

# Cosmology

## and Large Scale Structure



Today

Measurements of  $\Omega_m$

Homework 5 available

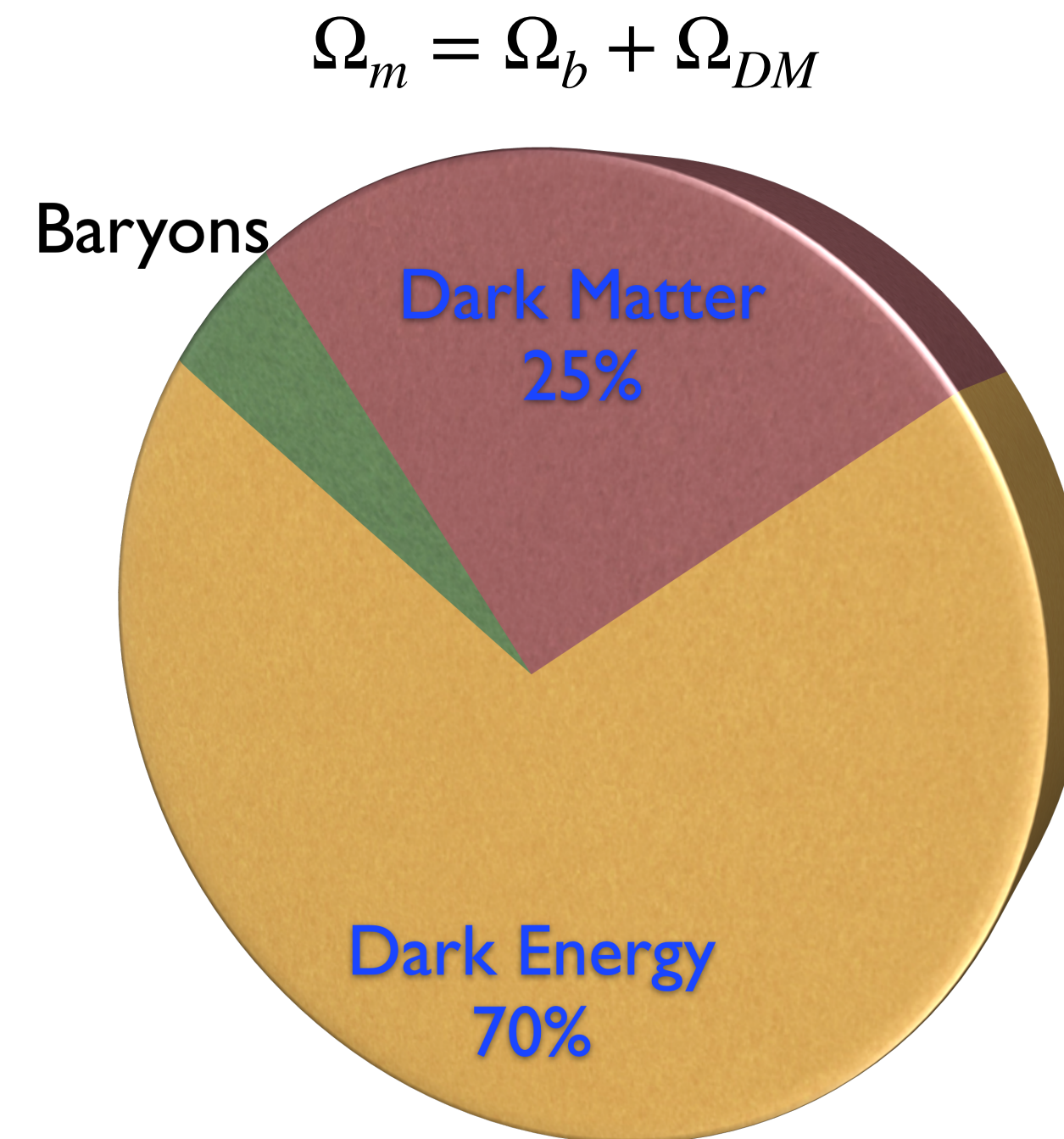
Time to pick a project topic

# Empirical Pillars of the Hot Big Bang

1. Hubble Expansion
2. Big Bang Nucleosynthesis  $\Omega_b$
3. Cosmic Microwave Background

## Auxiliary Hypotheses

- Dark matter  $\Omega_{DM}$
- Dark Energy  $\Omega_\Lambda$



# Cosmological Parameters

The search for two parameters has become six, maybe seven

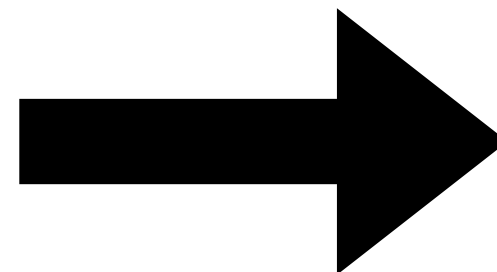
## two parameters

- Hubble expansion rate
  - $H_0$
- Mass density
  - $\Omega_m$

Or simply  $H_0, q_0$

but in the absence of dark energy,

$$q_0 = \frac{1}{2}\Omega_m$$



## six parameters

- Hubble expansion rate
  - $H_0$
- Power spectrum index and normalization
  - $n$  [ $P(k) \propto k^n$ ]
  - $\sigma_8$  (amplitude of mass fluctuations in 8 Mpc spheres)
- Mass-energy density
  - Normal matter (baryon) density  $\Omega_b$
  - Dark matter density  $\Omega_{\text{CDM}}$
  - Dark energy density (cosmological constant)  $\Omega_\Lambda$
  - Neutrino mass density  $\Omega_\nu$  (they're mass as well as energy)

# Current mass-energy content of the universe

“Vanilla LCDM”

mass density	$\Omega_{m_0}$	0.30	give or take a bit
normal matter	$\Omega_b$	0.05	baryons - from BBN
mass that is <i>not</i> normal matter	$\Omega_{\text{CDM}}$	0.25	cold dark matter
cosmic background radiation	$\Omega_r$	$5 \times 10^{-5}$	photons plus $4 \times 10^{-5}$ in neutrinos
neutrinos	$0.001 < \Omega_\nu < 0.002$		for 3 neutrino flavors with $0.06 < \sum_{i=1}^3 m_{\nu_i} < 0.12 \text{ eV}$ upper limit from cosmic structure formation lower limit from neutrino oscillations
dark energy	$\Omega_{\Lambda_0}$	0.70	energy density of vacuum

$$\Omega_x = \frac{\rho_x}{\rho_{\text{crit}}}$$

$$\rho_{\text{crit}} = \frac{3H_0^2}{8\pi G}$$

e.g.  $\Omega_\nu = \frac{\sum m_\nu}{93 \text{ eV}}$

since  $n_\nu = \frac{9}{11} n_\gamma$

## Measurements of the gravitating mass density

- Cluster M/L
  - measure M/L of a cluster, combine with measured luminosity density of universe.
- Weak lensing
  - measure shear over large scales
- Peculiar Velocity Field
  - measure deviations from Hubble flow
- Power spectrum of galaxies
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# Measurements of the gravitating mass density

- Cluster M/L

- measure M/L of a cluster, combine with measured luminosity density of universe.
- Mass from virial theorem

$$M \approx \frac{2.5}{G} \sigma^2 R_e$$

- luminosity  $L$  from observations of *cluster* galaxies
- $j$  from integrating the luminosity function of *field* galaxies:

$$j = \Phi^* L^* \Gamma(\alpha) \quad \rho_m = \left( \frac{M}{L} \right) j$$

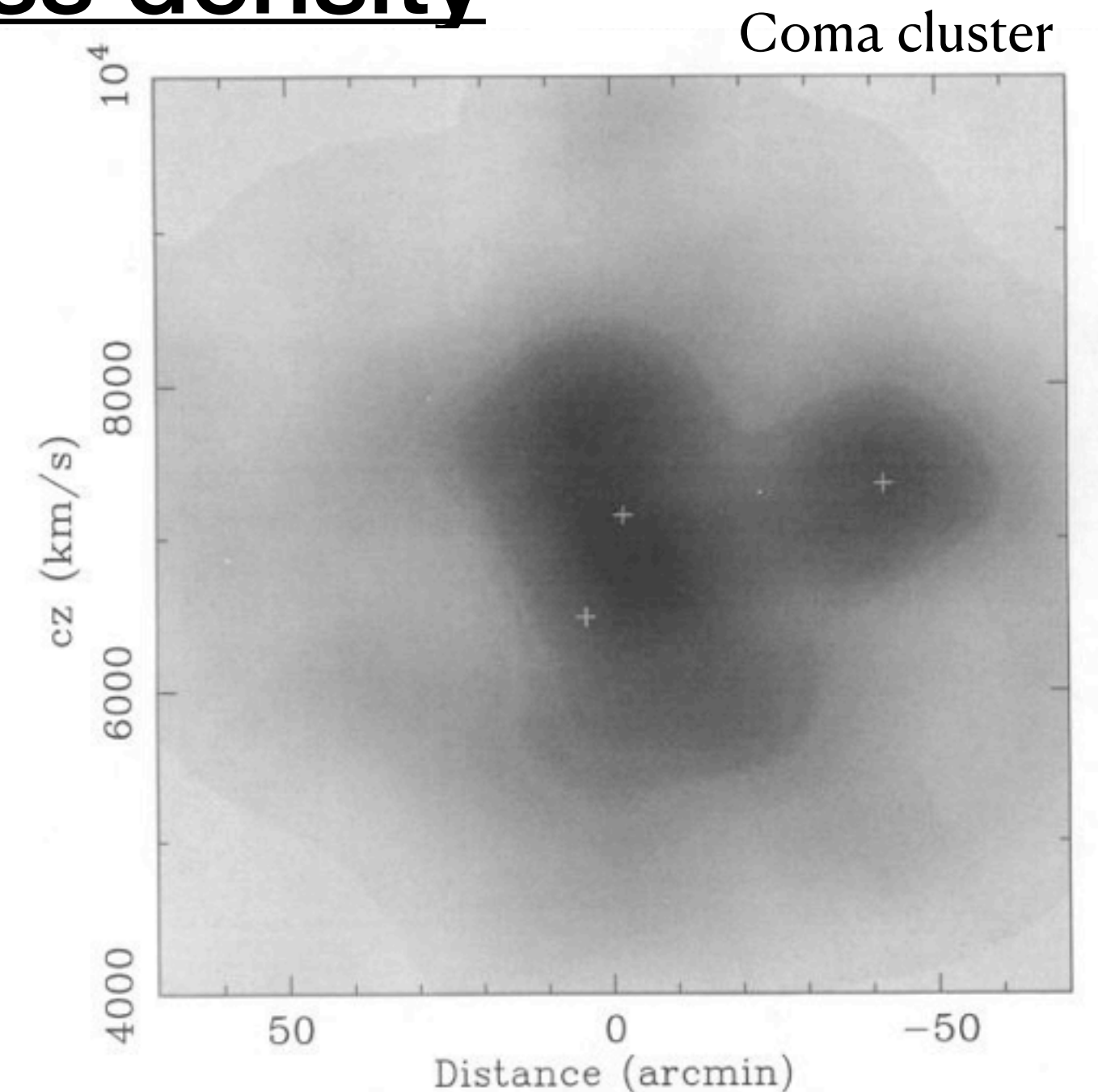


FIG. 10.—Galaxy density distribution projected onto the plane of radial velocity versus projected distance from the cluster center along the NE–SW diagonal (NE positive). The density is smoothed with a Gaussian of dispersion  $8'$  in the spatial dimension and  $300 \text{ km s}^{-1}$  in the velocity dimension. The positions of the three dominant galaxies are marked by crosses (left to right: NGC 4889, NGC 4874, NGC 4839). The gray scale is linear with density and runs from zero to the maximum.

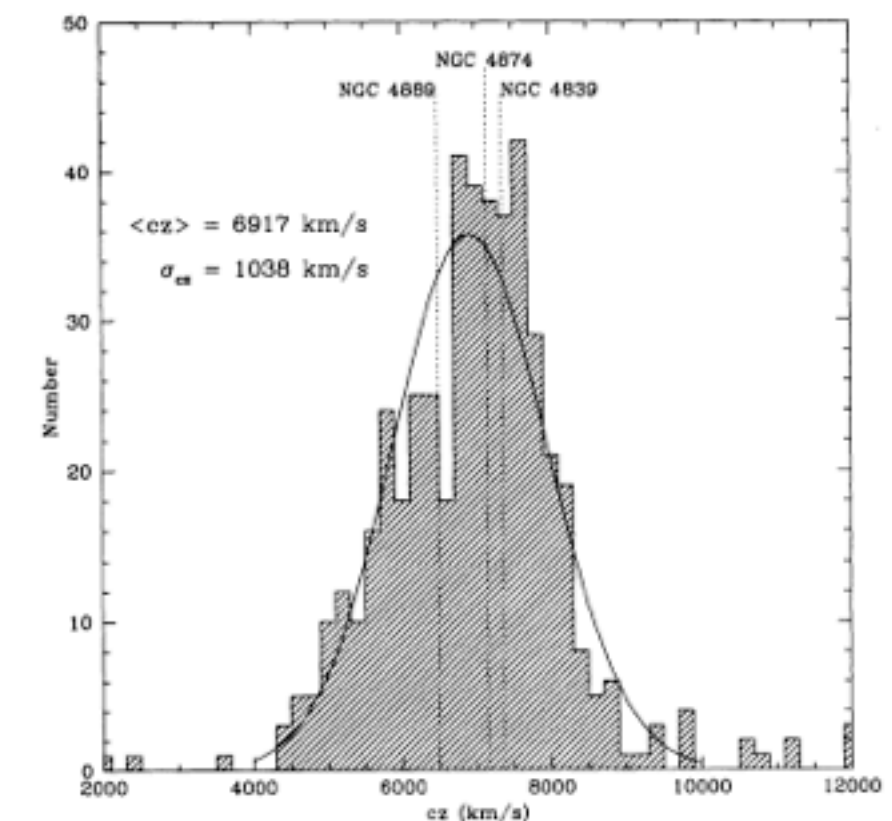


FIG. 5.—Distribution of radial velocities for galaxies in the Coma cluster. The curve is a Gaussian with mean  $6917 \text{ km s}^{-1}$  and standard deviation  $1038 \text{ km s}^{-1}$ . The velocities of the three dominant cluster galaxies are indicated.

# Measurements of the gravitating mass density

- Cluster M/L

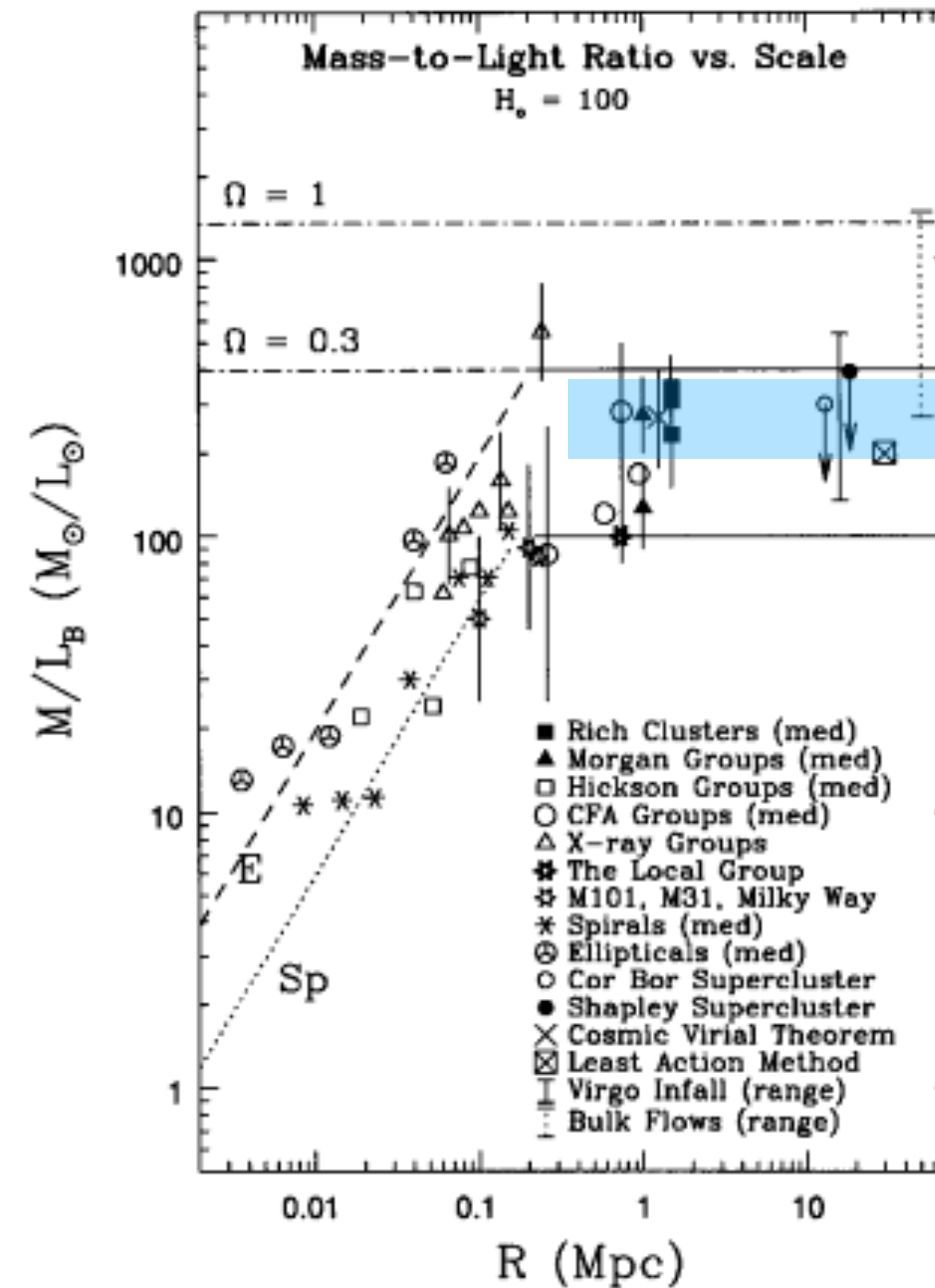
- measure M/L of a cluster, combine with measured luminosity density of universe.
- j from integrating the luminosity function of galaxies:

$$j = \Phi * L * \Gamma(\alpha) \quad \rho_m = \left( \frac{M}{L} \right) j$$

- Also, cluster baryon fractions:

$$f_b = \frac{M_b}{M_{tot}} \quad \longrightarrow \quad \Omega_m = \frac{\Omega_b}{f_b}$$

- both assume clusters are representative of the whole.



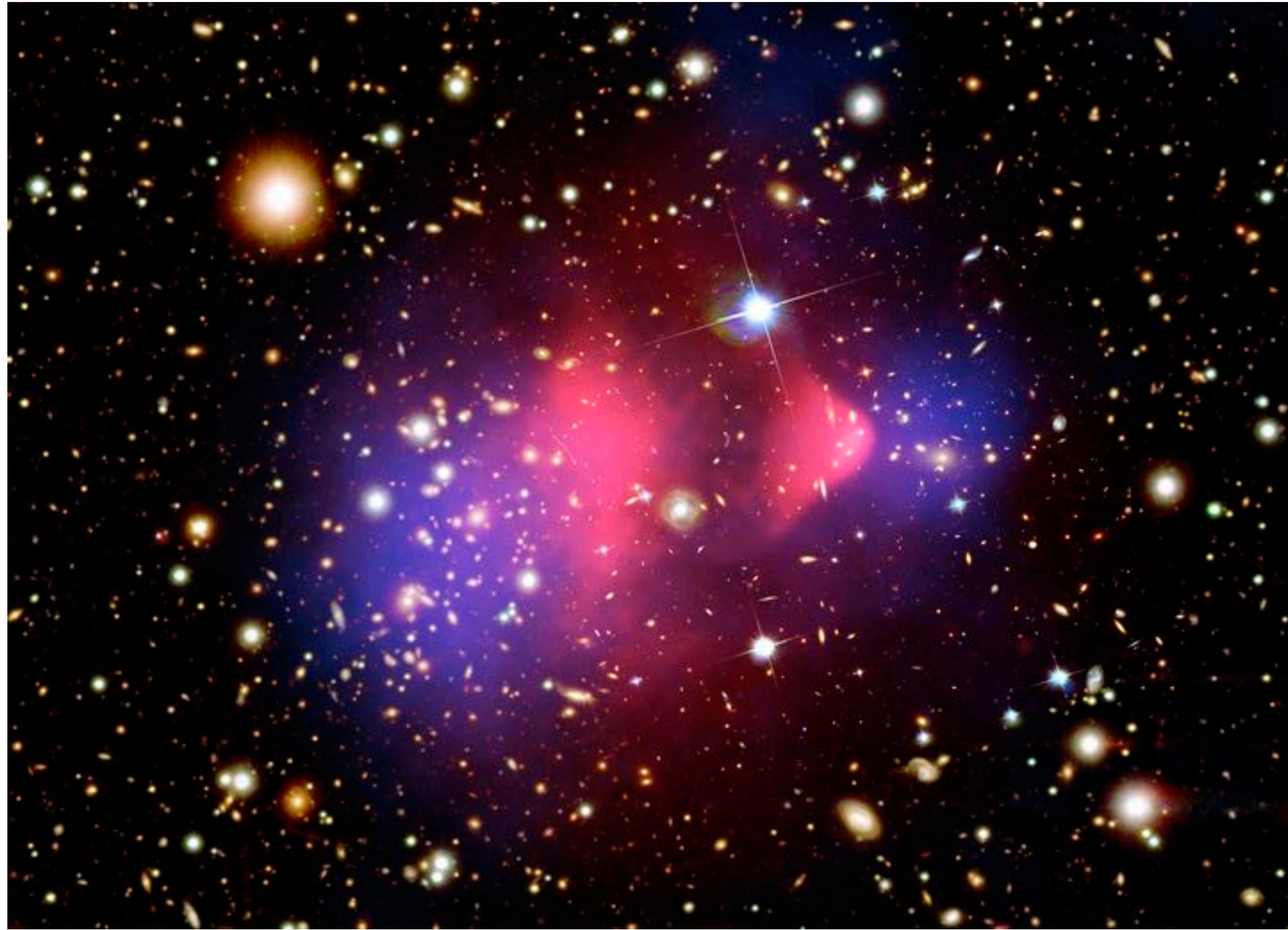
$$\Omega_m \approx \frac{1}{4}$$

$$\Omega_j \approx 10^{-3}$$

$$\frac{M}{L} \approx 250$$

FIG. 2.—Composite mass-to-light ratio of different systems—galaxies, groups, clusters, and superclusters—as a function of scale. The best-fit  $M/L_B \propto R$  lines for spirals and ellipticals (from Fig. 1) are shown. We present median values at different scales for the large samples of galaxies, groups and clusters, as well as specific values for some individual galaxies, X-ray groups, and superclusters. Typical  $1\sigma$  uncertainties and  $1\sigma$  scatter around median values are shown. Also presented, for comparison, are the  $M/L_B$  (or equivalently  $\Omega$ ) determinations from the cosmic virial theorem, the least action method, and the *range* of various reported results from the Virgocentric infall and large-scale bulk flows (assuming mass traces light). The  $M/L_B$  expected for  $\Omega = 1$  and  $\Omega = 0.3$  are indicated.

Bullet cluster

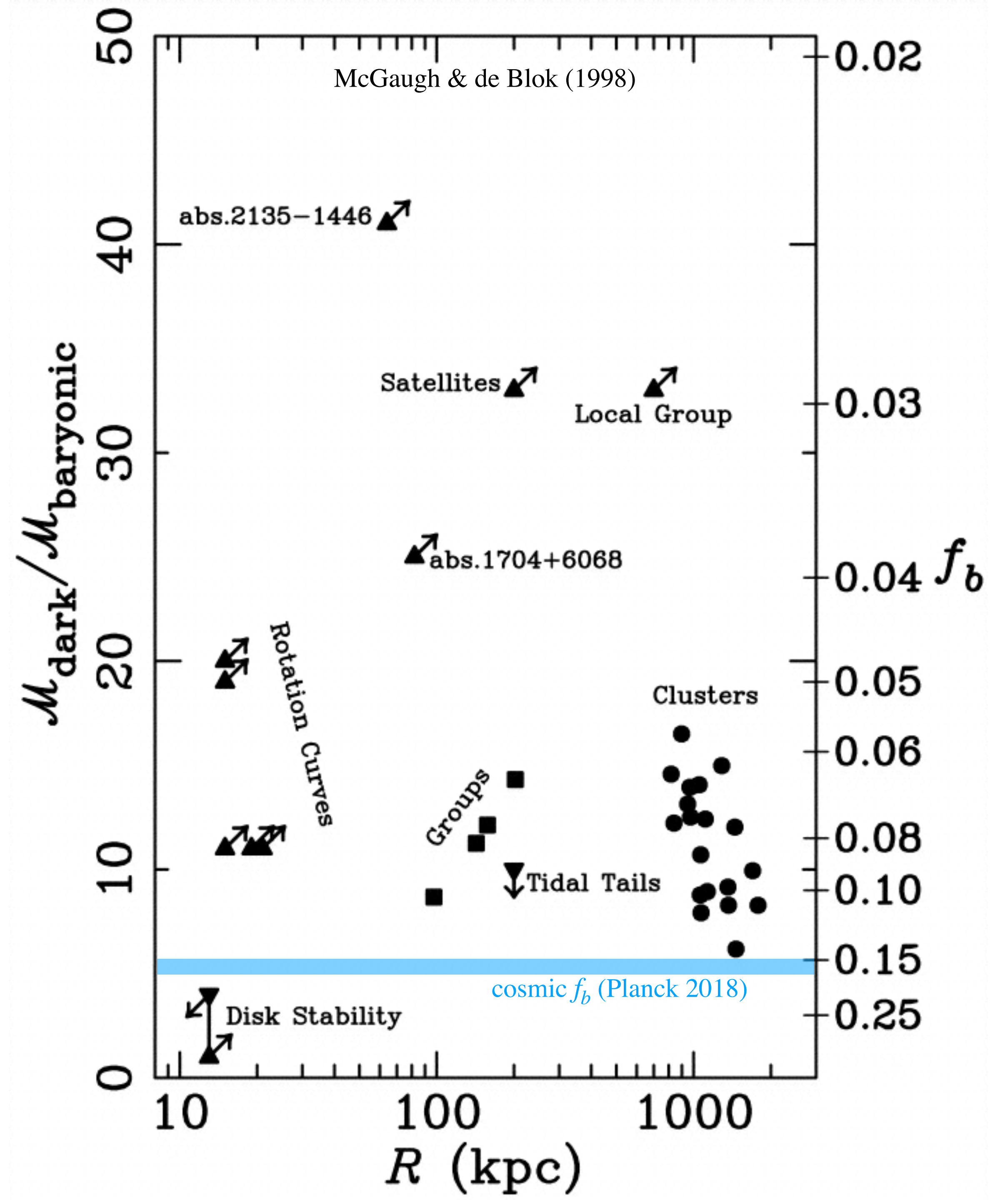


– cluster baryon fractions

$$f_b = \frac{M_b}{M_{tot}} \quad \circ \longrightarrow \quad \Omega_m = \frac{\Omega_b}{f_b}$$

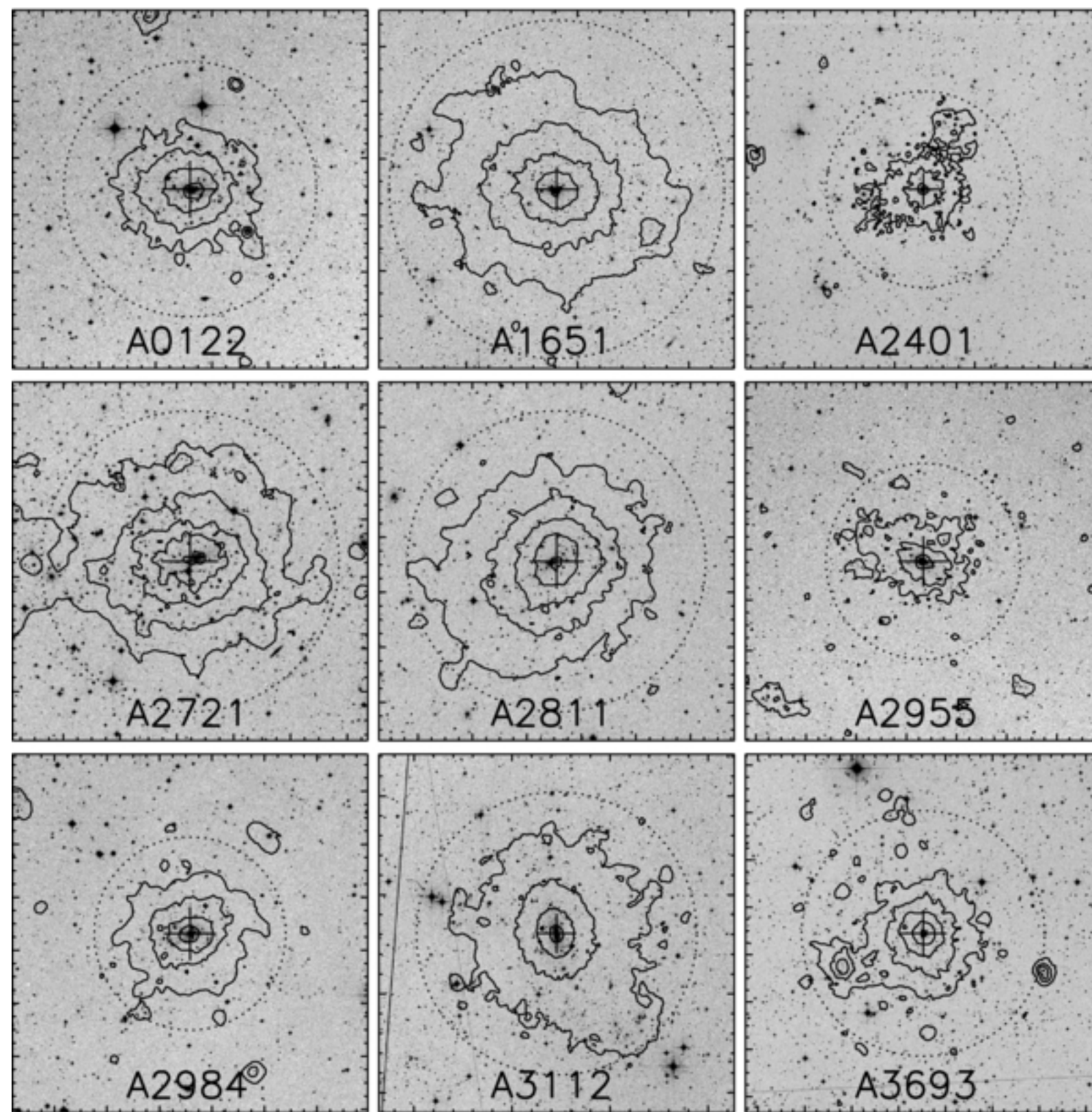
Measure cluster baryonic mass  $M_b$  from luminosity of X-ray gas (pink)  
plus stars in galaxies (yellow)

Measure cluster dynamical mass  $M_{tot}$  from X-ray temperature (pink)  
or weak lensing (blue)  
or velocity dispersion





– cluster baryon fractions



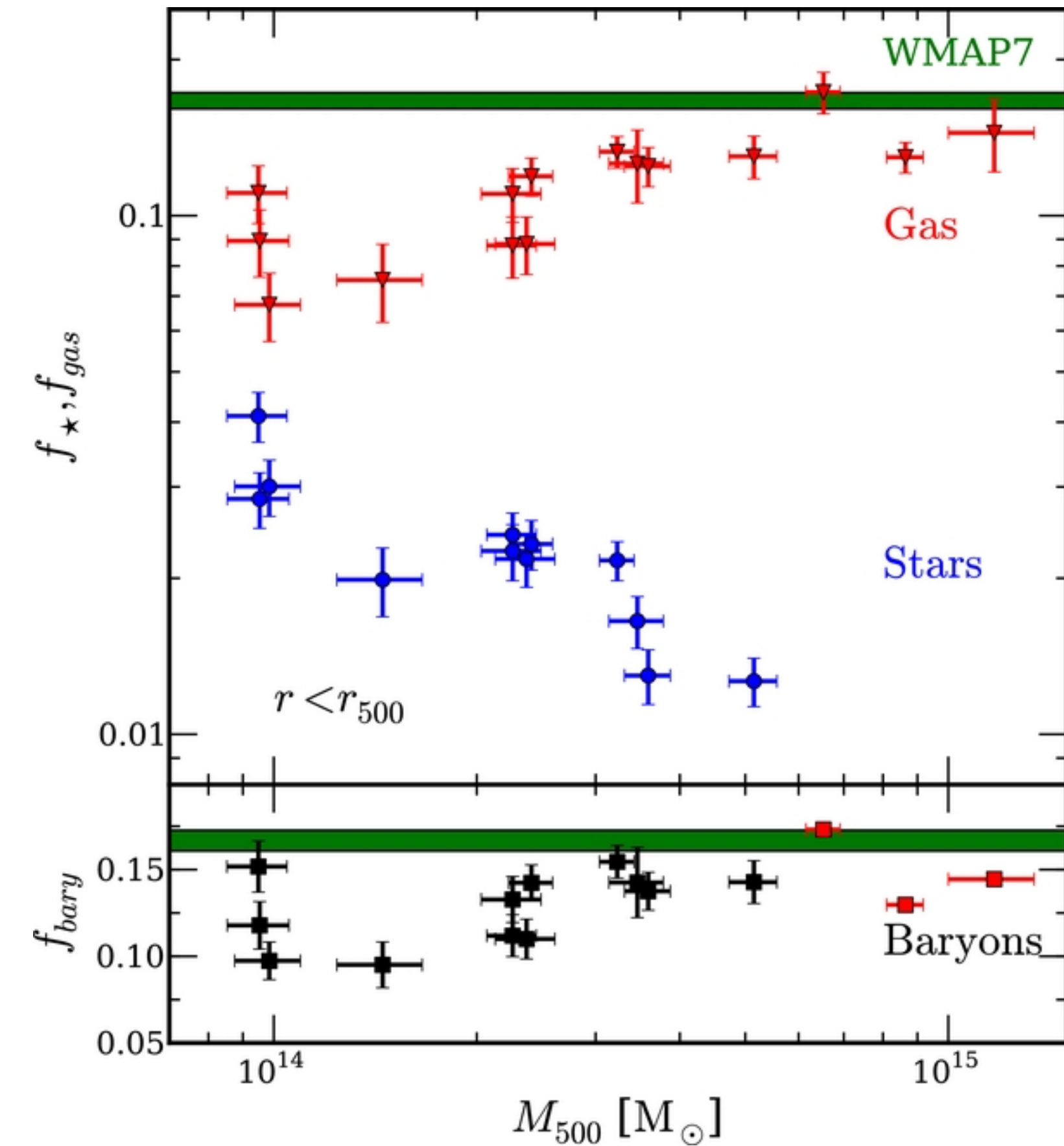
– cluster baryon fractions

$$f_b = \frac{M_b}{M_{tot}} \quad \circ \longrightarrow \quad \Omega_m = \frac{\Omega_b}{f_b}$$

Measure cluster baryonic mass  $M_b$  from luminosity of X-ray gas (contours) plus stars in galaxies (black)

Measure cluster dynamical mass  $M_{tot}$  from X-ray temperature (contours) or weak lensing or velocity dispersion

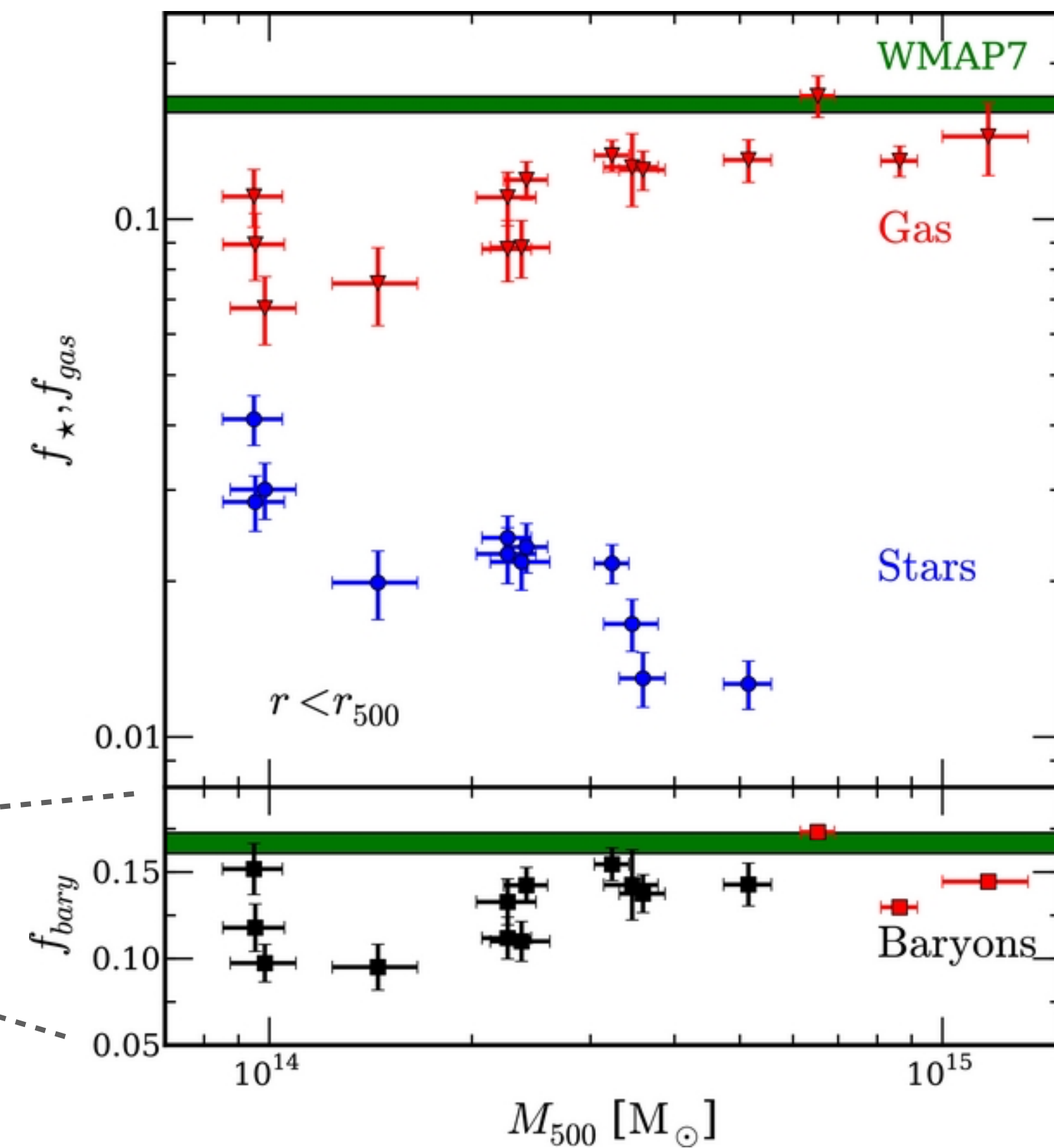
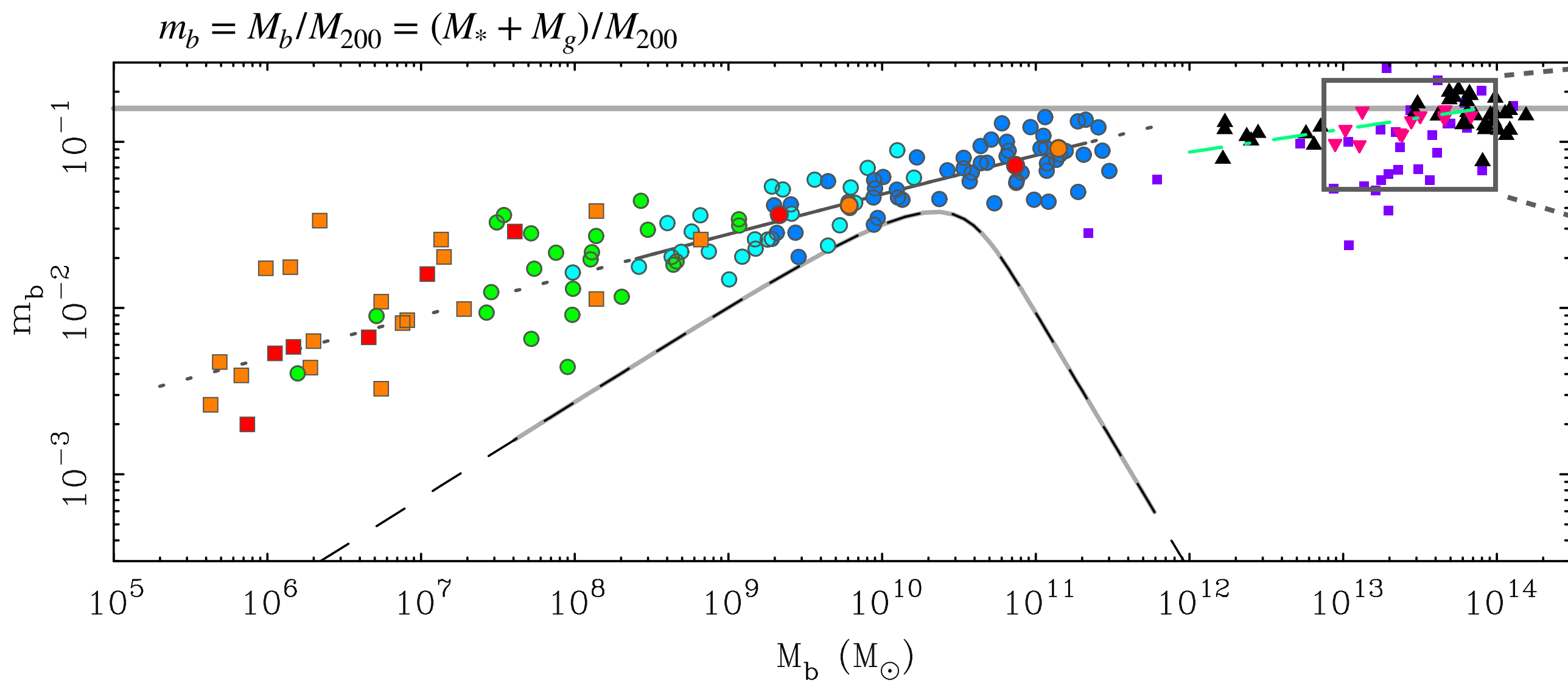
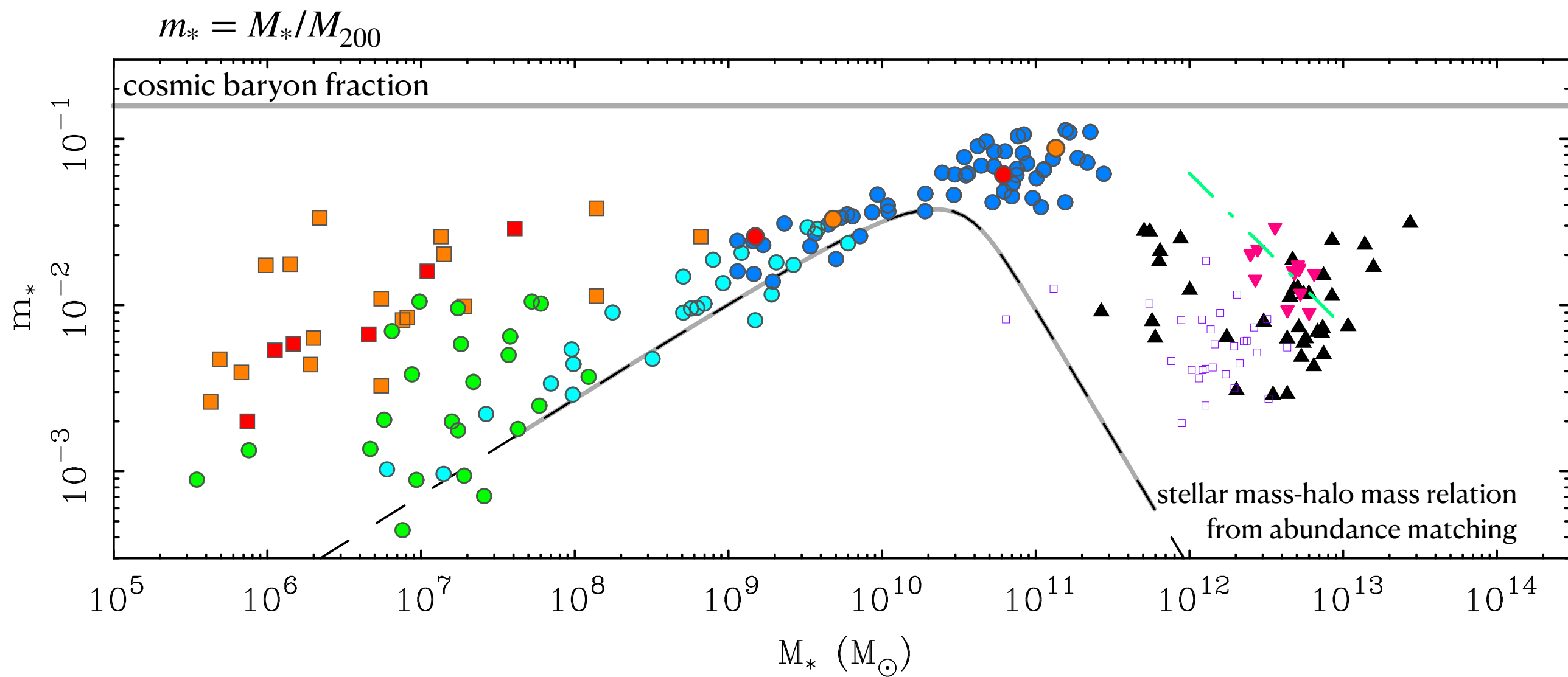
Gonzalez et al. (2013)



Most of the baryonic mass in rich clusters is in the hot, X-ray emitting gas of the ICM (intracluster medium). Only the most massive clusters approach the cosmic fraction found in fits to the acoustic power spectrum of the CMB. Lower mass clusters suffer a missing baryon problem.

– beyond cluster baryon fractions

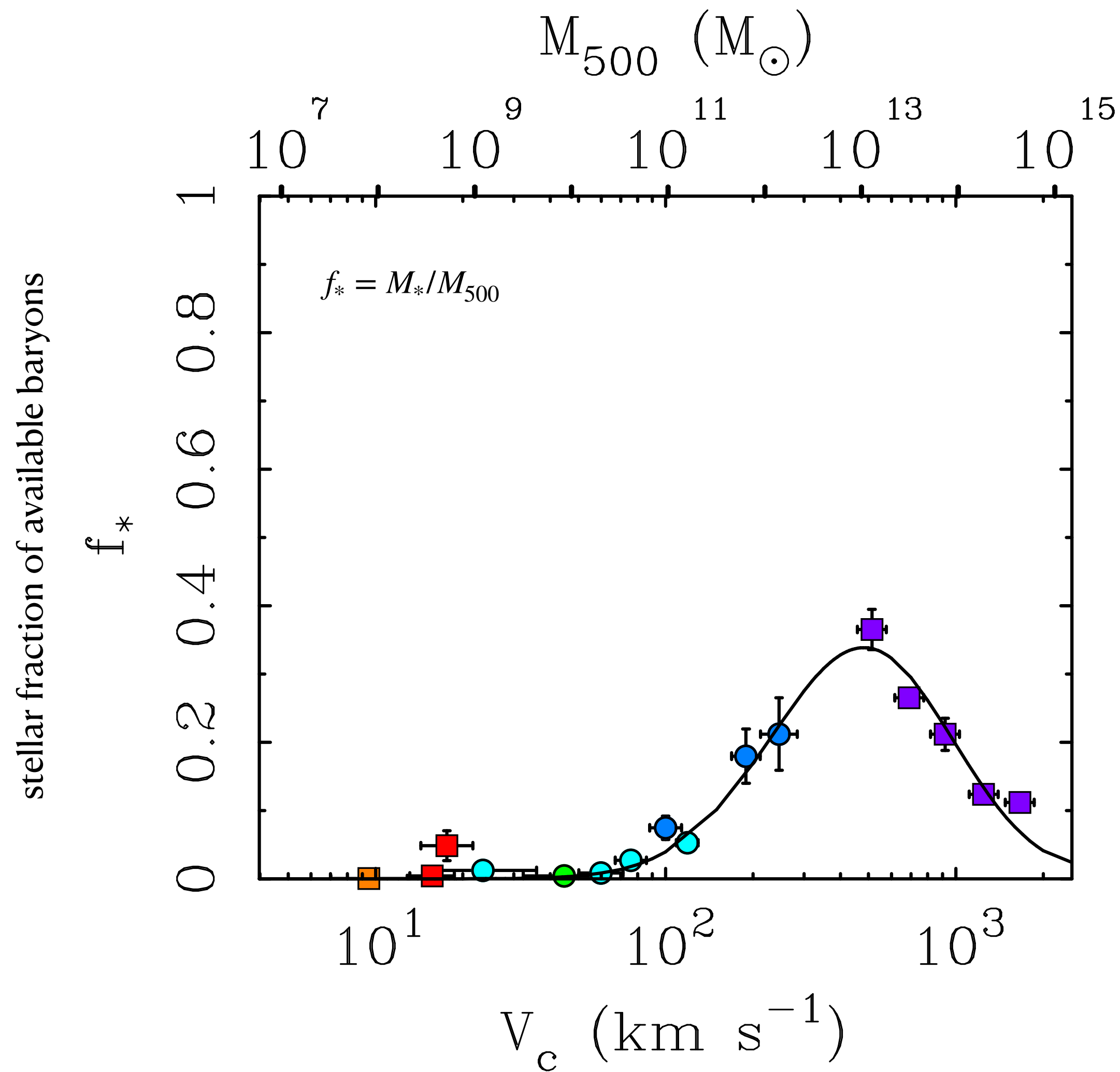
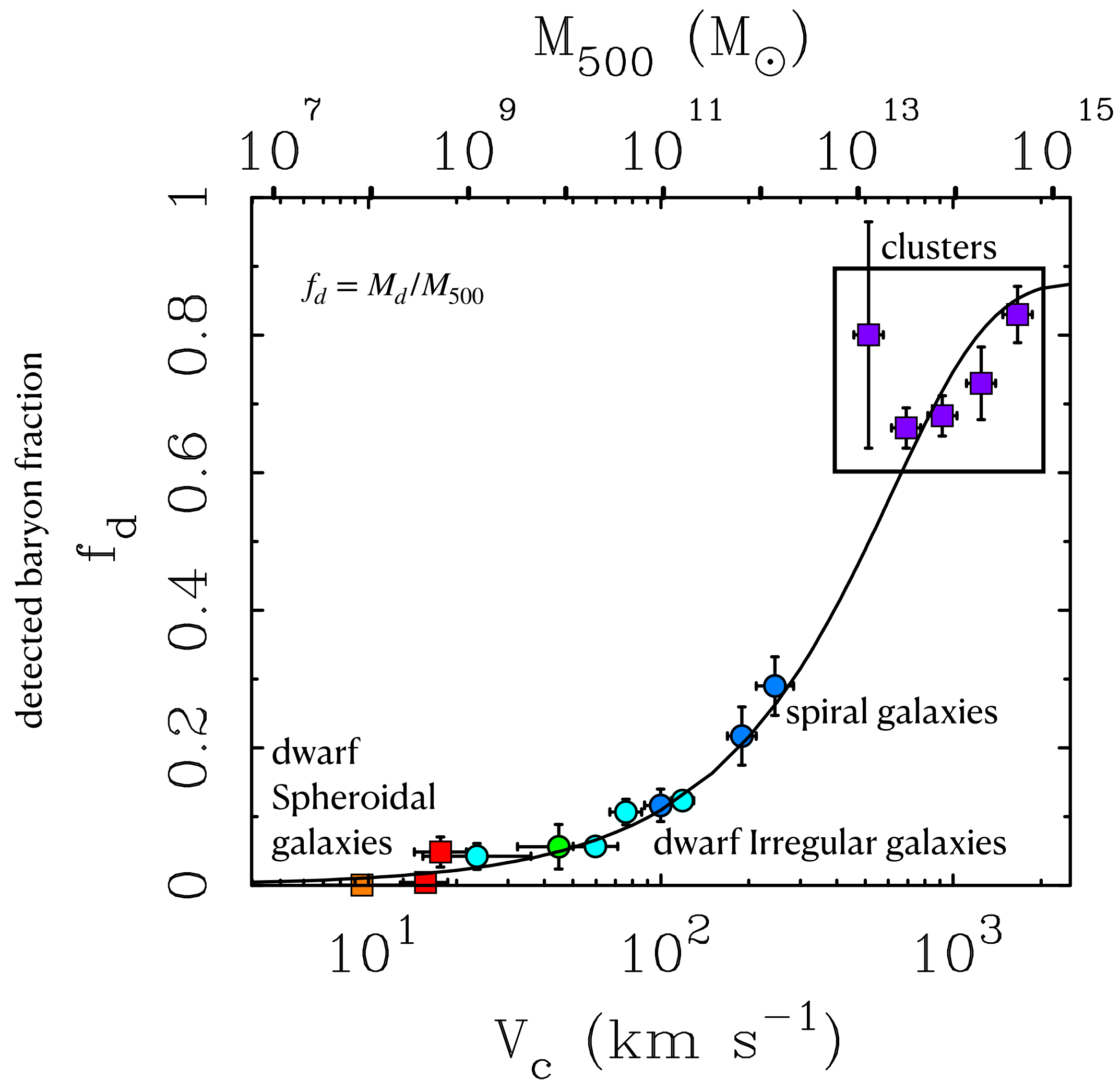
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– beyond cluster baryon fractions

McGaugh et al. (2010)



$$f_d = M_b / (f_b M_{200}) = (M_* + M_g) / (f_b M_{200})$$

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# Measurements of the gravitating mass density

- Weak lensing
  - measure shear over large scales

Dark Energy Survey  
arxiv:2002.11124

$$\Omega_m \approx 0.18 \pm 0.04$$

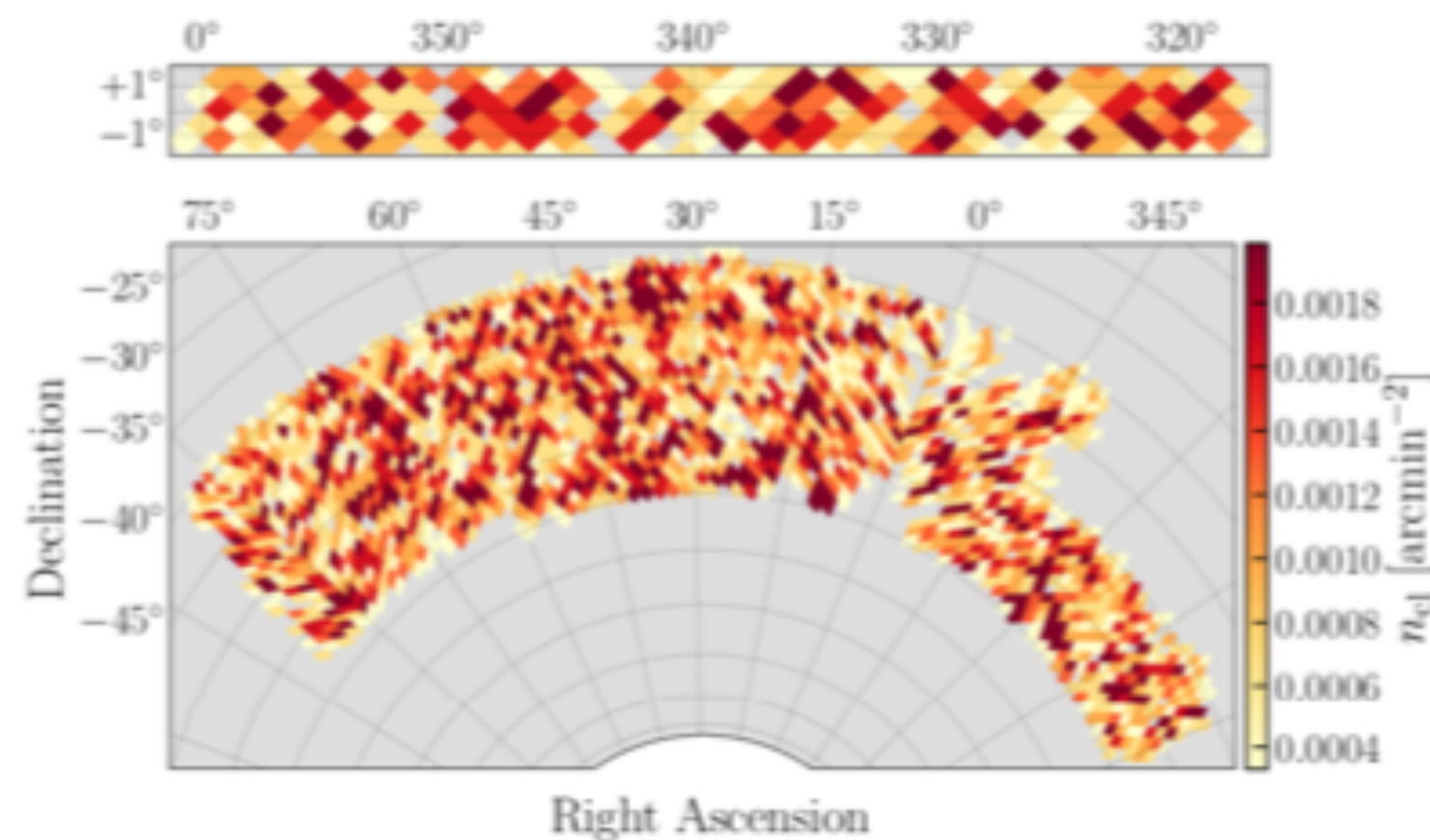
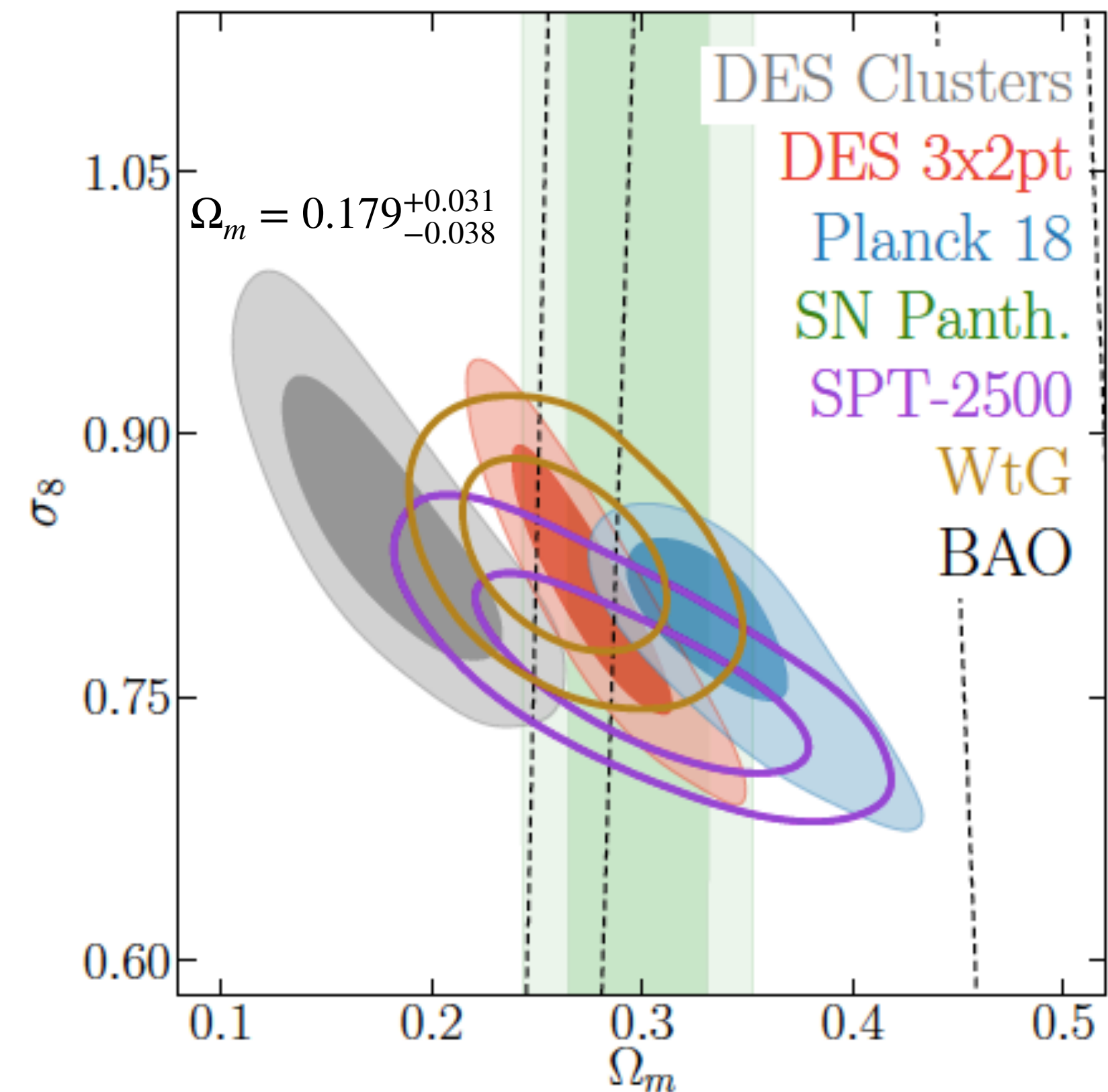


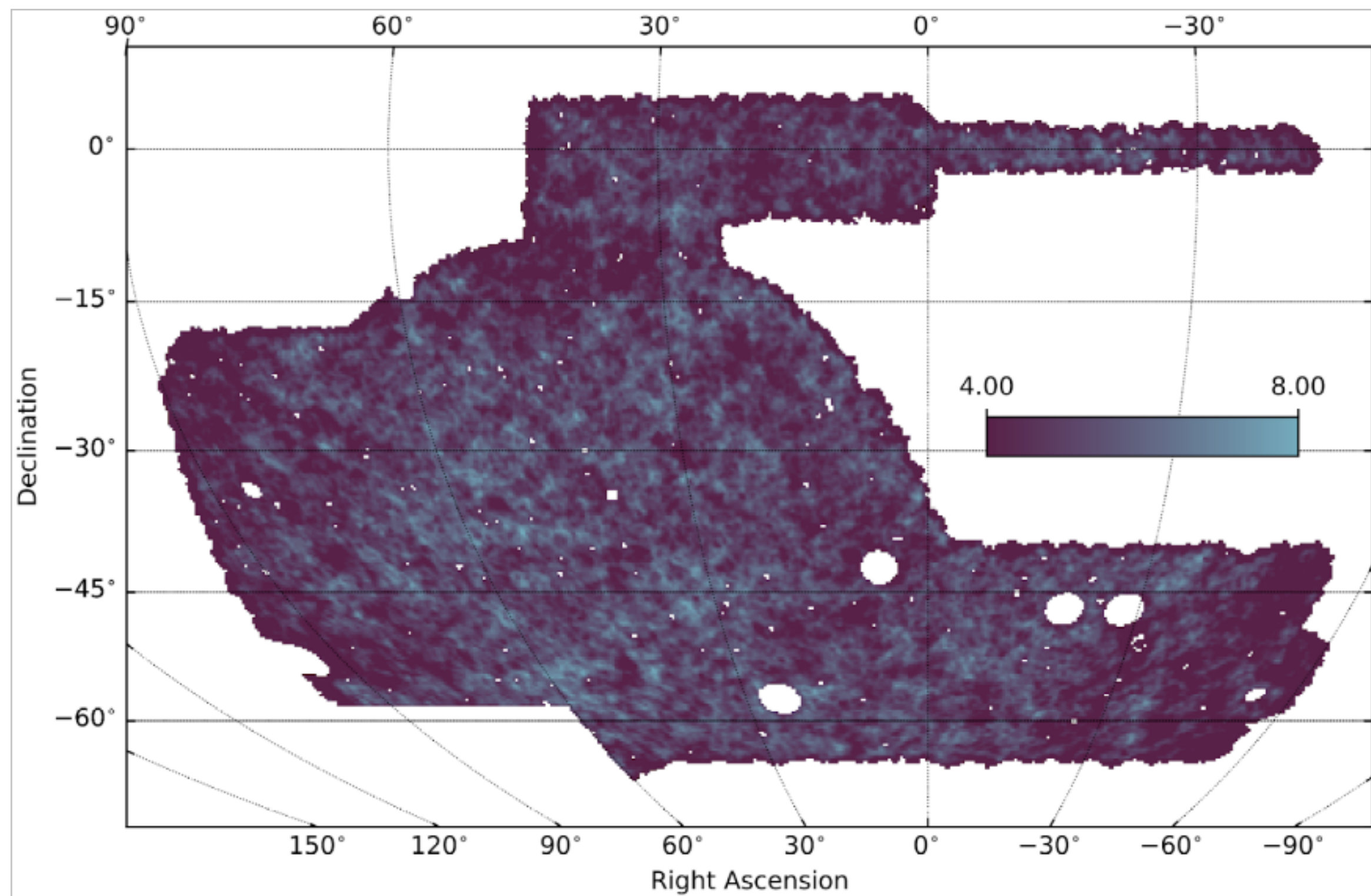
FIG. 1. The DES Y1 redMaPPer cluster density over the two non-contiguous regions of the Y1 footprint: the Stripe 82 region (116 deg<sup>2</sup>; *upper* panel) and the SPT region (1321 deg<sup>2</sup>; *lower* panel).



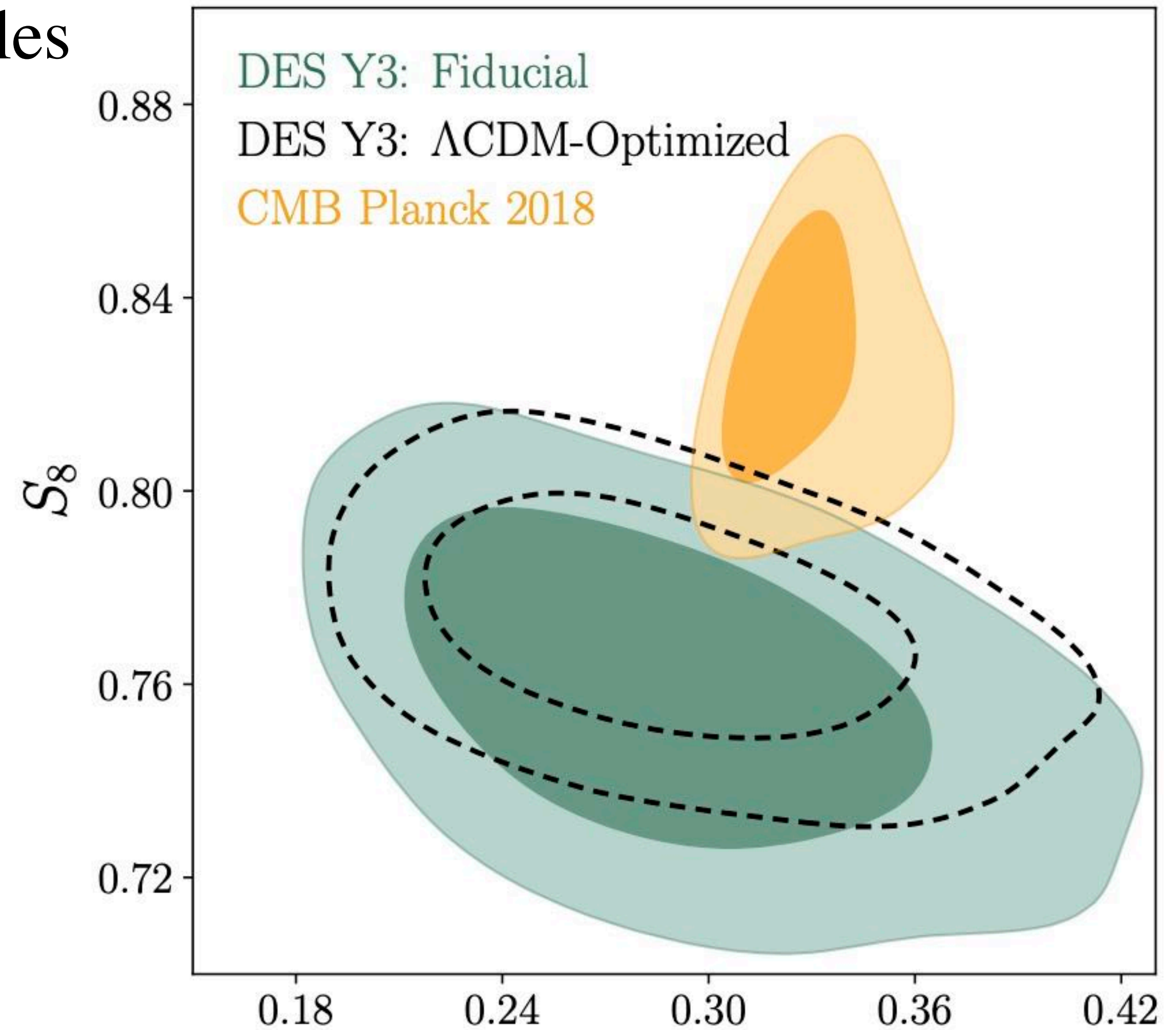
# Measurements of the gravitating mass density

- Weak lensing
  - measure shear over large scales

Dark Energy Survey  
Amon et al. (2022, PRD, 105, 023514)



$$S_8 = \sigma_8 \left( \frac{\Omega_m}{0.3} \right)^{1/2} = 0.759^{+0.025}_{-0.023}$$



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# Measurements of the gravitating mass density

- Peculiar Velocity Field
  - measure deviations from Hubble flow

in linear regime  $\frac{\delta\rho}{\rho} \ll 1$

$$\frac{\delta v}{v} \approx \frac{d \ln H}{d \ln \rho} \frac{\delta\rho}{\rho} \approx - \frac{1}{3} \frac{\Omega_m^{0.6}}{b} \frac{\delta\rho_g}{\rho_g}$$

peculiar velocity
distortion in Hubble flow induced by
mass over-density
bias

BIAS  $b$   
 relates  
 galaxy over-densities  
 to mass over-densities

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TONRY AND DAVIS

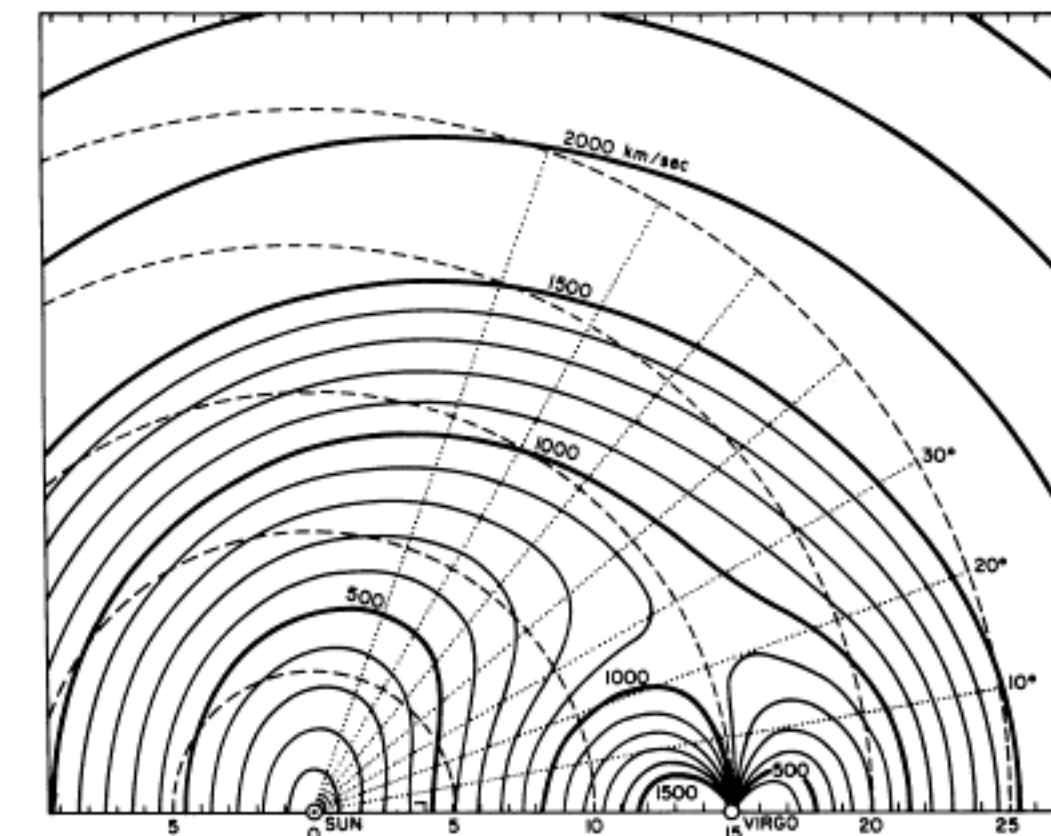


FIG. 1.—On a two-dimensional grid with the Earth and the Virgo cluster on the  $x$  axis, redshift contours are plotted for a Hubble flow perturbed by a Virgo-centric flow. An infall velocity of  $400 \text{ km s}^{-1}$  at our position is assumed. A pure Hubble flow would be concentric circles.

$$\Omega_m = 0.25 \pm 0.05$$



Davis et al. (1980) found

$$\Omega_m = 0.4 \pm 0.1$$

with a modern distance scale this becomes

$$\Omega_m = 0.25 \pm 0.05$$

*basically unchanged for over 40 years*

Lines are lines of constant  $\Omega_m$

ESTIMATES OF  $v_p$

Velocity	Source
$380 \pm 75$	Smoot and Lubin 1979
$480 \pm 75$	Aaronson <i>et al.</i> 1980
$350 \pm 50$	de Vaucouleurs and Bollinger 1979
$290 \pm 30^*$	Yahil 1980
$190 \pm 130$	Schechter 1968

\* Calculated with respect to the centroid at the local group as defined by Yahil *et al.* 1977.

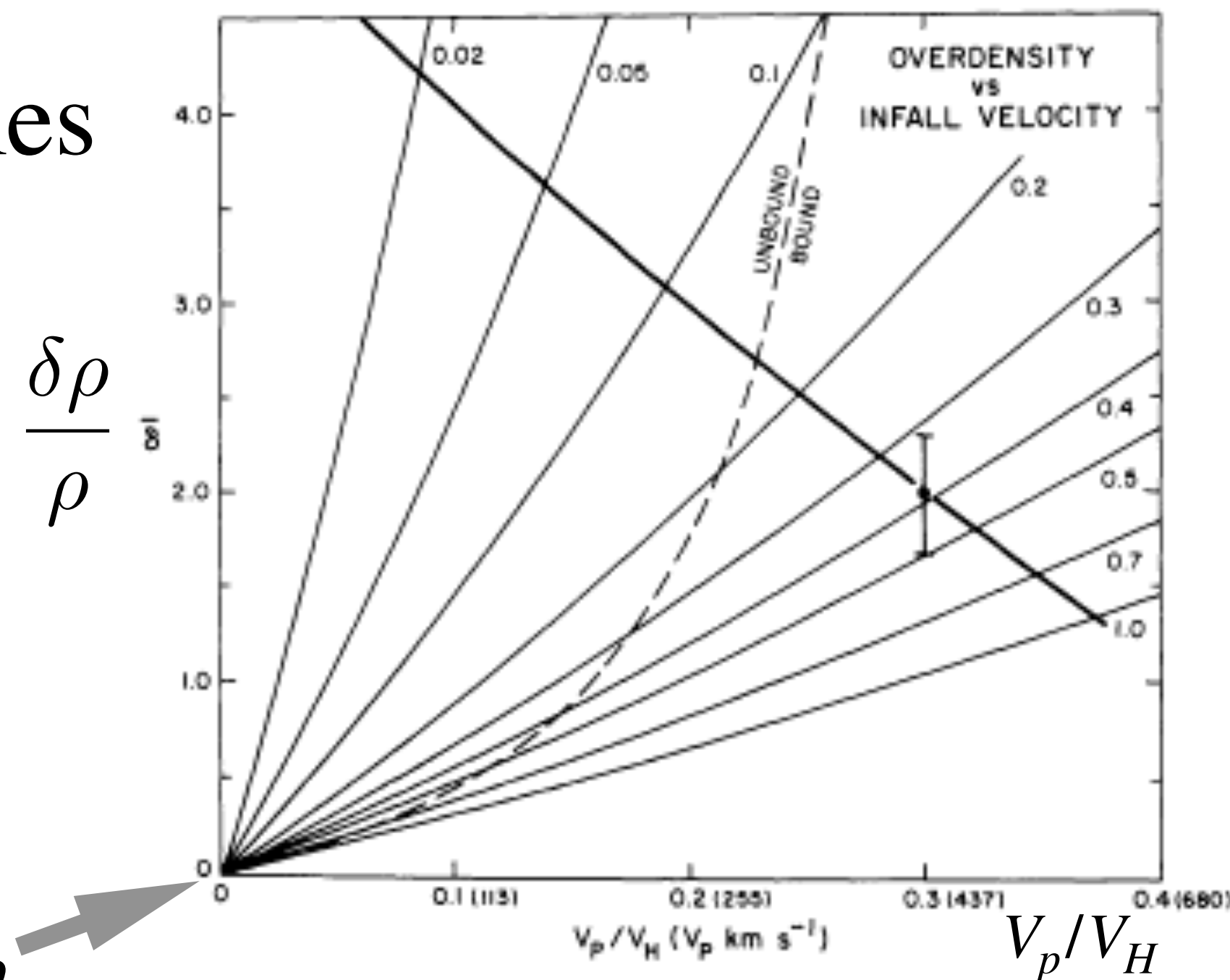


FIG. 1.—The mean overdensity of Virgo vs.  $v_p/v_H$  for various values of  $\Omega$ . The  $x$ -axis is also labeled with  $v_p$ , using a recessional velocity to Virgo of  $1020 \text{ km s}^{-1}$ . The measured overdensity is prescribed by the heavy line, and is marked at the favored position as given by the anisotropy of the Hubble flow and microwave background radiation. The error bar is an estimate of the 90% confidence limit of our determination of  $\bar{\delta}$ . Models to the right of the dotted line are bound to Virgo.

mated, roughly by density of galaxies as  $r^{-2}$ ; if the mass reduced peculiar velocity this model will apply which have not yet Virgo core and with  $\text{km s}^{-1}$  are assumed scale peculiar motion effect on the comp  $100 \text{ km s}^{-1} \text{ Mpc}^{-1}$ ,  $300 \text{ km s}^{-1}$  galactic Aaronson, and Hu sional velocity of Table 2 lists the co dom sample when b assumed here  $v_p/v_H$  The mean overd not at all sensitive

VIRGO	
Distance <sup>a</sup> (Mpc)	
0-5	.....
5-10	.....
10-15	.....
15-20	.....
20-25	.....
25-30	.....
30-35	.....
$\bar{\delta}$	.....

\* Assumes distance and  $H$   
<sup>b</sup> 600 objects  
<sup>c</sup> Within 1