that flattened mass distributions rotate faster than their spherical equivalent)



• The Tully-Fisher Relation

Slope = 4
 Normalization = 1/(a<sub>0</sub>G)
 Fundamentally a relation between Disk Mass and V<sub>flat</sub>
 No Dependence on Surface Brightness

- Dependence of conventional M/L on radius and surface brightness
- Rotation Curve Shapes
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#### Why? Physics of the BTFR scaling relation

#### dark matter

halos:  $M_{tot} \propto V^3$ 

baryons:  $M_d \propto V^x$ 

 $x \geq 3$  depending on  $m_d(V)$ 

Should depend on disk scale length, unless all disks submaximal

Should work as long as object not tidally disrupted

 $\begin{array}{l} \underline{\text{MOND}}\\ M_{tot} = M_b = \frac{V^4}{a_0 G}\\ \text{an absolute consequence}\\ \text{of the force law for a << a_0:}\\ g_N = \mu \left(\frac{g}{a_0}\right)g\\ \text{Newtonian regime:}\\ \mu \to 1 \ \text{for }g \gg a_0 \ \text{so }g = g_N \end{array}$ 

MOND regime:  $\mu \to g/a_0 \text{ for } g \ll a_0 \text{ so } g = \sqrt{g_N a_0}$ 

Should only work for objects in MOND regime

• The Tully-Fisher Relation













MOND naturally explains Renzo's Rule

NGC 1560

![](_page_18_Figure_2.jpeg)

reflected in the kinematics, even though dark matter should be totally dominant.

MOND fits are equivalent to choosing  $M^*/L$  to place galaxies on the RAR (Li et al. 2018)

![](_page_19_Figure_1.jpeg)

![](_page_20_Figure_0.jpeg)

![](_page_21_Figure_0.jpeg)

![](_page_22_Figure_0.jpeg)

![](_page_23_Figure_0.jpeg)

![](_page_24_Figure_0.jpeg)

![](_page_25_Figure_0.jpeg)

![](_page_26_Figure_0.jpeg)

![](_page_27_Figure_0.jpeg)

![](_page_28_Figure_0.jpeg)

Band: stellar population model

![](_page_28_Figure_2.jpeg)

• The Tully-Fisher Relation

![](_page_28_Figure_5.jpeg)

- **P** Rotation Curve Shapes
- Surface Density ~ Surface Brightness
- Detailed Rotation Curve Fits
- Stellar Population Mass-to-Light Ratios

Prediction	Test Positive?	A Priori?
MASR (Tully-Fisher)		
1. Normalization	Yes	No
2. Slope	Yes	No
3. Mass & Asymptotic Speed	Yes	Yes
4. Surface Brightness Independence	Yes	Yes
Rotation Curves		
5. Flat Rotation Curves	Yes	No
<ol> <li>Acceleration Discrepancy</li> </ol>	Yes	Yes
7. Rotation Curve Shapes	Yes	Yes
<ol> <li>Surface Brightness &amp; Density</li> </ol>	Yes	Yes
9. Detailed Fits	Yes	No
<ol> <li>Stellar Population Y<sub>*</sub></li> </ol>	Yes	—
11. Feature Correspondence	Yes	—
Disk Stability		
12. Freeman Limit	Yes	No
<ol> <li>13. Vertical Velocity Dispersions</li> </ol>	?	No
14. LSB Galaxy Morphology	Yes	Yes

Table 1. MOND Predictions & Tests.