

# DARK MATTER

ASTR 333/433

SPRING 2024

TR 11:30AM-12:45PM

SEARS 552

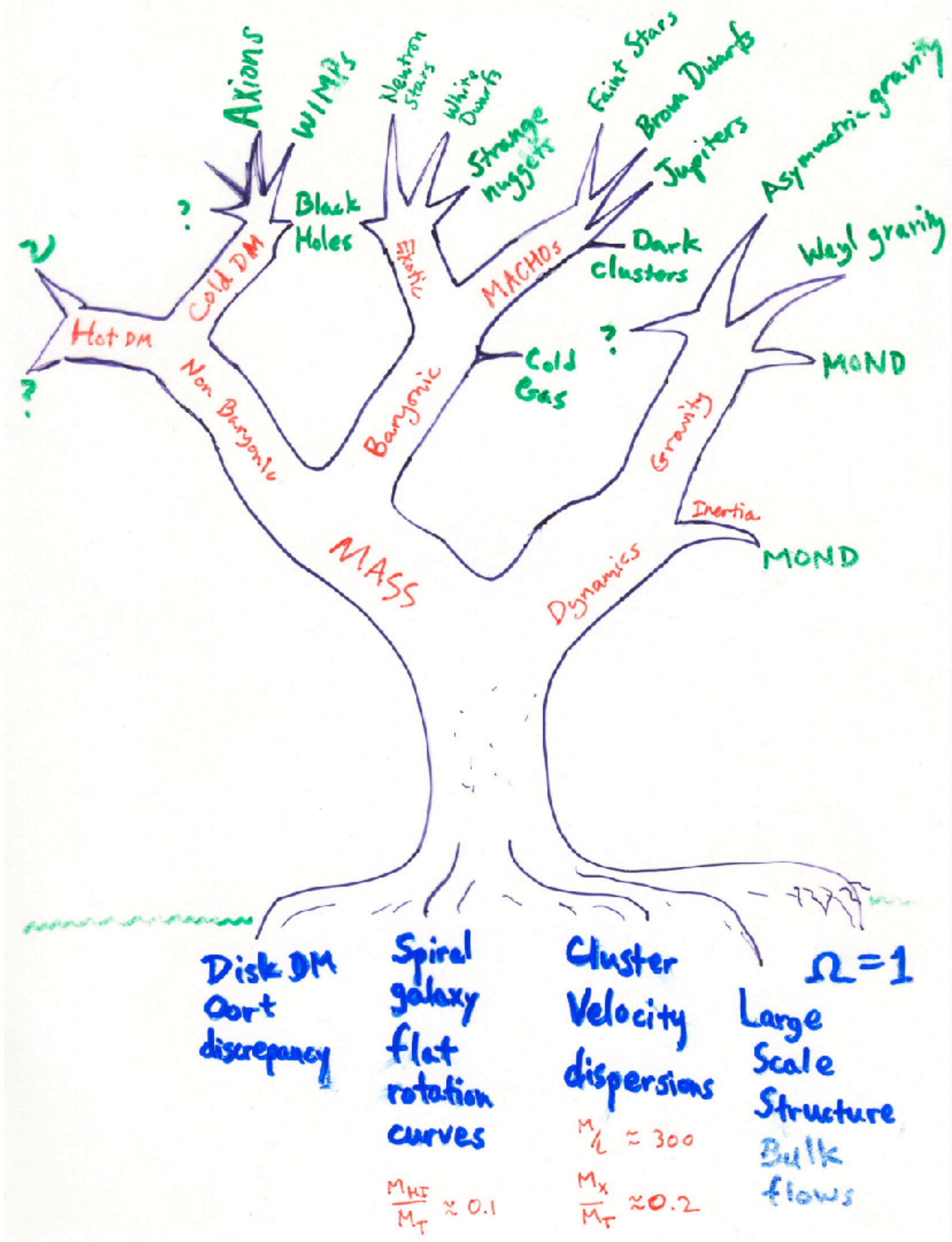
<http://astroweb.case.edu/ssm/ASTR333/>

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CASE WESTERN RESERVE  
UNIVERSITY EST. 1826

# Dark Matter Halos

Many models; none entirely appropriate

- Pseudo-isothermal

$$\longrightarrow V_{\text{iso}}(R) = V_{\infty} \sqrt{1 - \frac{R_C}{R} \arctan\left(\frac{R}{R_C}\right)} \quad V_{\infty} = \sqrt{4\pi G \rho_0 R_C^2}$$

- NFW

- Burkert

- Einasto

- DC14

- coreNFW

- etc. - see Li et al. (2020, ApJS, 247, [31](#) ; arXiv:2001.10538)

$$\longrightarrow V_{\text{NFW}}(R) = V_{200} \sqrt{\frac{\ln(1 + cx) - cx/(1 + cx)}{x[\ln(1 + c) - c/(1 + c)]}} \quad x = \frac{R}{R_{200}} \quad c = \frac{R_{200}}{R_s}$$

sometimes refer to halos by their “virial” temperature  $kT_{\text{vir}} \propto \sigma^2$

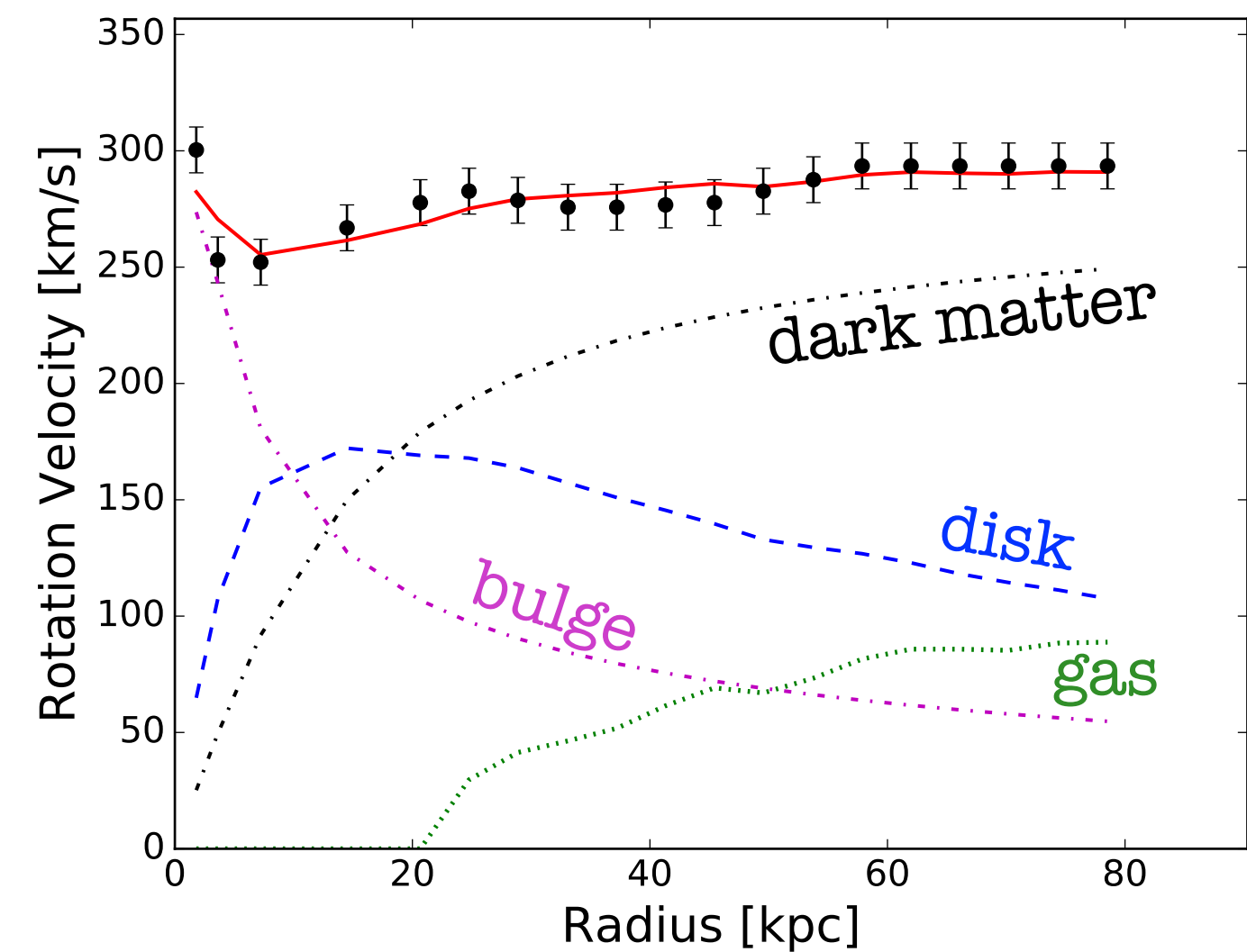
$$\sigma = \frac{1}{\sqrt{3}} V_{200}$$



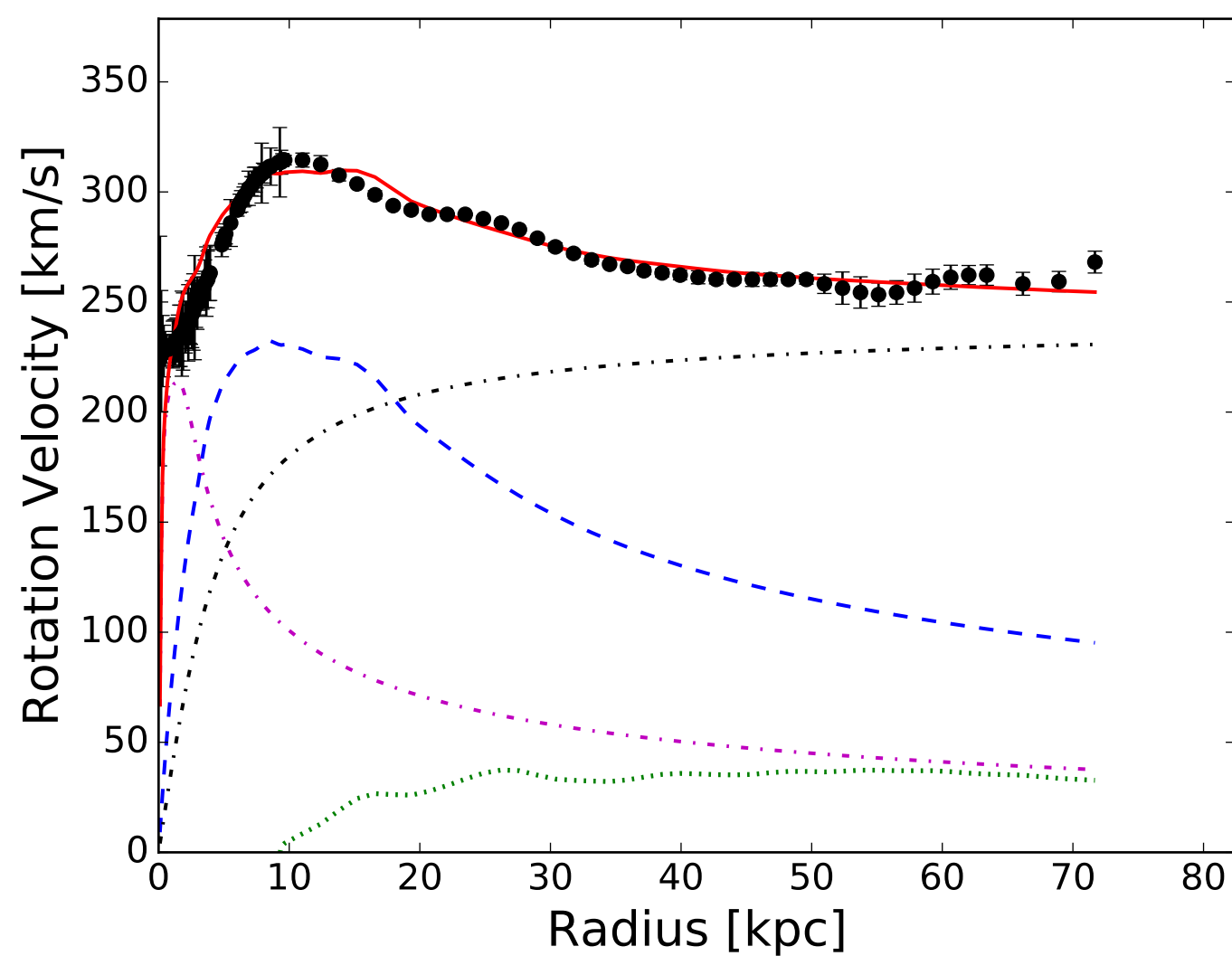
# Rotation curve fits: two halo models fit to three galaxies

ISO

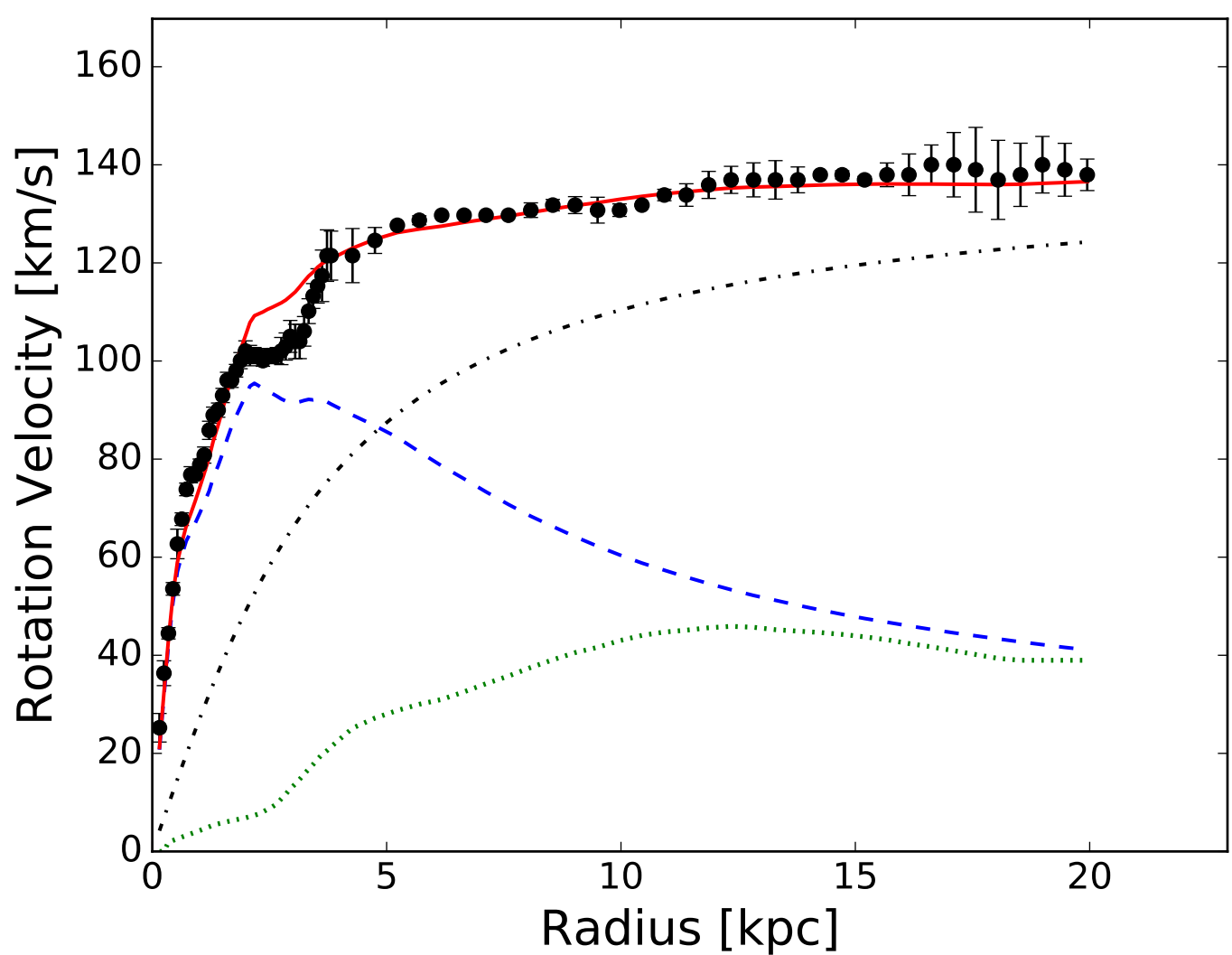
UGC 2885



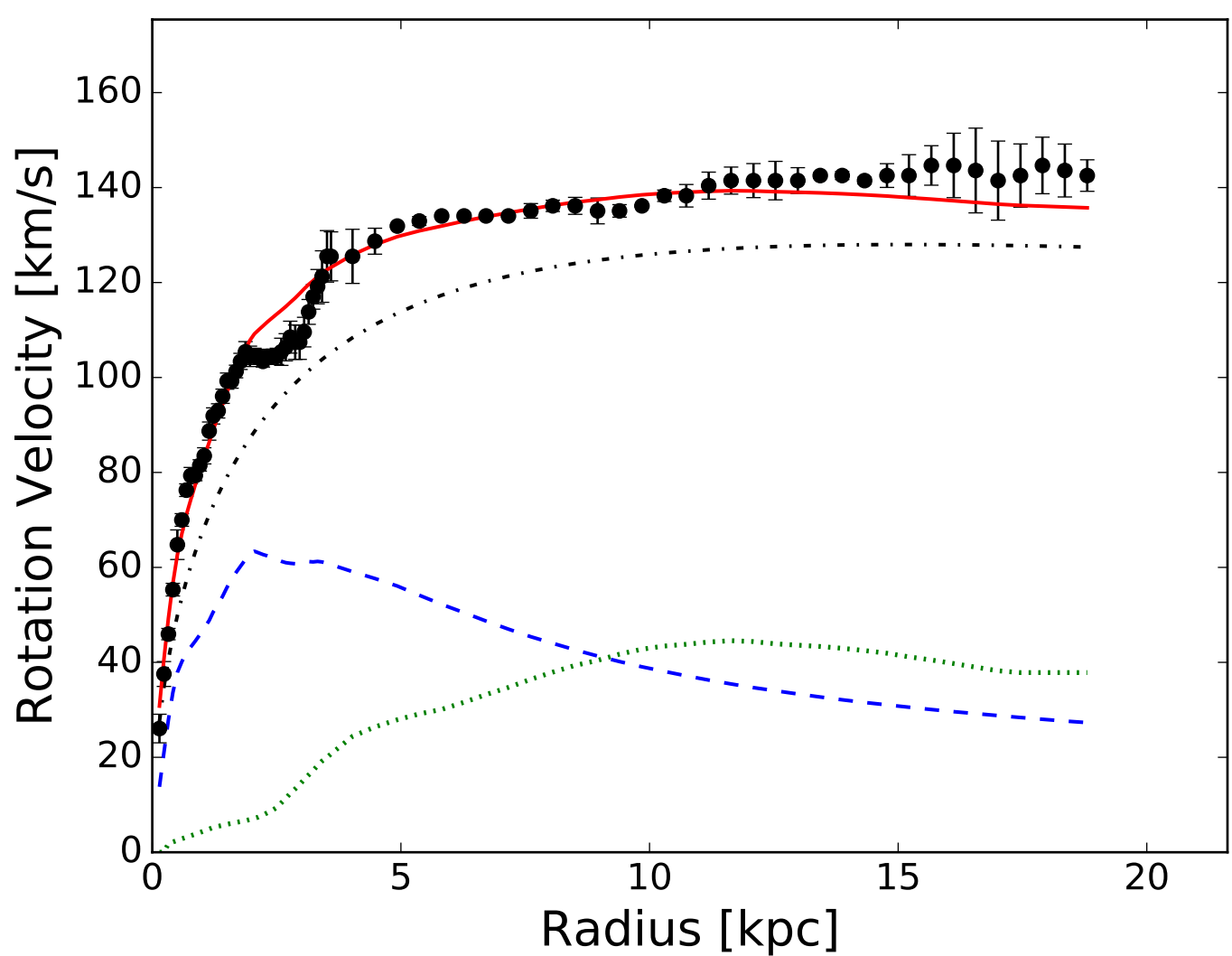
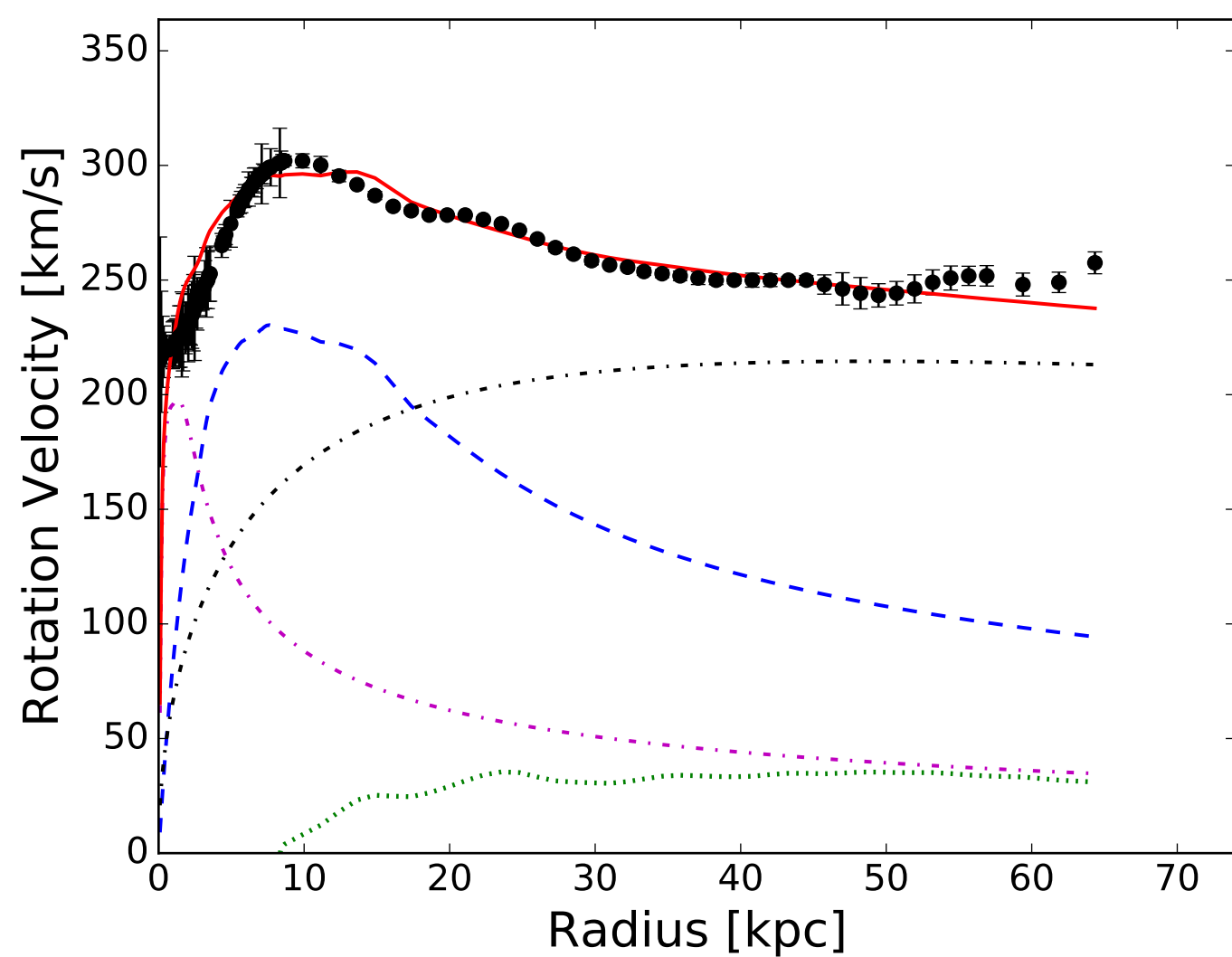
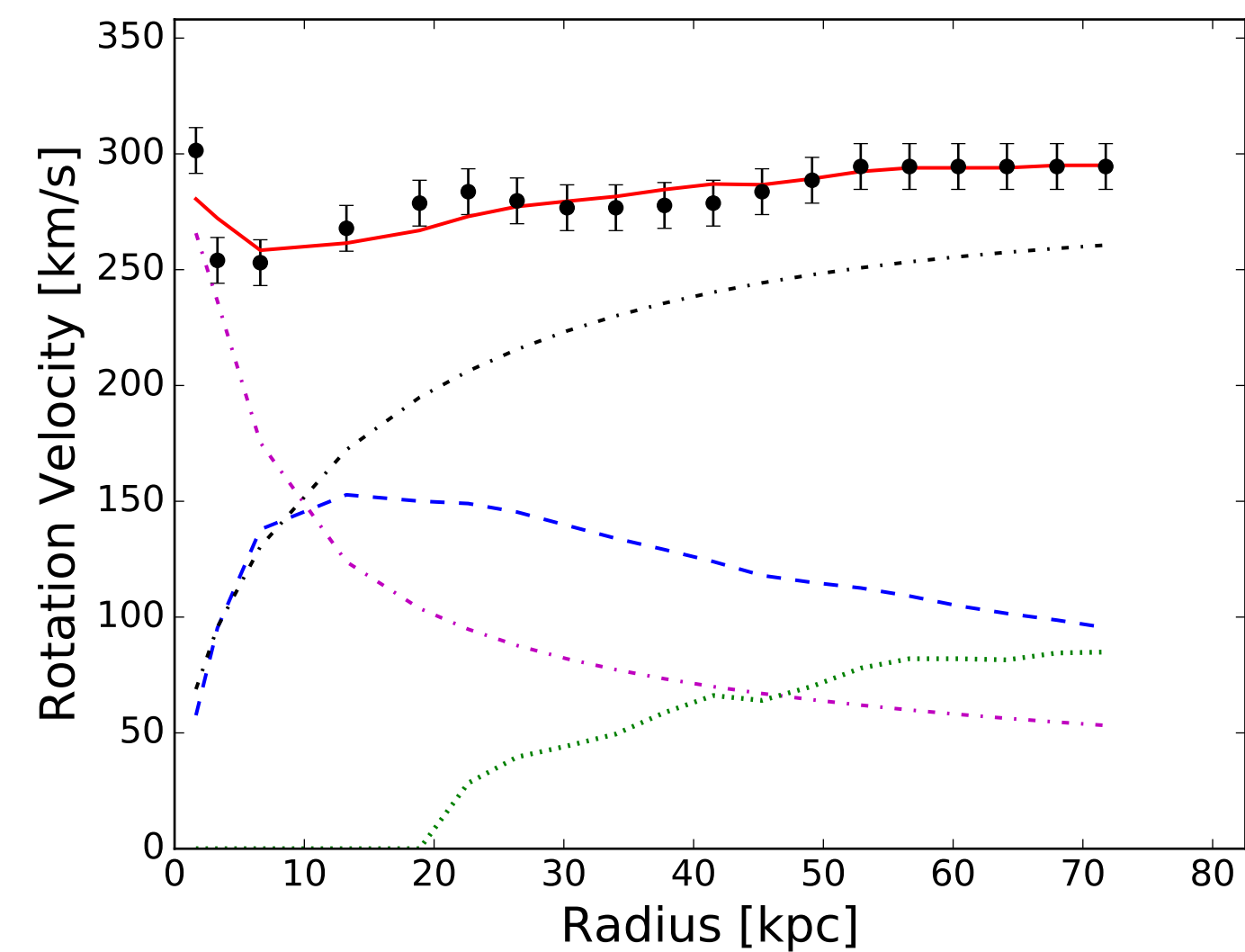
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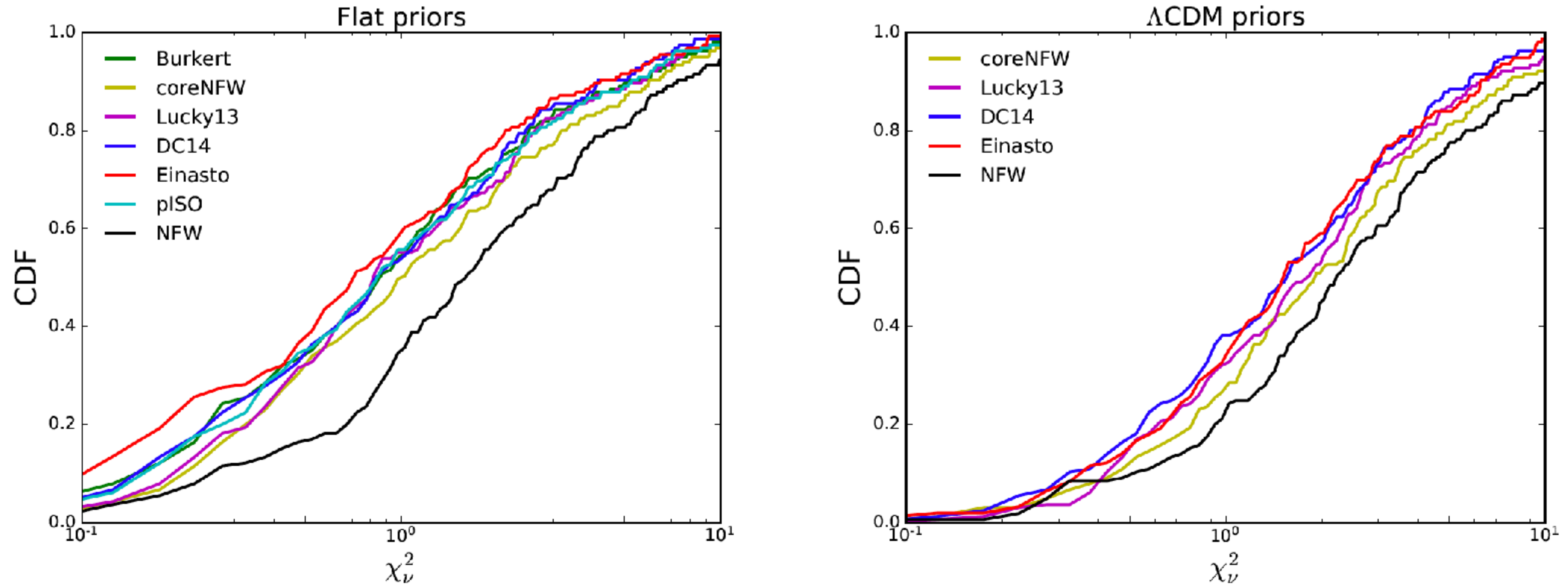
NGC 2403



NFW



# Cumulative distribution of $\chi_\nu^2$ for dark matter halo fits with different Bayesian priors



**Figure 1.** Cumulative distributions of the reduced  $\chi_\nu^2$  for seven halo profiles with flat (left) and  $\Lambda$ CDM priors (right).

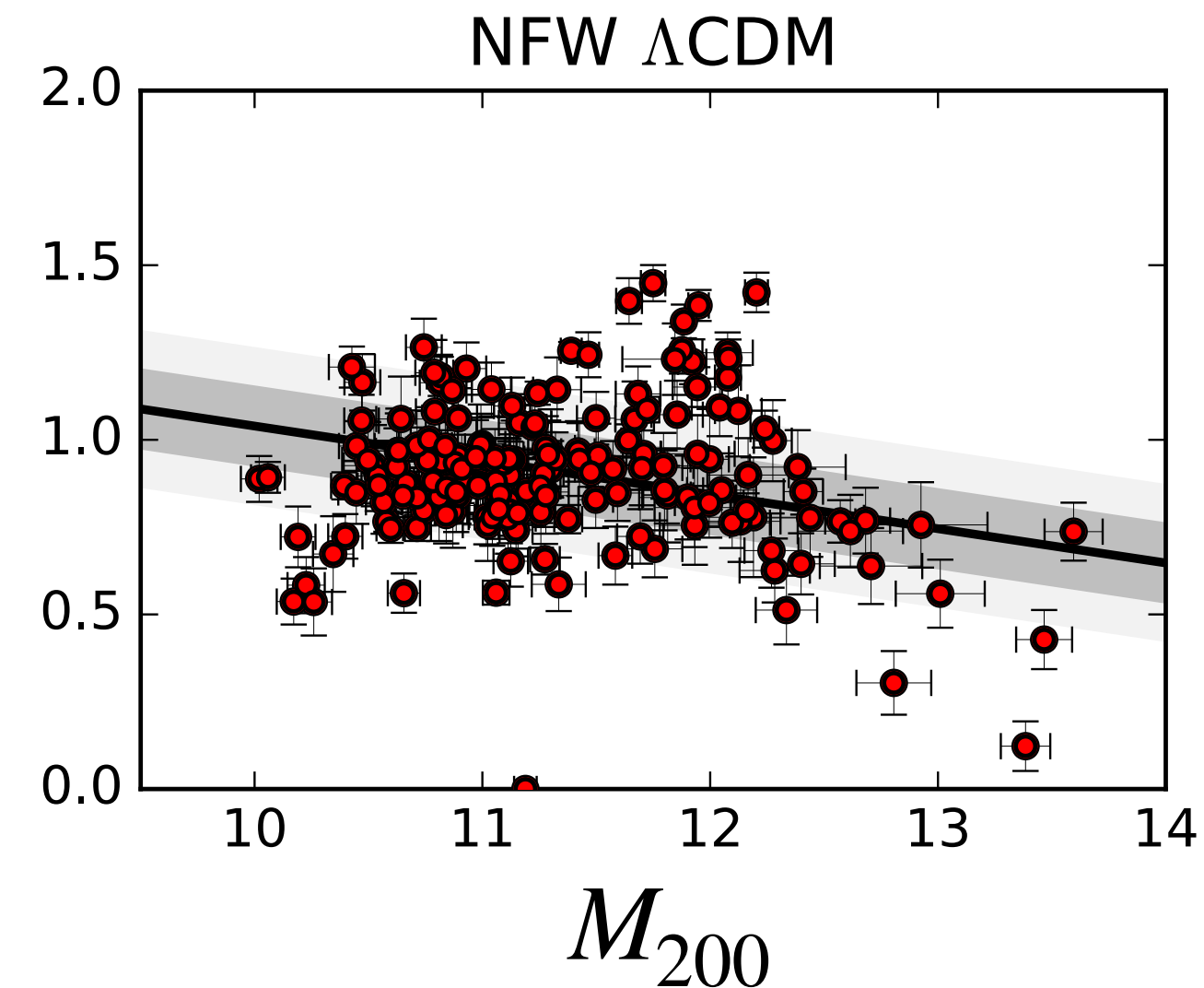
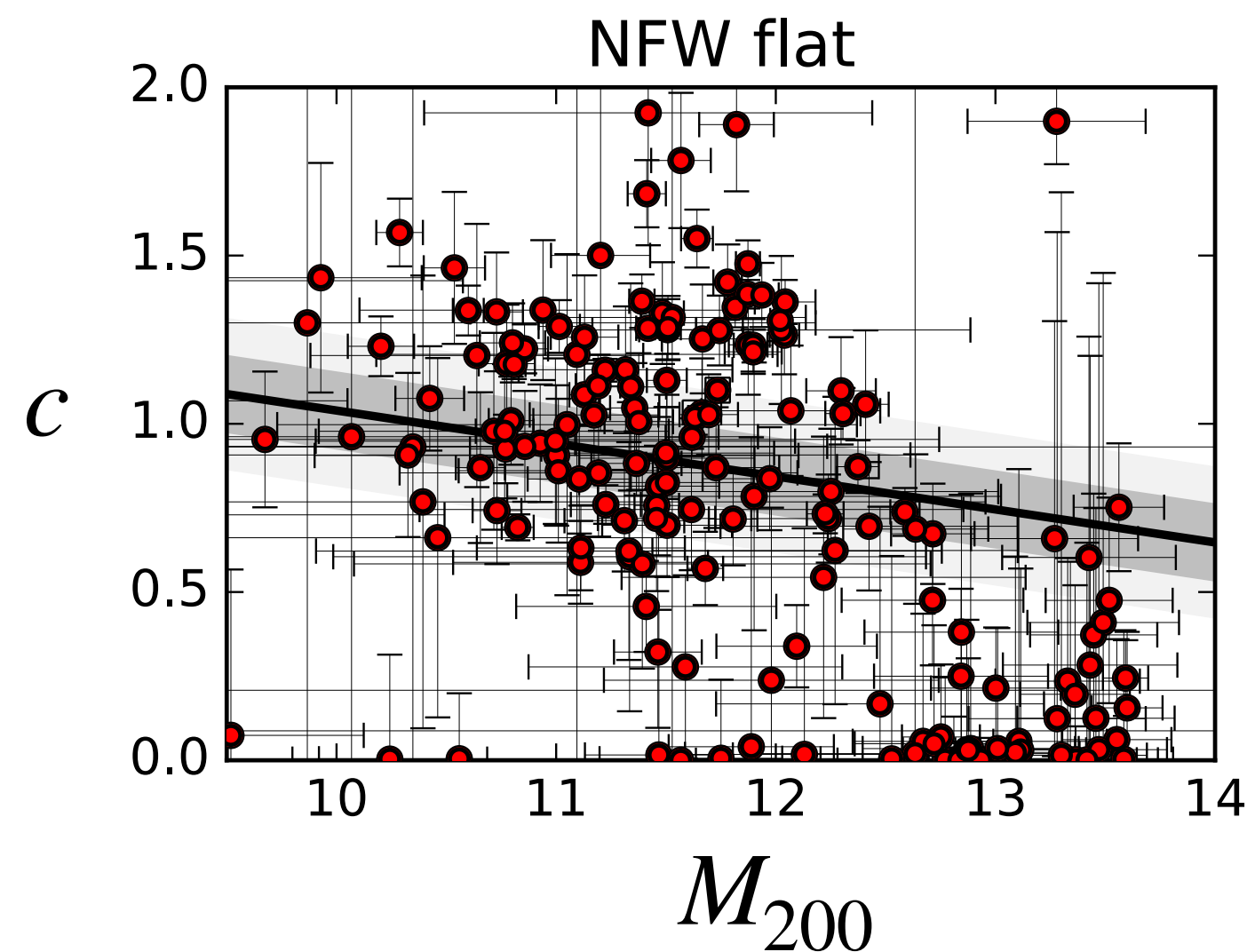
# $\Lambda$ CDM priors

## flat priors

## LCDM priors

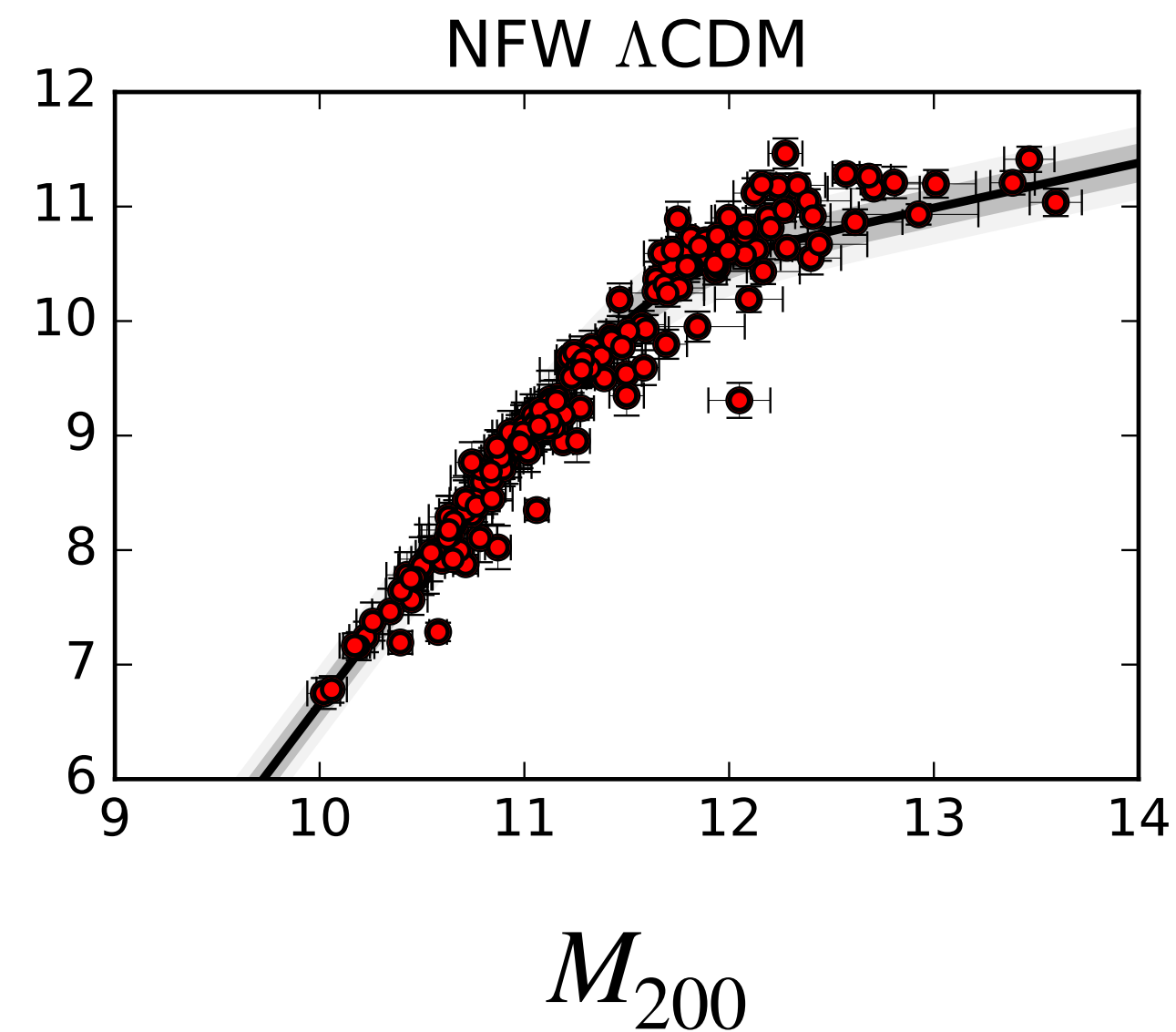
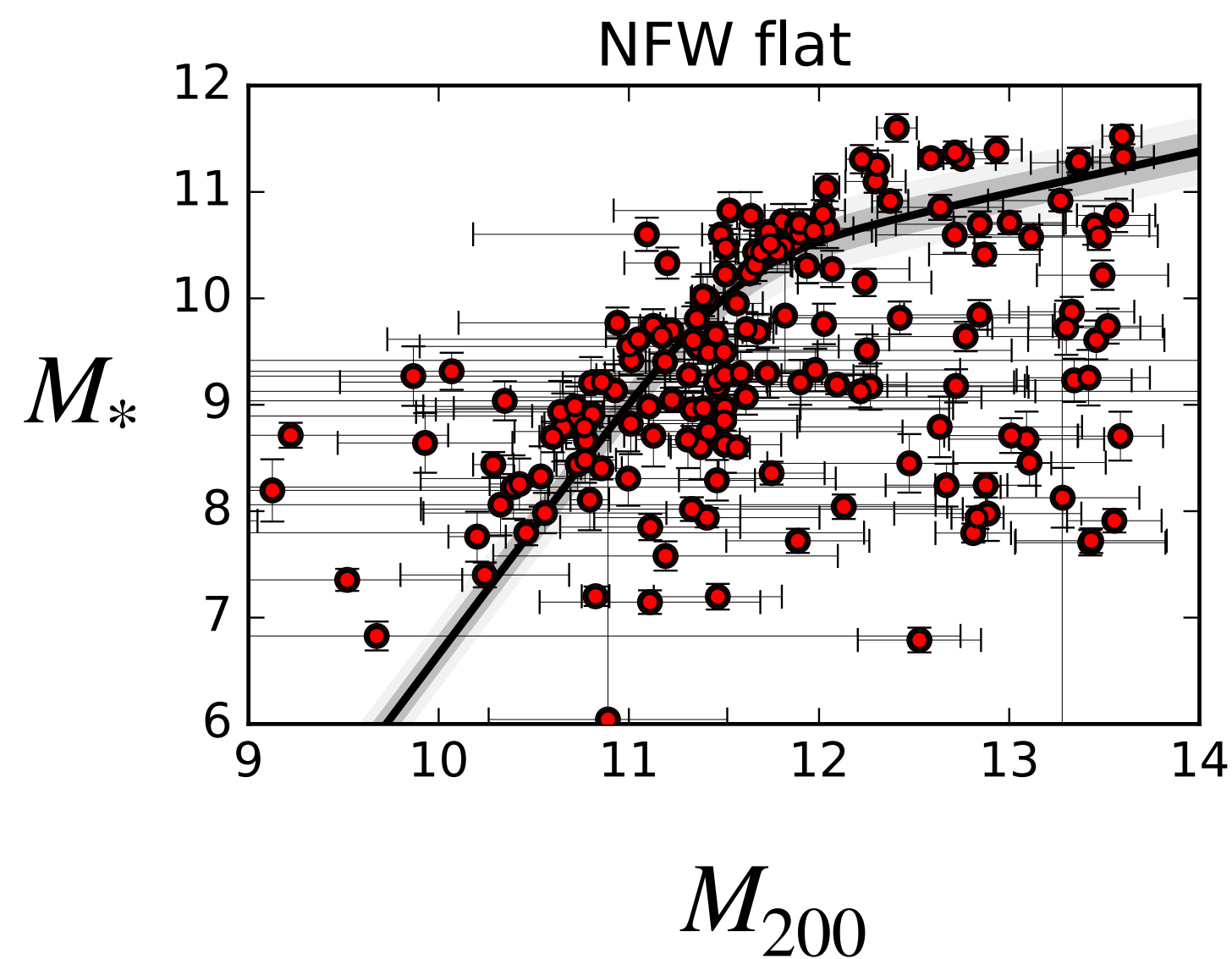
halo mass-concentration relation

$$c - M_{200}$$



stellar mass-halo mass relation

$$M_* - M_{200}$$



# Radial Acceleration Relation

The observed acceleration correlates with that predicted by the baryons

The data are well fit by

$$g_{\text{obs}} = \frac{g_{\text{bar}}}{1 - e^{-\sqrt{g_{\text{bar}}/g_{\dagger}}}}$$

$$g_{\dagger} = 1.20 \times 10^{-10} \text{ m s}^{-2}$$

$$\pm 0.02 \text{ (random)} \pm 0.24 \text{ (systematic)}$$

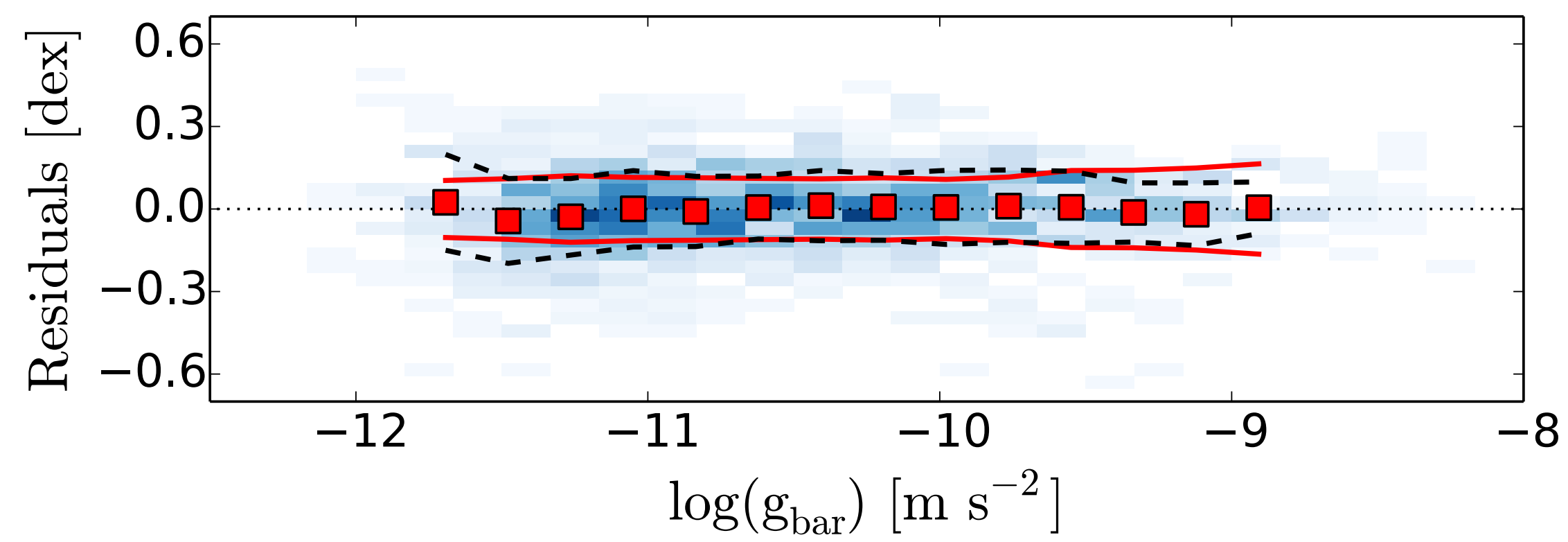
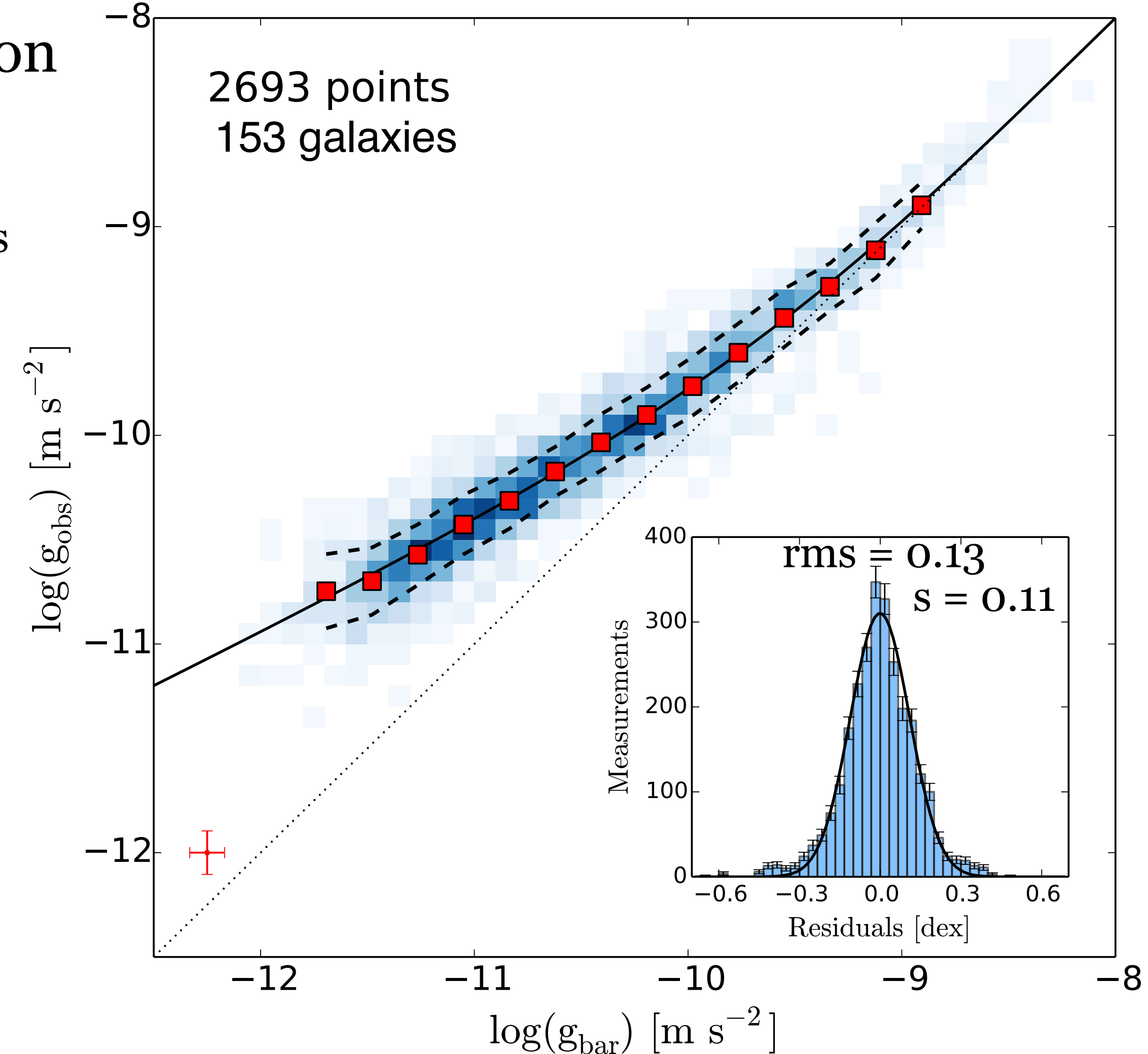
Lelli et al. (2017)

McGaugh et al. (2016)

observed rms scatter

scatter expected from  
observational errors

The data are consistent with  
zero intrinsic scatter





The Radial Acceleration Relation can be used to infer the dark matter distribution just by looking at a galaxy.

total

$$g_{\text{obs}} = \mathcal{F}(g_{\text{bar}})$$

$$\mathcal{F} = \frac{g_{\text{bar}}}{1 - e^{-\sqrt{g_{\text{bar}}/g_{\dagger}}}}$$

dark  
matter

$$g_{\text{DM}} = g_{\text{obs}} - g_{\text{bar}}$$

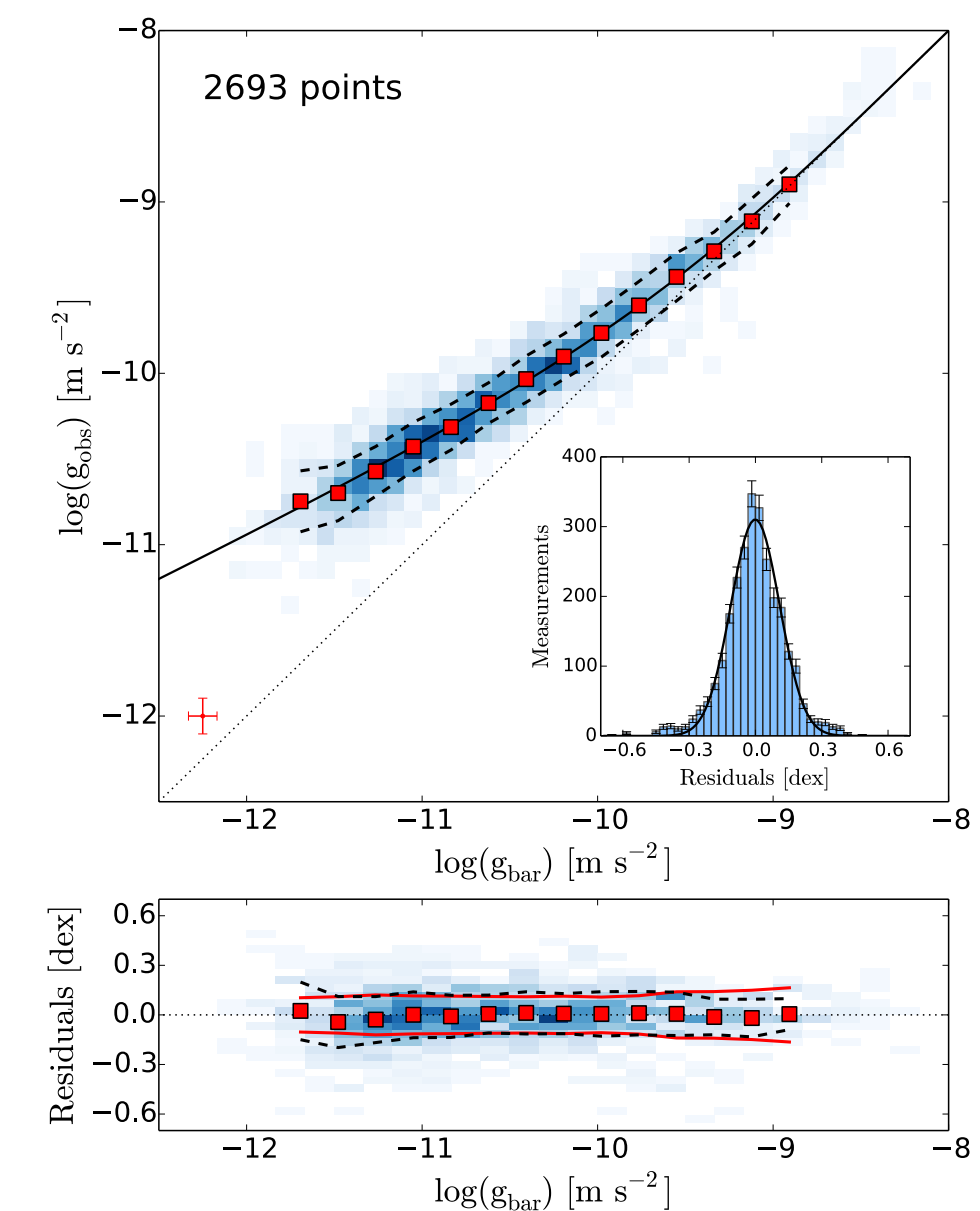
$$g_{\dagger} = 1.20 \times 10^{-10} \text{ m s}^{-2}$$

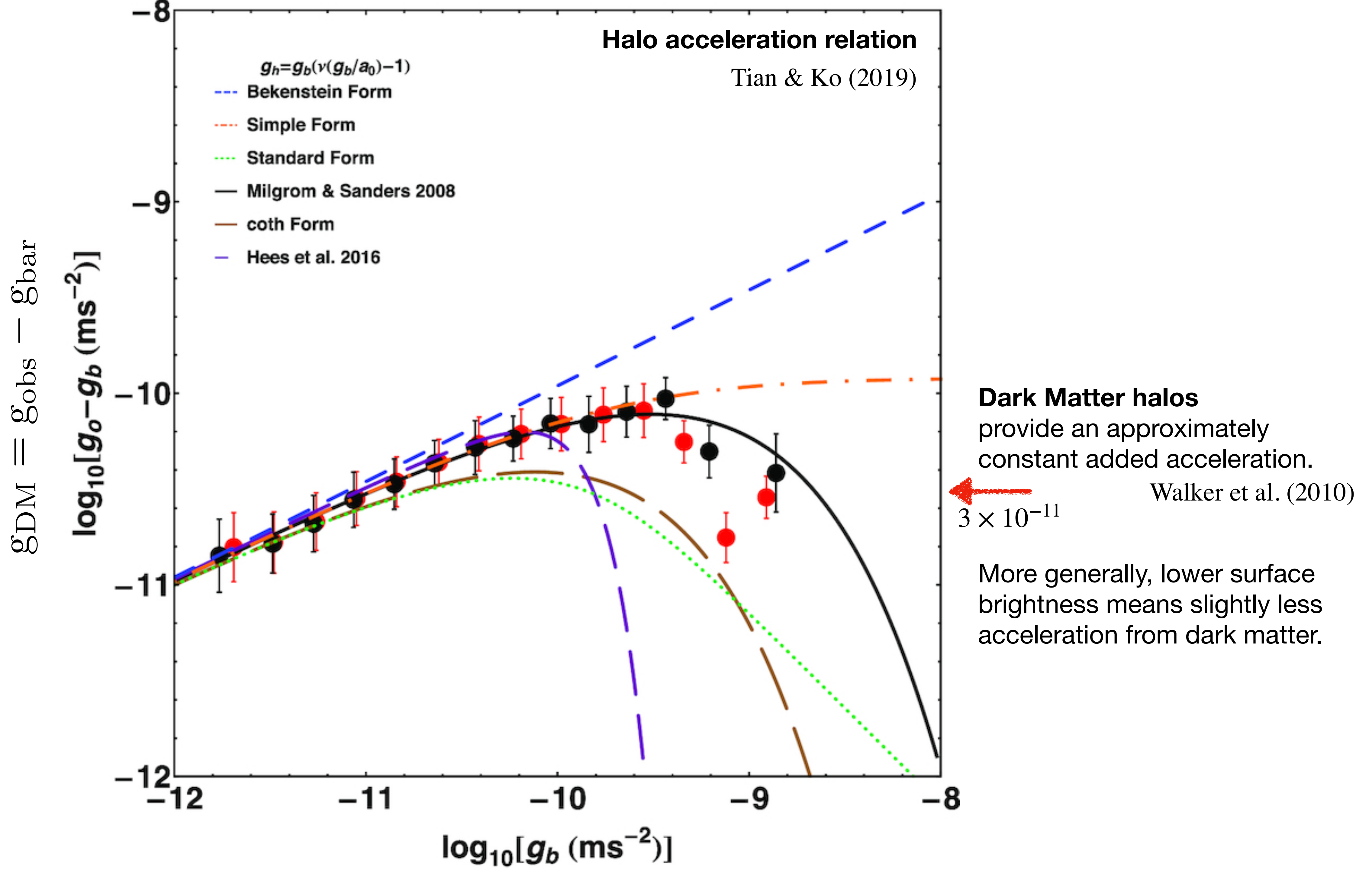
$$\pm 0.02 \text{ (random)} \pm 0.24 \text{ (systematic)}$$

$$g_{\text{DM}} = \mathcal{F}(g_{\text{bar}}) - g_{\text{bar}}$$

The dark matter distribution is specified by the baryon distribution

**That's weird**







# Galaxy Formation

A many faceted problem  
(sort of like Cthulhu being a multi-tentacled nightmare cult god)

Competition between gas accretion (to form disks) and lumpy fragments (forms spheroids, substructure)



## Monolithic galaxy formation collapse of one big gas cloud

(e.g., Eggen, Lynden-Bell, & Sandage 1962)

## Hierarchical galaxy formation

“bottom up” formation from sequence of mergers

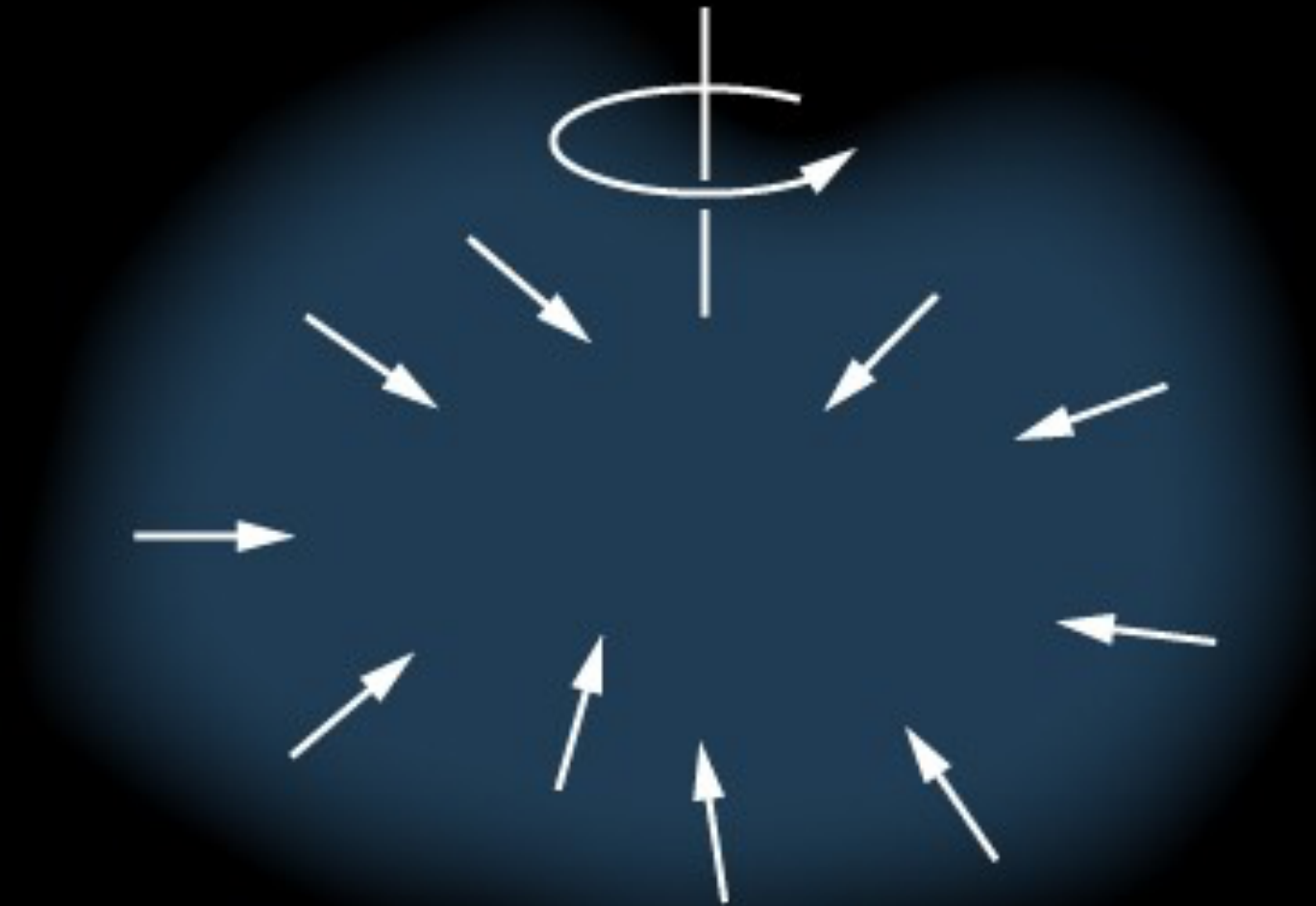
(big galaxies are built up with small galaxies - modern picture with CDM)

## Searle-Zinn (1978) fragments:

“...halo [globular] clusters originated within transient protogalactic fragments that gradually lost gas while undergoing chemical evolution and continued to fall into the Galaxy after the collapse of its central regions had been completed.”

# Monolithic galaxy formation

1 gas starts to collapse

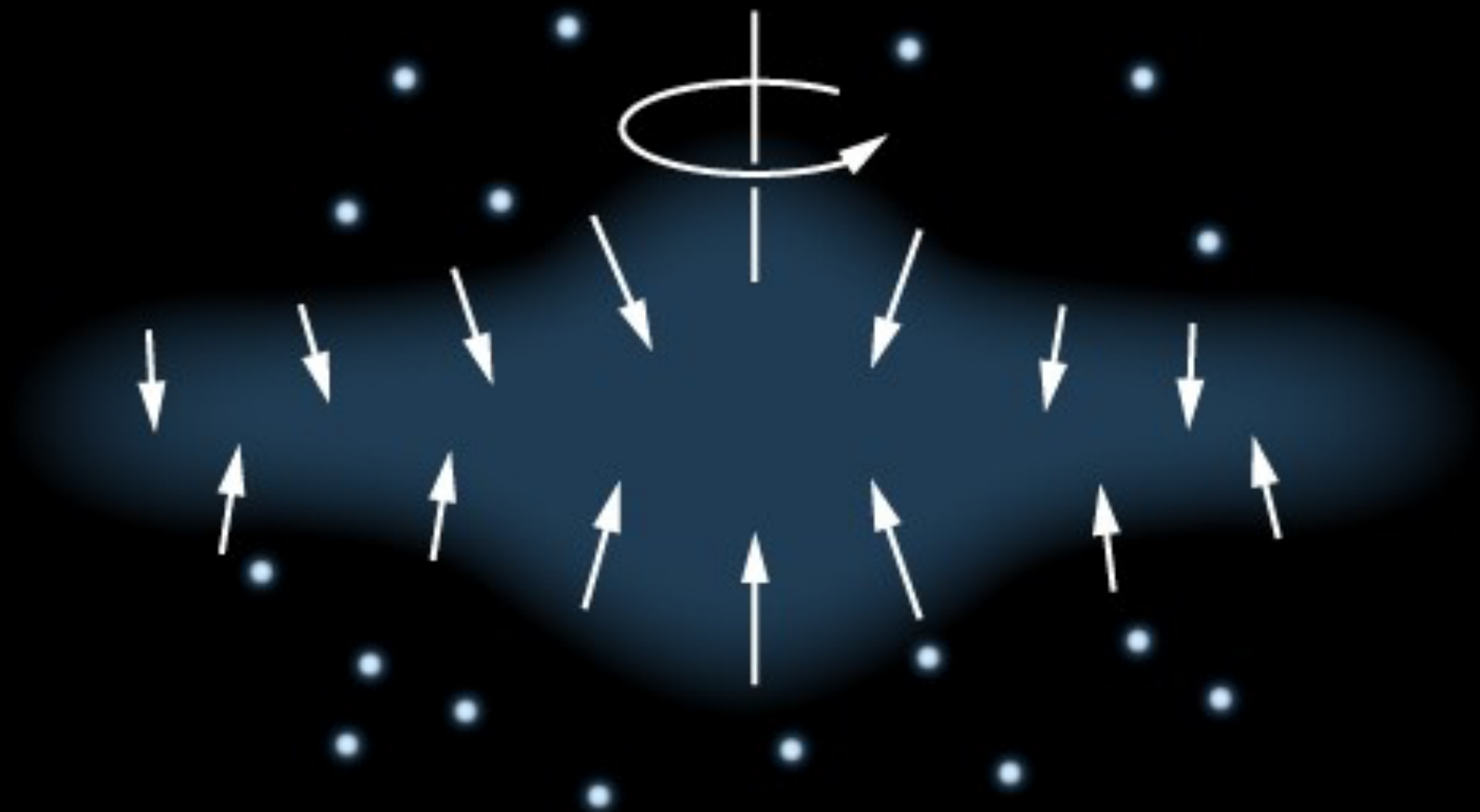


2 first stars form during collapse



retain memory of infall in their radial orbits

3 gas settles into disk



plane of disk specified by initial angular momentum

4 stars form in disk



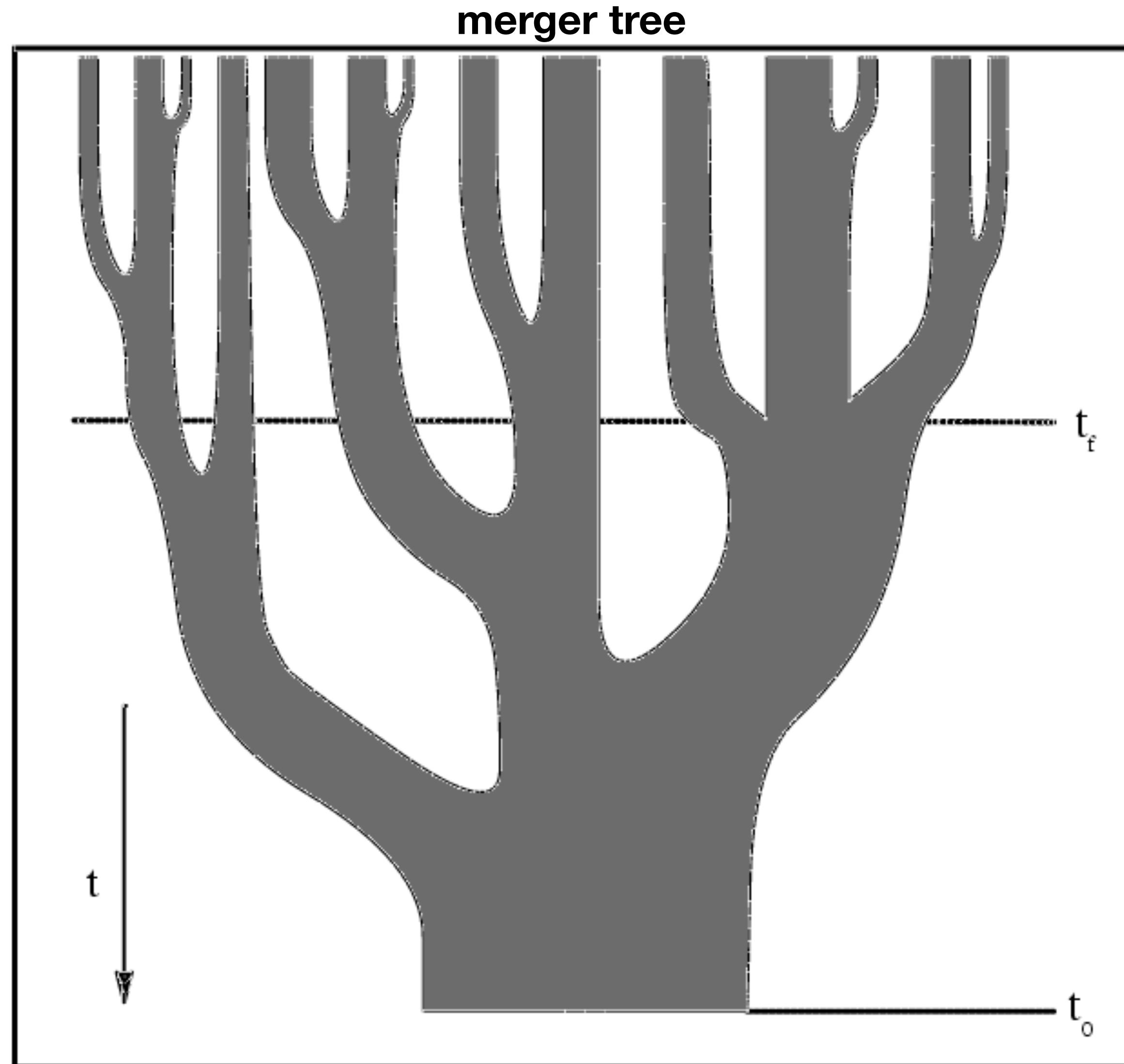
Good at forming spiral galaxies

# Hierarchical galaxy formation (bottom up - *not* monolithic)

Small objects  
conglomerate to  
make big ones

Gas dissipates and cools to  
form thin disks.

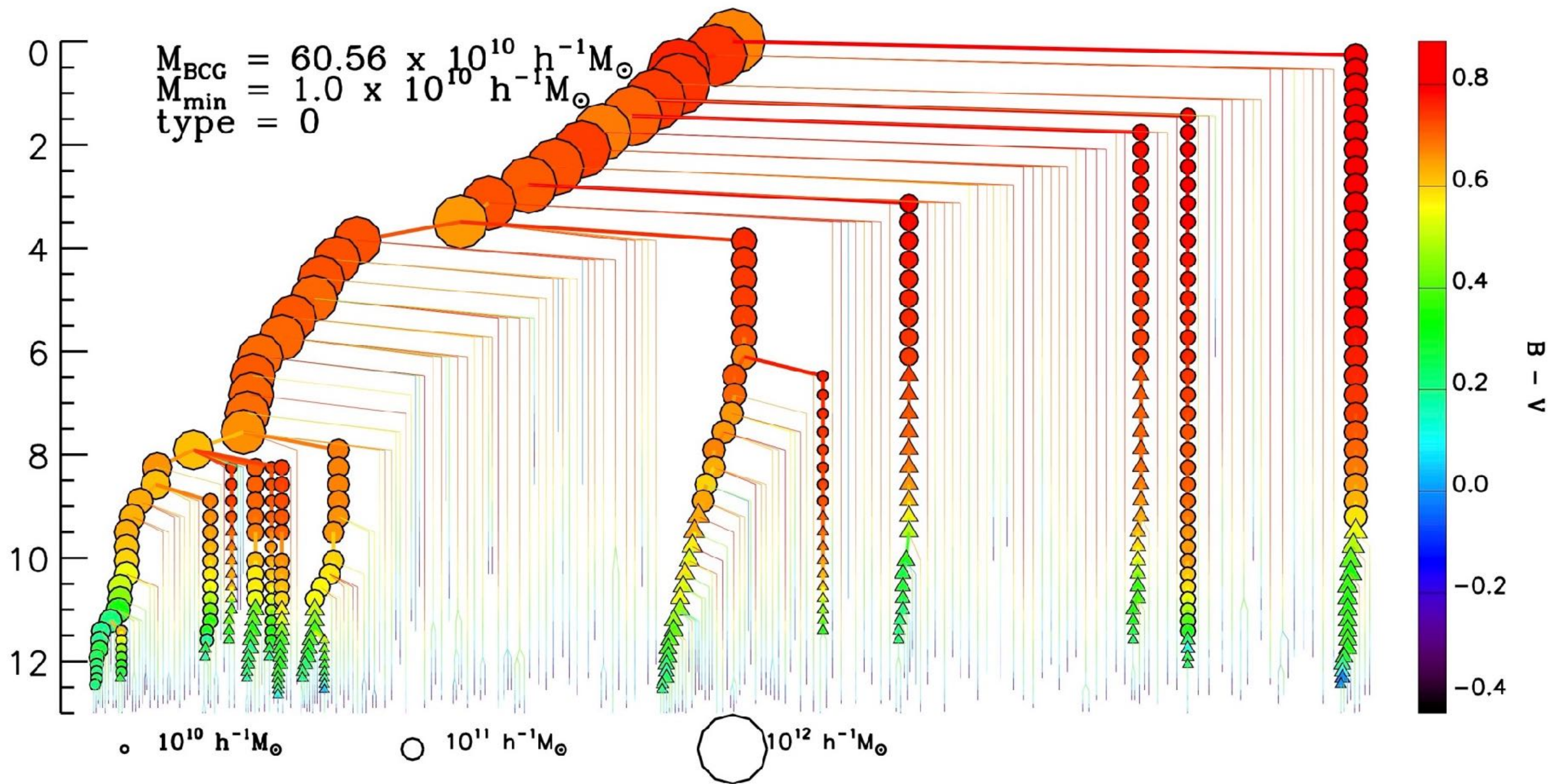
Stars cannot cool: if hot  
coming in, stay hot.



**Figure 6.** A schematic representation of a “merger tree” depicting the growth of a halo as the result of a series of mergers. Time increases from top to bottom in this figure and the widths of the branches of the tree represent the masses of the individual parent halos. Slicing through the tree horizontally gives the distribution of masses in the parent halos at a given time. The present time  $t_0$  and the formation time  $t_f$  are marked by horizontal lines, where the formation time is defined as the time at which a parent halo containing in excess of half of the mass of the final halo was first created.



lookback time (Gyr)





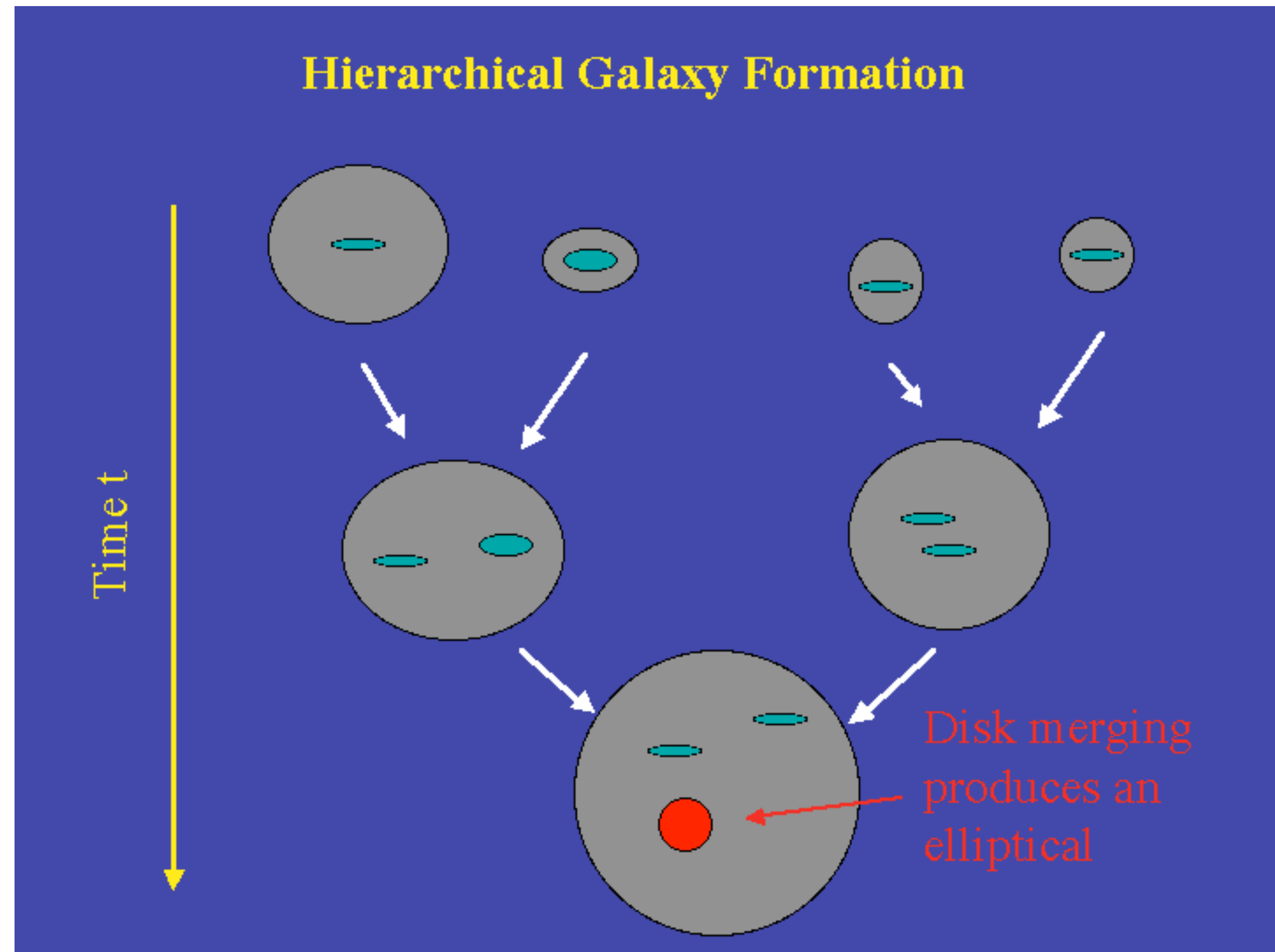
## merging subhalos containing protogalaxies

Gray:  
dark matter halos

Blue:  
gas rich disks

Red:  
elliptical merger  
remnant

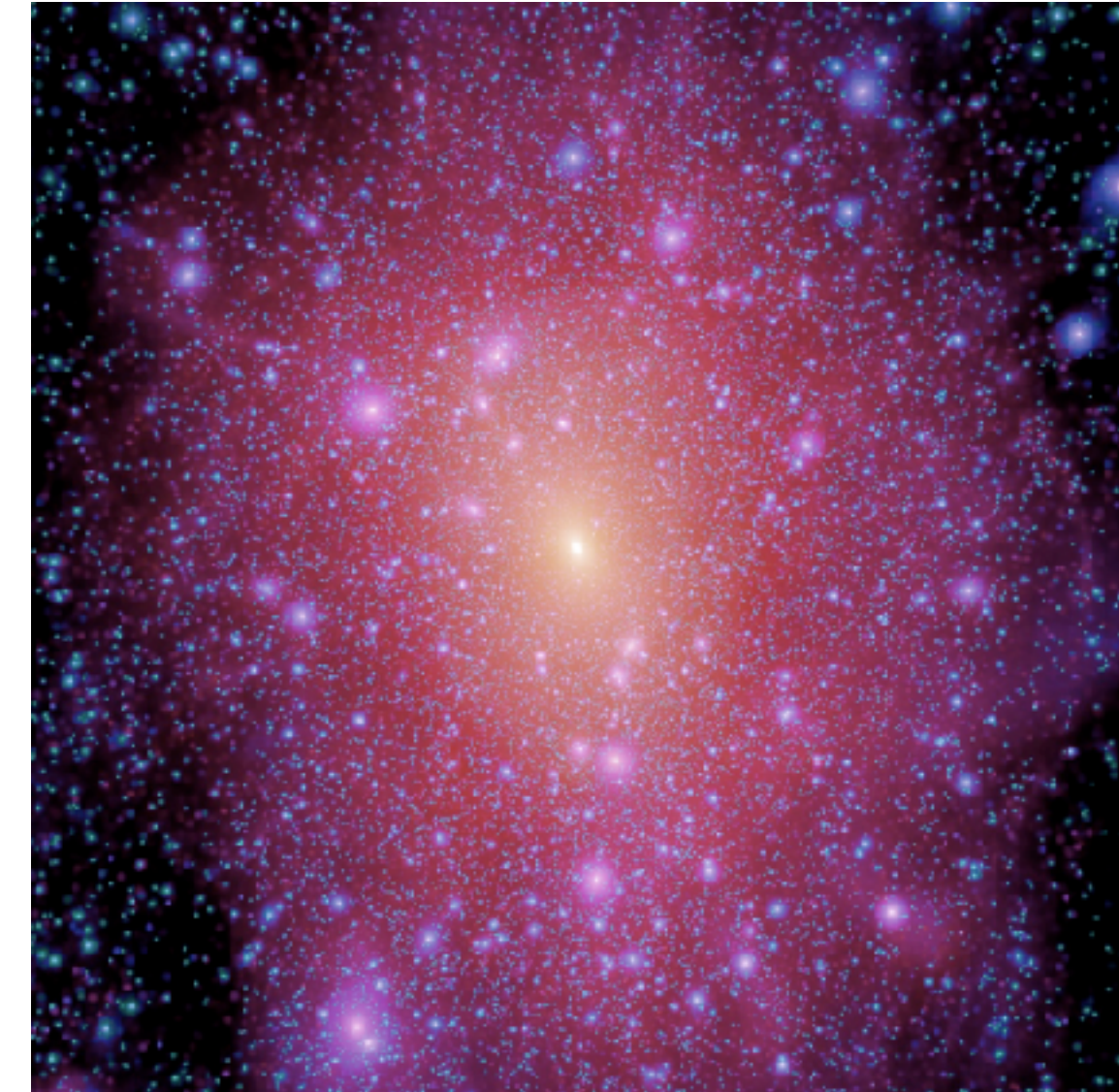
sometimes it is  
imagined that a disk  
re-forms around an  
elliptical to form a  
bulge+disk system  
like and Sa galaxy



**Good at forming elliptical galaxies**

# Sequence of events in galaxy formation

1. Dark matter halos form; merge into ever larger masses
2. Baryons fall into the potential wells of DM halos
3. Gas dissipates, sinks to centers of DM halos
  - Halos compressed by sinking baryons
  - gas forms rotating disks at centers of DM halos
4. Stars form in disks
  - Feedback heats gas, dissuading further gas accretion
5. Mergers transform some disks into ellipticals
  - star formation truncated
6. Renewed gas accretion may re-form disks around ellipticals
  - thus becoming the bulges of S0s and early type spirals
7. Merging lessens; more gradual accretion of dark matter and gas may continue
8. Galaxies





# Sequence of events in galaxy formation

1. Dark matter halos form; merge into ever larger masses

$$c_{200} = \frac{R_{200}}{r_s}$$

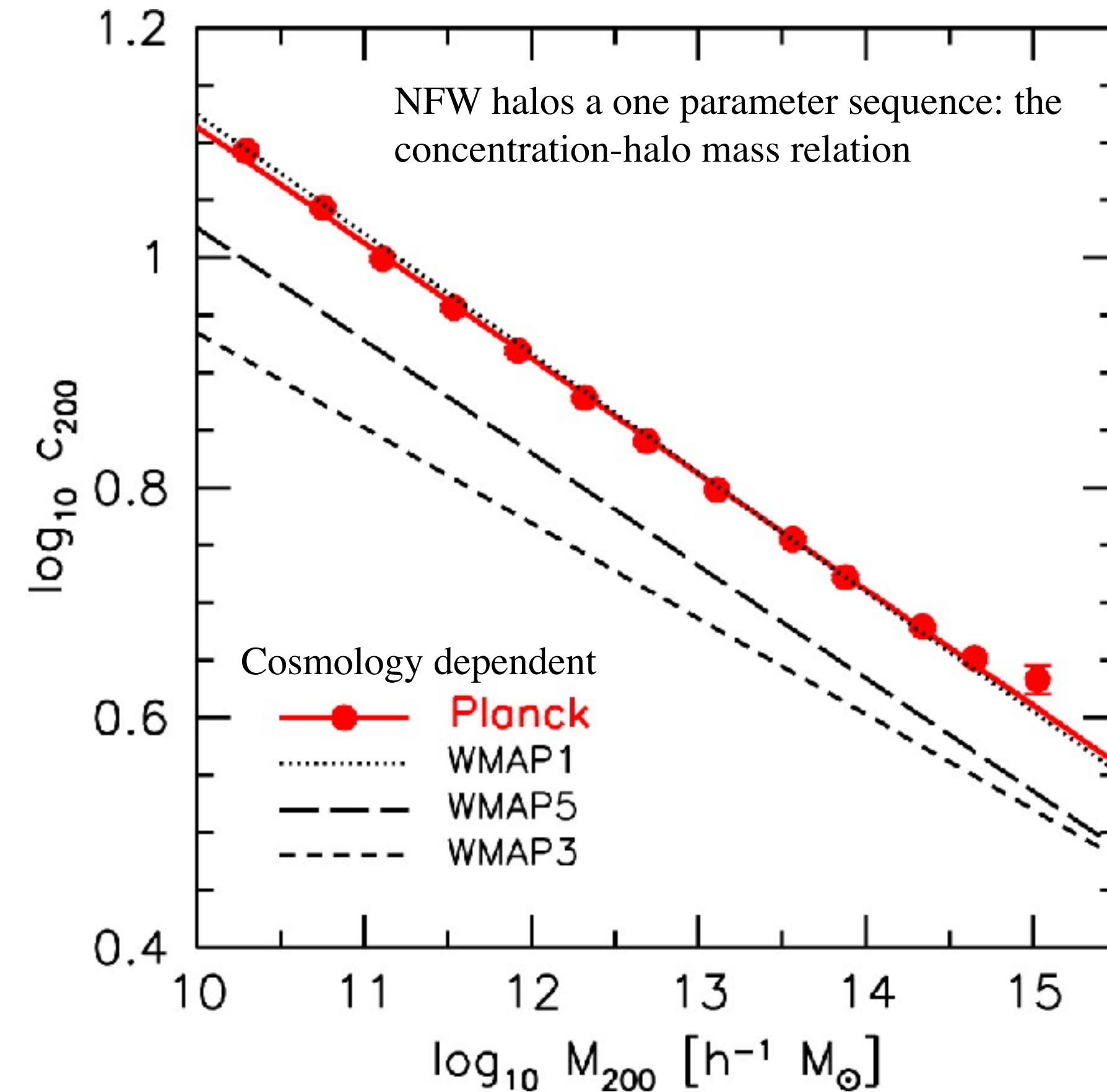
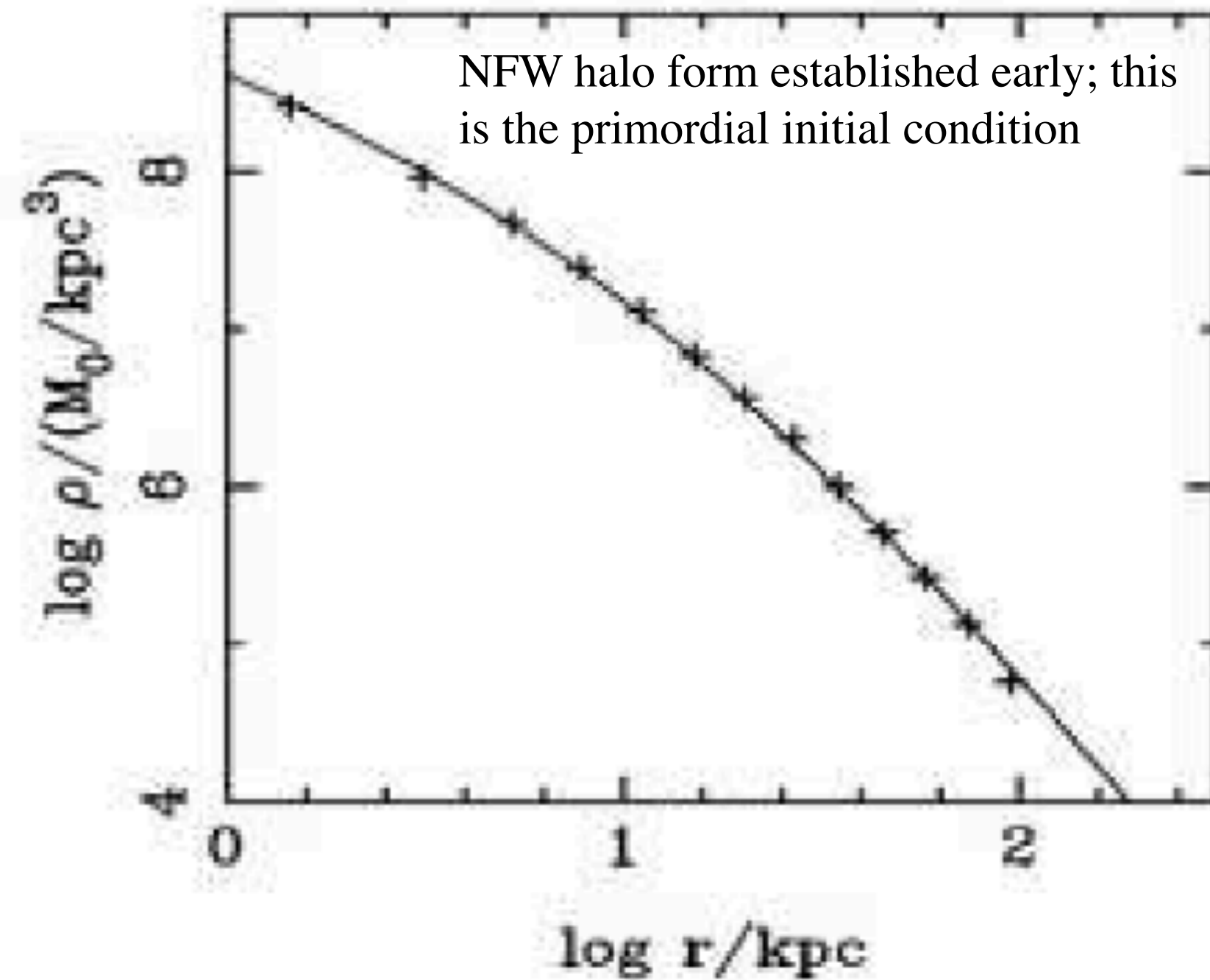


FIG. 1: Density profile of the million particle dark matter halo simulation of Dubinski & Carlberg 1990 (crosses). The solid line shows the best fit NFW profile (Eqn. 1) to the original data. This Figure was adapted from<sup>22</sup> by John Dubinski and it is reproduced here with his permission.

# Sequence of events in galaxy formation

## 1. Dark matter halos form; merge into ever larger masses

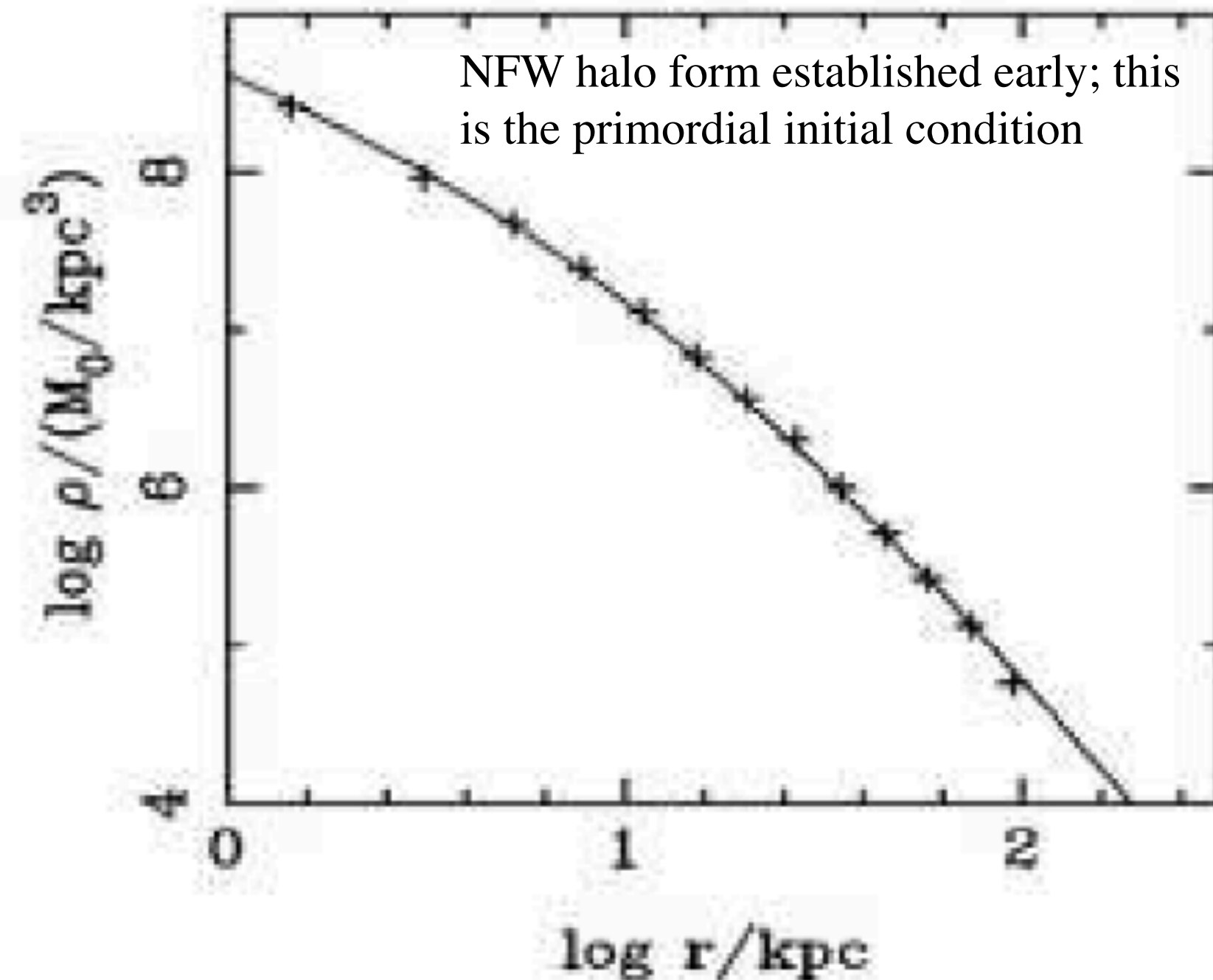


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Halo mass correlates with halo size and the circular speed at the virial radius:

$$M_{\Delta} = \frac{4\pi}{3} \Delta \rho_{crit} R_{\Delta}^3$$

for  $\Delta = 200$

$$V_{200} = R_{200} h$$

$$M_{200} = (3.3 \times 10^5 M_{\odot} \text{ km}^{-3} \text{ s}^3) V_{200}^3$$

This is often cited as the cosmic origin of the Tully-Fisher relation, but must include fudge factors

$$M_* = m_* M_{200}$$

$$V_f = f_V V_{200}$$