

DARK MATTER

ASTR 333/433

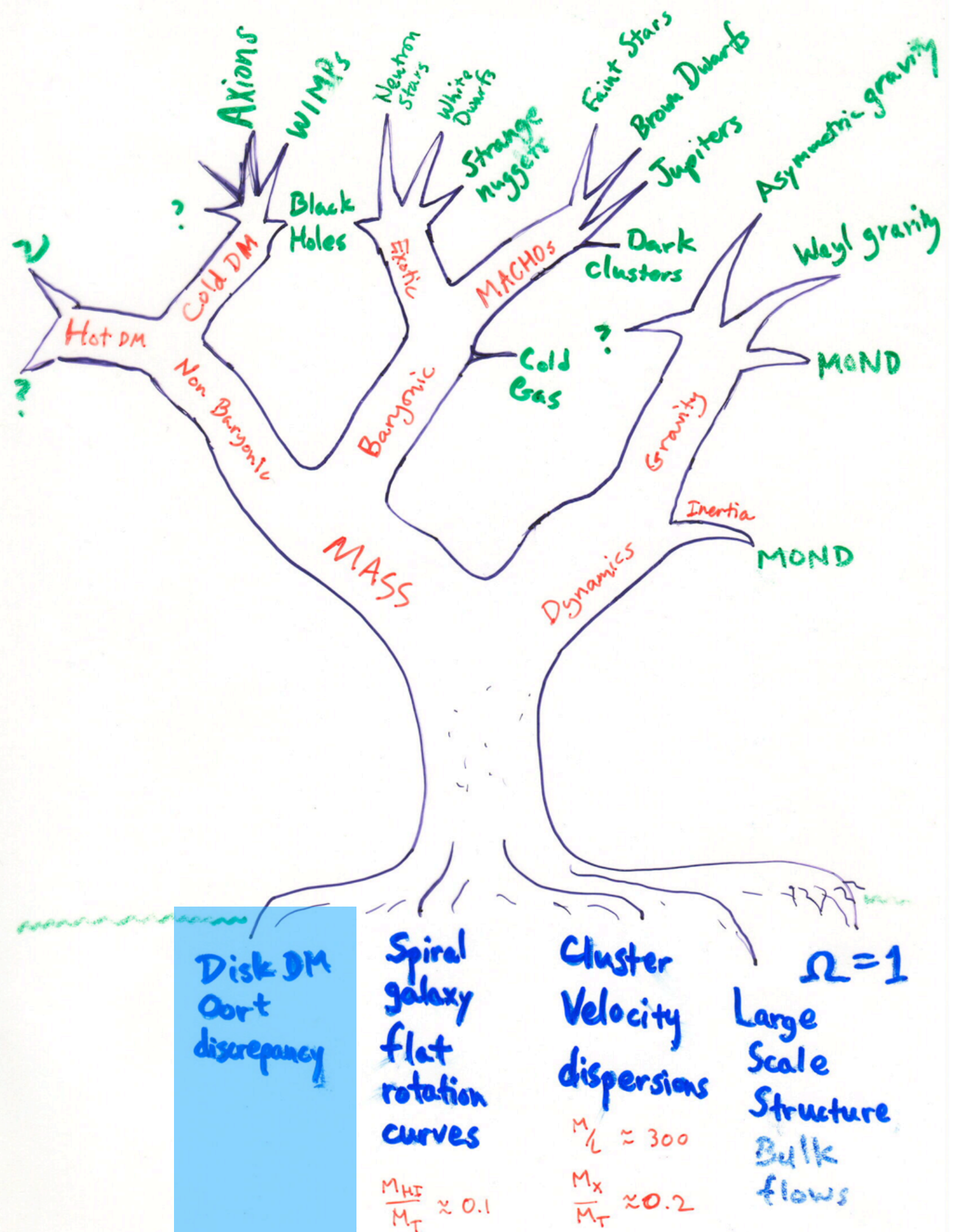
TODAY

Vertical motion in the Milky Way

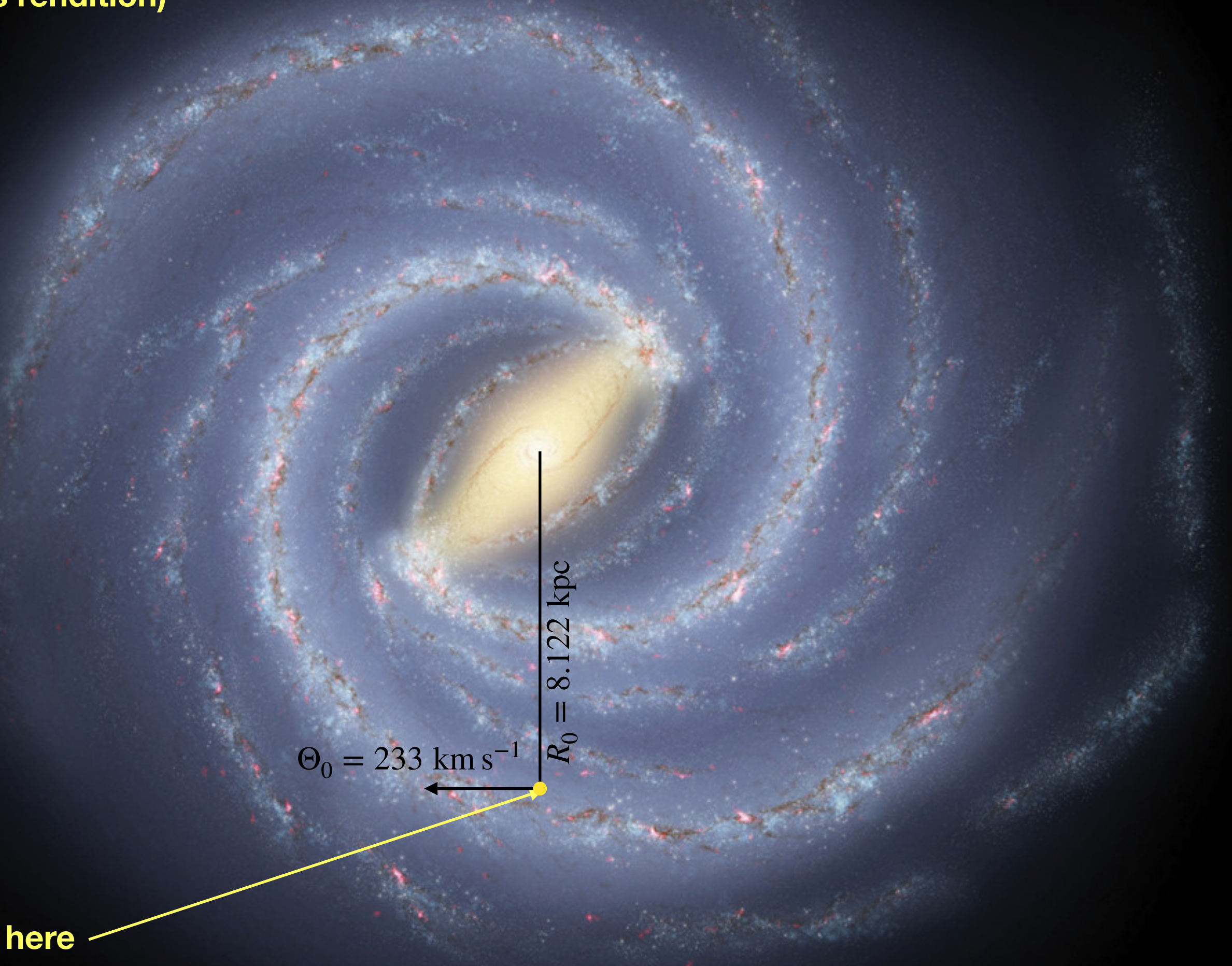
the Oort limit

The Bar Instability

Ostriker & Peebles; Sellwood



Milky Way
(artist's rendition)



$\Theta_0 = 233 \text{ km s}^{-1}$

$R_0 = 8.122 \text{ kpc}$

You are here



Oort limit - imagine the disk as a plane parallel slab

from Sparke & Gallagher

First, think of balancing KE with PE for a small mass m orbiting a big mass M : $\frac{1}{2}mv^2 \sim \frac{GMm}{r}$

So we can solve for the big mass M : $v^2 \sim \frac{2GM}{r}$

Now, instead of a big mass M , think of a circular patch of radius r and surface density Σ (in $M_{\text{sun}}/\text{pc}^2$). It has a total mass: $M \sim \Sigma_0 \pi r^2$

So plug that in and get $v^2 \sim 2\pi G \Sigma_0 r$

Or, now thinking about a group of stars: $\sigma_z^2 \sim 2\pi G \Sigma_0 z_0$

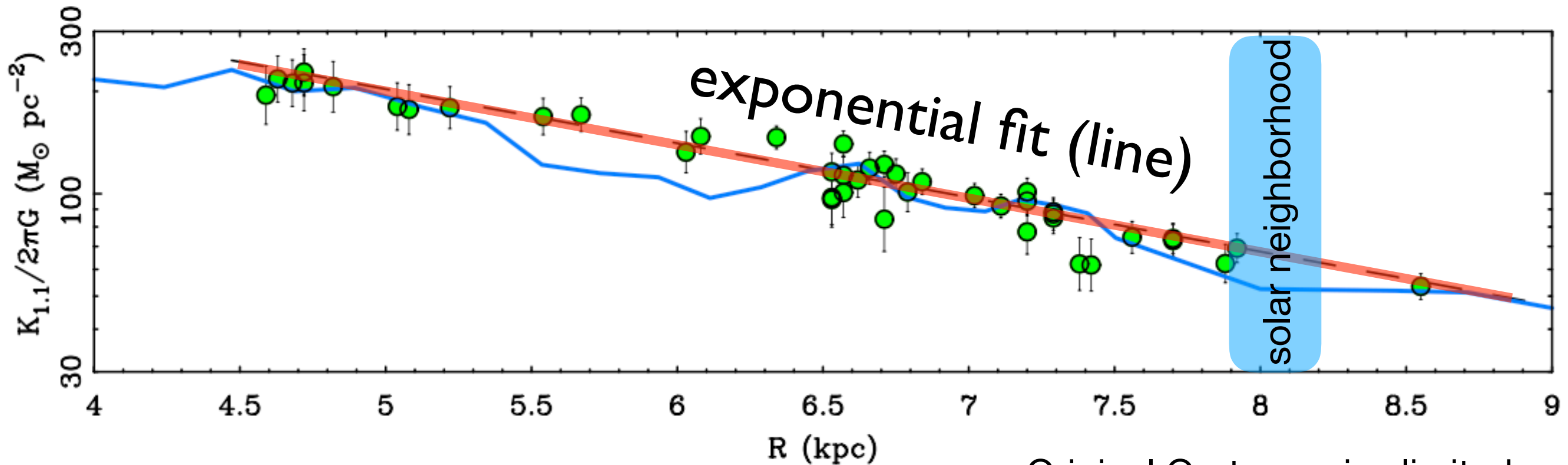
So if we measure velocity dispersions and scale heights for groups of stars, we can measure the mass density of the Galaxy's disk. This was first done in the early 1960s by Jan Oort and is called the **Oort limit**. A recent (and more sophisticated) analysis gives $\sim 70 M_{\text{sun}}/\text{pc}^2$.

Now let's just add up all the mass we see:

Stars	$25 M_{\text{sun}}/\text{pc}^2$
Stellar remnants (mostly WDs)	$20 M_{\text{sun}}/\text{pc}^2$
Gas (HI+H2)	$5 M_{\text{sun}}/\text{pc}^2$
Total	$50 M_{\text{sun}}/\text{pc}^2$

Are we happy with these sums?

$$K_Z = 2\pi G \Sigma + \frac{Z}{R} \frac{\partial V^2}{\partial R}$$



$$\Sigma(R) = \Sigma_{\odot} e^{-\frac{(R - R_{\odot})}{R_d}}$$

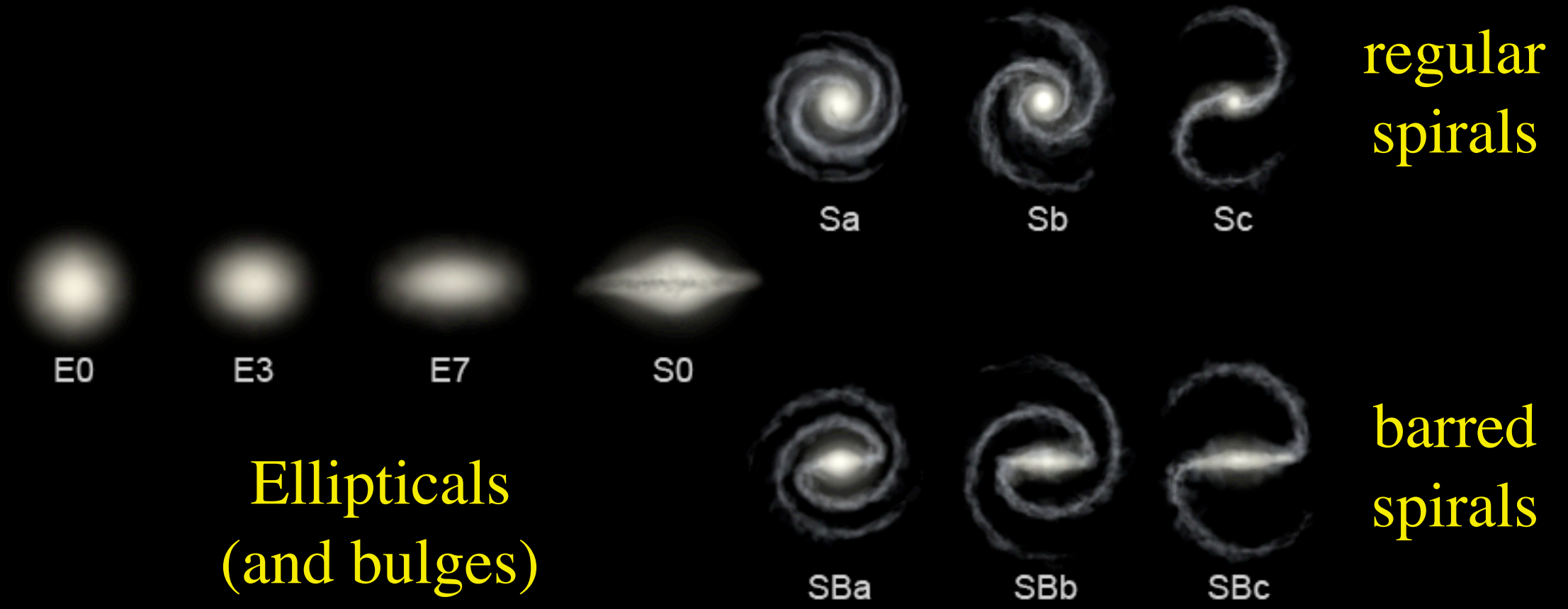
Original Oort exercise limited to the solar neighborhood.
Can now expand to other radii.

$$\Sigma_{\odot} = 38 M_{\odot} \text{pc}^{-2} \quad (\text{stars only})$$

$$R_d = 2.15 \text{ kpc} \quad \text{Bovy \& Rix (2013)}$$

Galaxy Morphology

The Hubble Tuning-fork sequence



Ellipticals
(and bulges)
3D ellipsoids
pressure support
 V/σ small

Spirals
2D disks
rotational support
 V/σ large

NGC 628: a spiral galaxy



NGC 1300: a barred spiral galaxy



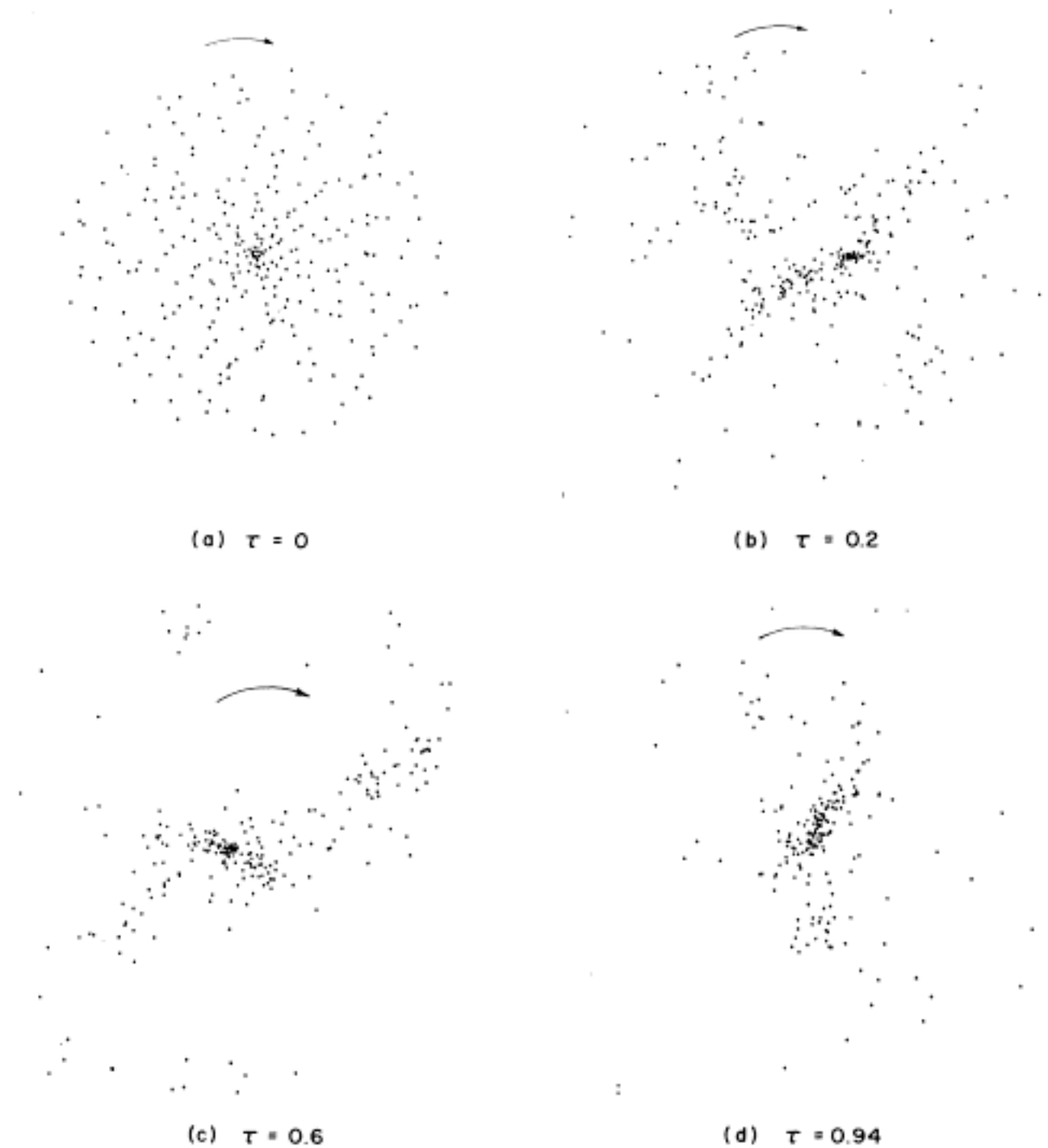
The Bar Instability

Spiral disks unstable to the development of $m=2$ bar modes.

Left to themselves, spiral disks fall apart in just a few dynamical times (< 1 Gyr for the Milky Way).

Ostriker & Peebles (1973)

Sellwood (2016)

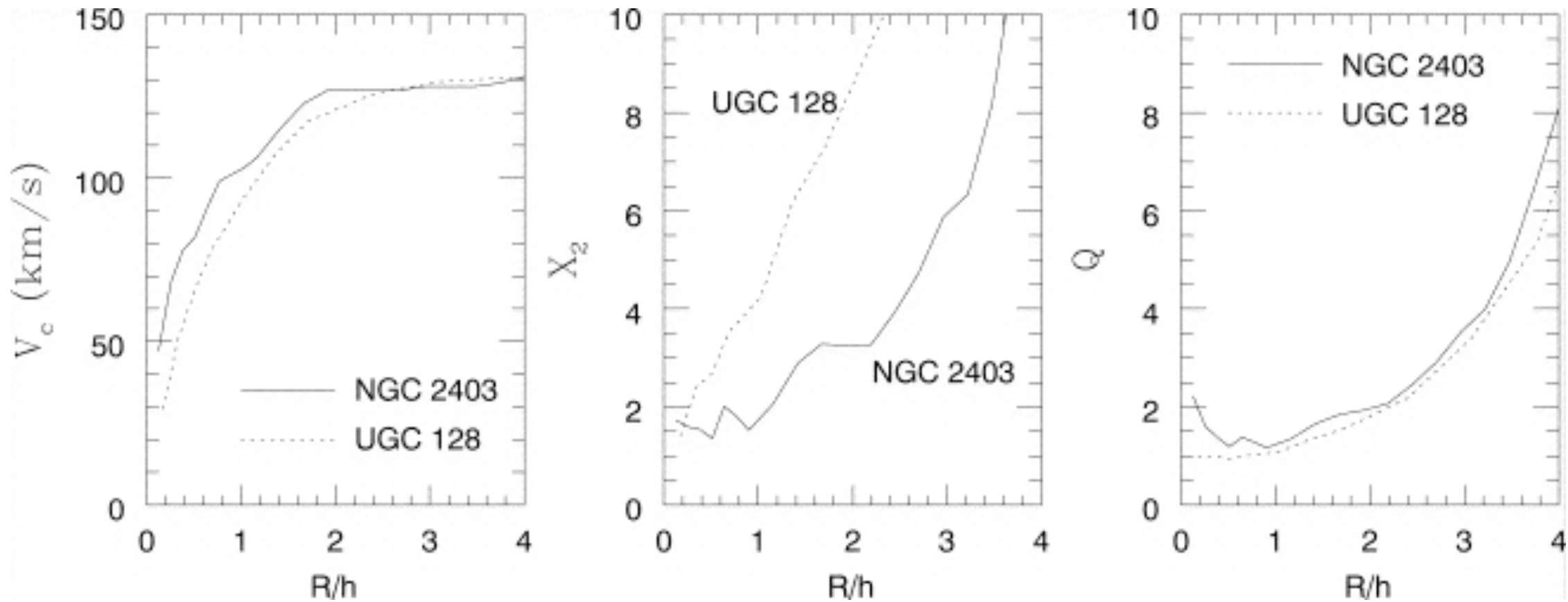


<http://burro.astr.cwru.edu/Academics/Astr222/Galaxies/Spiral/nohalo.mpg>

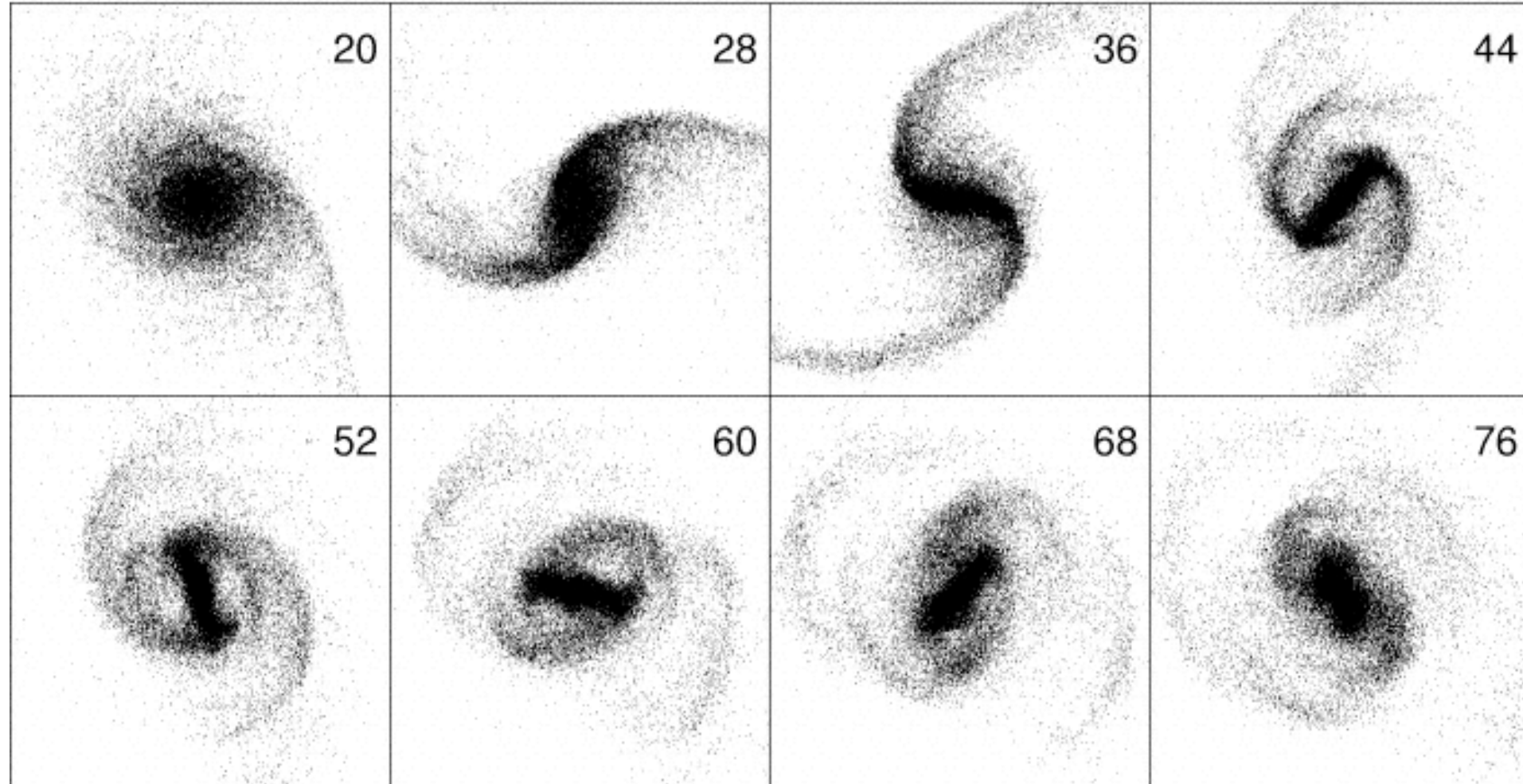
<http://burro.astr.cwru.edu/Academics/Astr222/Galaxies/Spiral/halo.mpg>

NGC 2403: high surface brightness

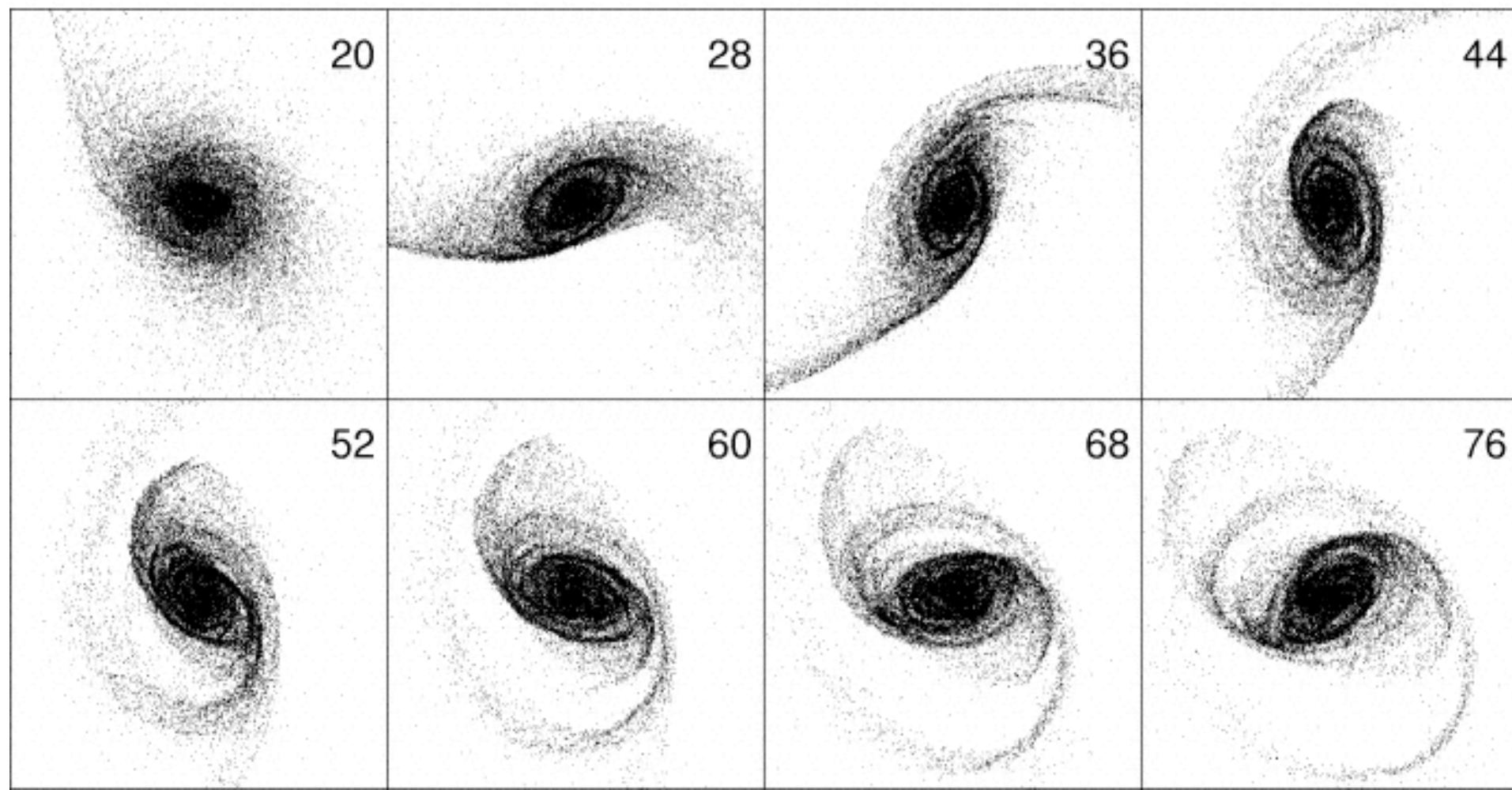
UGC 128: low surface brightness



High surface
density



Low surface
density



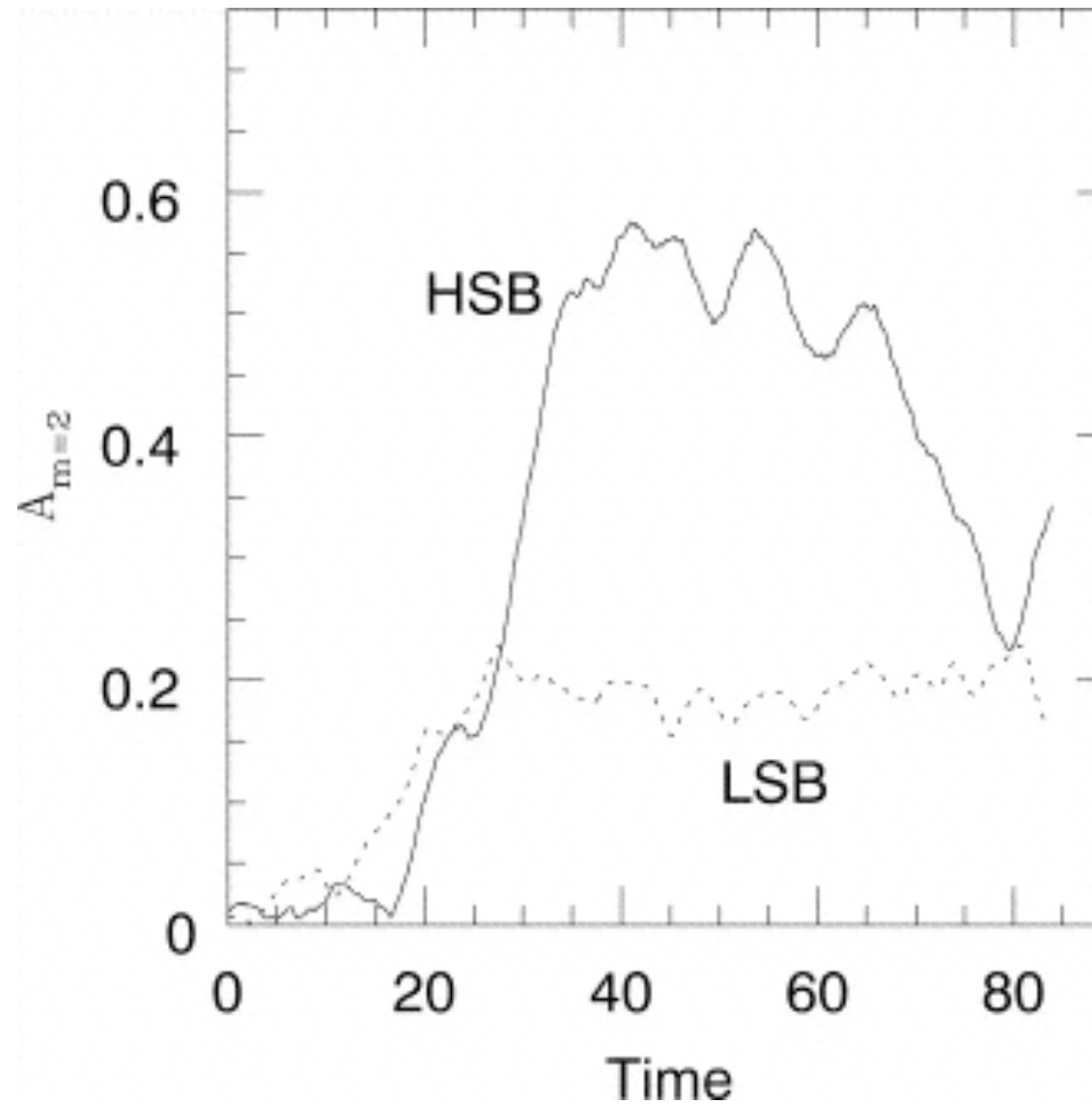
$$A_m = \frac{1}{N} \sum_{j=1}^N e^{i[m\theta_j + p \ln(R_j)]}$$

A bar is an m=2 mode

A two-armed spiral is an m=2 mode with a pitch angle $p > 0$.

A four armed-spiral has m=4, etc.

Amplitude of Bar



<https://www.youtube.com/watch?v=gSwiXwP56js>

<http://www.youtube.com/watch?v=byl9yhITDsM>

Sellwood (2016)

Time evolution of the bar amplitude in models with differing $\frac{M_{halo}}{M_{disk}}$

