

# ASTR 201 - Homework #2 Solutions

Ch. 3: 9).  $A = 1$   $\frac{P^2}{A^3} = 1.0$   
Kepler's 3<sup>rd</sup> Law:  $P^2 = A^3 \rightarrow \frac{P^2}{A^3} = 1$

Ch 3: 33).  $A = 50 \text{ AU}$ ;  $P = ?$   
 $P^2 = A^3 \rightarrow P = A^{3/2}$

$$P = (50)^{3/2} \approx \boxed{354 \text{ years}}$$

Ch 4: 6)  $M_V = 0.8 M_E$ ;  $R_V = 0.95 R_E$   
 $F_V = ?$ ;  $m = \text{your mass}$

$$F_V = \cancel{m} g_V = \frac{G M_V \cancel{m}}{R_V^2} = \frac{G(0.8 M_E)}{(0.95 R_E)^2}$$
$$g_V \approx \frac{G(0.8 M_E)}{0.9 R_E^2} \approx 0.9 \frac{G M_E}{R_E^2}$$
$$= 0.9 g_E$$

Ex.:  $m = 50 \text{ kg}$ ,  $g_E = 10 \text{ m/s}^2$   
Weight =  $m g_E = 500 \text{ N}$

$g_V = 9 \text{ m/s}^2$   
Weight (Venus) =  $(50)(9) = 450 \text{ N}$

→ D - 10 percent less than on Earth

Ch 4: 31)  $M_M = 0.1 M_E$ ;  $R_M = 0.5 R_E$ ;  $g_M = ?$

$$F = \frac{GMm}{R^2} = mg$$

$$g_M = \frac{GM_M}{R_M^2} = \frac{G(0.1 M_E)}{(0.5 R_E)^2} = \frac{G(0.1 M_E)}{0.25 R_E^2}$$

$$g_M = 0.4 G M_E / R_E^2 = \boxed{0.4 g_E}$$

$$m = 50 \text{ kg}; g_E = 10 \text{ m/s}^2; g_M = 4 \text{ m/s}^2$$

$$\text{Weight (Earth)} = mg_E = (50)(10) = 500 \text{ N}$$

$$\text{Weight (Mars)} = mg_M = (50)(4) = 200 \text{ N}$$

Hollywood movies

Ch 4: 37 (E.C). Galilean Moons: Io, Europa, Ganymede, & Castillo

$P^2 = A^3 \rightarrow \frac{P^2}{A^3}$  should be the same for each moon

$$\text{Io: } P = 1.77 \text{ d}; A = 421.8 \times 10^3 \text{ km} = 421,800 \text{ km}$$

$$P^2/A^3 = (1.77)^2 / (421,800)^3 \approx 4.2 \times 10^{-17} \frac{\text{d}^2}{\text{km}^3}$$

$$\text{Europa: } P = 3.55 \text{ d}; A = 671,100 \text{ km}$$

$$P^2/A^3 \approx 4.2 \times 10^{-17} \frac{\text{d}^2}{\text{km}^3}$$

$$\text{Ganymede: } P = 7.15 \text{ d}; A = 1,070,600 \text{ km}$$

$$P^2/A^3 \approx 4.2 \times 10^{-17} \frac{\text{d}^2}{\text{km}^3}$$

$$\text{Castillo: } P = 16.69 \text{ d}; A = 1,883,000 \text{ km}$$

$$P^2/A^3 \approx 4.2 \times 10^{-17} \frac{\text{d}^2}{\text{km}^3}$$

$\frac{P^2}{A^3}$  is consistent for each moon; Kepler's 3<sup>rd</sup> law applies